



## *College Algebra with Trigonometry*

This course covers the topics outlined below. You can customize the scope and sequence of this course to meet your curricular needs.

### Curriculum (582 topics)

- Algebra and Geometry Review (184 topics)
  - ◆ Real Numbers and Algebraic Expressions (18 topics)
    - ◇ Ordering integers
    - ◇ Identifying numbers as integers or non-integers
    - ◇ Identifying numbers as rational or irrational
    - ◇ Signed fraction addition or subtraction: Basic
    - ◇ Signed fraction subtraction involving double negation
    - ◇ Signed fraction multiplication: Basic
    - ◇ Signed fraction division
    - ◇ Exponents and integers: Problem type 1
    - ◇ Exponents and integers: Problem type 2
    - ◇ Exponents and signed fractions
    - ◇ Order of operations with integers
    - ◇ Order of operations with integers and exponents
    - ◇ Evaluating a linear expression: Integer multiplication with addition or subtraction
    - ◇ Evaluating a quadratic expression: Integers
    - ◇ Evaluating a linear expression: Signed fraction multiplication with addition or subtraction
    - ◇ Distributive property: Integer coefficients
    - ◇ Using distribution and combining like terms to simplify: Univariate
    - ◇ Using distribution with double negation and combining like terms to simplify: Multivariate
  - ◆ Exponents (28 topics)
    - ◇ Introduction to the product rule of exponents
    - ◇ Product rule with positive exponents: Univariate
    - ◇ Product rule with positive exponents: Multivariate
    - ◇ Introduction to the power of a power rule of exponents
    - ◇ Introduction to the power of a product rule of exponents
    - ◇ Power rules with positive exponents: Multivariate products
    - ◇ Power rules with positive exponents: Multivariate quotients
    - ◇ Power and product rules with positive exponents
    - ◇ Simplifying a ratio of multivariate monomials: Basic
    - ◇ Introduction to the quotient rule of exponents
    - ◇ Simplifying a ratio of univariate monomials
    - ◇ Quotient of expressions involving exponents
    - ◇ Simplifying a ratio of multivariate monomials: Advanced
    - ◇ Power and quotient rules with positive exponents
    - ◇ Evaluating expressions with exponents of zero
    - ◇ Evaluating an expression with a negative exponent: Whole number base
    - ◇ Evaluating an expression with a negative exponent: Positive fraction base
    - ◇ Evaluating an expression with a negative exponent: Negative integer base
    - ◇ Rewriting an algebraic expression without a negative exponent

- ◇ Introduction to the product rule with negative exponents
- ◇ Product rule with negative exponents
- ◇ Quotient rule with negative exponents: Problem type 1
- ◇ Quotient rule with negative exponents: Problem type 2
- ◇ Power of a power rule with negative exponents
- ◇ Power rules with negative exponents
- ◇ Power and quotient rules with negative exponents: Problem type 1
- ◇ Power and quotient rules with negative exponents: Problem type 2
- ◇ Power, product, and quotient rules with negative exponents
- ◆ Polynomial Expressions (15 topics)
  - ◇ Degree and leading coefficient of a univariate polynomial
  - ◇ Simplifying a sum or difference of two univariate polynomials
  - ◇ Multiplying a univariate polynomial by a monomial with a positive coefficient
  - ◇ Multiplying a univariate polynomial by a monomial with a negative coefficient
  - ◇ Multiplying a multivariate polynomial by a monomial
  - ◇ Multiplying binomials with leading coefficients of 1
  - ◇ Multiplying binomials with leading coefficients greater than 1
  - ◇ Multiplying binomials in two variables
  - ◇ Multiplying conjugate binomials: Univariate
  - ◇ Multiplying conjugate binomials: Multivariate
  - ◇ Squaring a binomial: Univariate
  - ◇ Squaring a binomial: Multivariate
  - ◇ Multiplying binomials with negative coefficients
  - ◇ Multiplication involving binomials and trinomials in one variable
  - ◇ Multiplication involving binomials and trinomials in two variables
- ◆ Factoring Polynomials (29 topics)
  - ◇ Greatest common factor of 2 numbers
  - ◇ Factoring a linear binomial
  - ◇ Introduction to the GCF of two monomials
  - ◇ Greatest common factor of three univariate monomials
  - ◇ Greatest common factor of two multivariate monomials
  - ◇ Factoring out a monomial from a polynomial: Univariate
  - ◇ Factoring out a monomial from a polynomial: Multivariate
  - ◇ Factoring out a binomial from a polynomial: Basic
  - ◇ Factoring a univariate polynomial by grouping: Problem type 1
  - ◇ Factoring a univariate polynomial by grouping: Problem type 2
  - ◇ Factoring a multivariate polynomial by grouping: Problem type 1
  - ◇ Factoring a quadratic with leading coefficient 1
  - ◇ Factoring a quadratic in two variables with leading coefficient 1
  - ◇ Factoring out a constant before factoring a quadratic
  - ◇ Factoring a quadratic with leading coefficient greater than 1: Problem type 1
  - ◇ Factoring a quadratic with leading coefficient greater than 1: Problem type 2
  - ◇ Factoring a quadratic with leading coefficient greater than 1: Problem type 3
  - ◇ Factoring a quadratic in two variables with leading coefficient greater than 1
  - ◇ Factoring a quadratic with a negative leading coefficient
  - ◇ Factoring a perfect square trinomial with leading coefficient 1
  - ◇ Factoring a perfect square trinomial with leading coefficient greater than 1
  - ◇ Factoring a difference of squares in one variable: Basic
  - ◇ Factoring a difference of squares in one variable: Advanced
  - ◇ Factoring a difference of squares in two variables
  - ◇ Factoring a polynomial involving a GCF and a difference of squares: Univariate
  - ◇ Factoring a product of a quadratic trinomial and a monomial
  - ◇ Factoring with repeated use of the difference of squares formula

- ◇ Factoring a sum or difference of two cubes
- ◇ Factoring out a binomial from a polynomial: Advanced
- ◆ Rational Expressions (43 topics)
  - ◇ Restriction on a variable in a denominator: Linear
  - ◇ Simplifying a ratio of factored polynomials: Linear factors
  - ◇ Simplifying a ratio of polynomials using GCF factoring
  - ◇ Simplifying a ratio of linear polynomials: 1,  $-1$ , and no simplification
  - ◇ Simplifying a ratio of polynomials by factoring a quadratic with leading coefficient 1
  - ◇ Simplifying a ratio of polynomials: Problem type 1
  - ◇ Simplifying a ratio of polynomials: Problem type 2
  - ◇ Multiplying rational expressions involving multivariate monomials
  - ◇ Multiplying rational expressions made up of linear expressions
  - ◇ Multiplying rational expressions involving quadratics with leading coefficients of 1
  - ◇ Dividing rational expressions involving multivariate monomials
  - ◇ Dividing rational expressions involving linear expressions
  - ◇ Dividing rational expressions involving quadratics with leading coefficients of 1
  - ◇ Least common multiple of 2 numbers
  - ◇ Least common multiple of 3 numbers
  - ◇ Introduction to the LCM of two monomials
  - ◇ Finding the LCD of rational expressions with linear denominators: Relatively prime
  - ◇ Finding the LCD of rational expressions with linear denominators: Common factors
  - ◇ Writing equivalent rational expressions with monomial denominators
  - ◇ Writing equivalent rational expressions with polynomial denominators
  - ◇ Writing equivalent rational expressions involving opposite factors
  - ◇ Introduction to adding fractions with variables and common denominators
  - ◇ Adding rational expressions with common denominators and monomial numerators
  - ◇ Adding rational expressions with common denominators and binomial numerators
  - ◇ Adding rational expressions with common denominators and GCF factoring
  - ◇ Adding rational expressions with common denominators and quadratic factoring
  - ◇ Adding rational expressions with different denominators and a single occurrence of a variable
  - ◇ Adding rational expressions with denominators  $ax$  and  $bx$ : Basic
  - ◇ Adding rational expressions with denominators  $ax$  and  $bx$ : Advanced
  - ◇ Adding rational expressions with denominators  $ax^n$  and  $bx^m$
  - ◇ Adding rational expressions with linear denominators without common factors: Basic
  - ◇ Adding rational expressions with linear denominators without common factors: Advanced
  - ◇ Adding rational expressions with linear denominators with common factors: Basic
  - ◇ Adding rational expressions with denominators  $ax-b$  and  $b-ax$
  - ◇ Complex fraction without variables: Problem type 1
  - ◇ Complex fraction without variables: Problem type 2
  - ◇ Complex fraction involving univariate monomials
  - ◇ Complex fraction: GCF factoring
  - ◇ Complex fraction: Quadratic factoring
  - ◇ Complex fraction made of sums involving rational expressions: Problem type 1
  - ◇ Complex fraction made of sums involving rational expressions: Problem type 2
  - ◇ Complex fraction made of sums involving rational expressions: Problem type 3
  - ◇ Complex fraction made of sums involving rational expressions: Problem type 4
- ◆ Perfect Squares and  $n$ th Roots (10 topics)
  - ◇ Finding all square roots of a number
  - ◇ Square root of a rational perfect square
  - ◇ Square roots of perfect squares with signs
  - ◇ Square roots of integers raised to even exponents
  - ◇ Introduction to simplifying a radical expression with an even exponent
  - ◇ Square root of a perfect square monomial

- ◇ Introduction to solving an absolute value equation
- ◇ Cube root of an integer
- ◇ Finding  $n^{\text{th}}$  roots of perfect  $n^{\text{th}}$  powers with signs
- ◇ Finding the  $n^{\text{th}}$  root of a perfect  $n^{\text{th}}$  power monomial
- ◆ Rational Exponents (8 topics)
  - ◇ Converting between radical form and exponent form
  - ◇ Rational exponents: Unit fraction exponents and whole number bases
  - ◇ Rational exponents: Unit fraction exponents and bases involving signs
  - ◇ Rational exponents: Non–unit fraction exponent with a whole number base
  - ◇ Rational exponents: Negative exponents and fractional bases
  - ◇ Rational exponents: Product rule
  - ◇ Rational exponents: Quotient rule
  - ◇ Rational exponents: Power of a power rule
- ◆ Radical Expressions (28 topics)
  - ◇ Simplifying the square root of a whole number less than 100
  - ◇ Simplifying the square root of a whole number greater than 100
  - ◇ Simplifying a radical expression with an even exponent
  - ◇ Introduction to simplifying a radical expression with an odd exponent
  - ◇ Simplifying a radical expression with an odd exponent
  - ◇ Simplifying a radical expression with two variables
  - ◇ Simplifying a higher root of a whole number
  - ◇ Introduction to simplifying a higher radical expression
  - ◇ Simplifying a higher radical expression: Univariate
  - ◇ Introduction to square root addition or subtraction
  - ◇ Square root addition or subtraction
  - ◇ Introduction to simplifying a sum or difference of radical expressions: Univariate
  - ◇ Simplifying a sum or difference of radical expressions: Univariate
  - ◇ Introduction to square root multiplication
  - ◇ Square root multiplication: Basic
  - ◇ Square root multiplication: Advanced
  - ◇ Introduction to simplifying a product of radical expressions: Univariate
  - ◇ Simplifying a product of radical expressions: Univariate
  - ◇ Introduction to simplifying a product involving square roots using the distributive property
  - ◇ Simplifying a product involving square roots using the distributive property: Basic
  - ◇ Simplifying a product involving square roots using the distributive property: Advanced
  - ◇ Special products of radical expressions: Conjugates and squaring
  - ◇ Simplifying a quotient of square roots
  - ◇ Simplifying a quotient involving a sum or difference with a square root
  - ◇ Rationalizing a denominator: Quotient involving square roots
  - ◇ Rationalizing a denominator: Square root of a fraction
  - ◇ Rationalizing a denominator using conjugates: Integer numerator
  - ◇ Rationalizing a denominator using conjugates: Square root in numerator
- ◆ Geometry (5 topics)
  - ◇ Circumference of a circle
  - ◇ Volume of a rectangular prism
  - ◇ Introduction to the Pythagorean Theorem
  - ◇ Pythagorean Theorem
  - ◇ Word problem involving the Pythagorean Theorem
- Equations and Inequalities (118 topics)
  - ◆ Linear Equations and Applications (34 topics)
    - ◇ Additive property of equality with signed fractions
    - ◇ Multiplicative property of equality with signed fractions
    - ◇ Solving a multi–step equation given in fractional form

- ◇ Solving a linear equation with several occurrences of the variable: Variables on the same side and distribution
- ◇ Solving a linear equation with several occurrences of the variable: Variables on both sides and distribution
- ◇ Solving a linear equation with several occurrences of the variable: Variables on both sides and two distributions
- ◇ Solving a linear equation with several occurrences of the variable: Fractional forms with monomial numerators
- ◇ Solving a two-step equation with signed fractions
- ◇ Solving a linear equation with several occurrences of the variable: Variables on both sides and fractional coefficients
- ◇ Solving a linear equation with several occurrences of the variable: Fractional forms with binomial numerators
- ◇ Solving equations with zero, one, or infinitely many solutions
- ◇ Solving a proportion of the form  $(x+a)/b = c/d$
- ◇ Solving for a variable in terms of other variables using addition or subtraction: Basic
- ◇ Solving for a variable in terms of other variables using addition or subtraction: Advanced
- ◇ Solving for a variable in terms of other variables using multiplication or division: Basic
- ◇ Solving for a variable in terms of other variables using multiplication or division: Advanced
- ◇ Solving for a variable in terms of other variables using addition or subtraction with division
- ◇ Solving for a variable inside parentheses in terms of other variables
- ◇ Solving for a variable in terms of other variables in a linear equation with fractions
- ◇ Translating a sentence into a one-step equation
- ◇ Translating a sentence into a multi-step equation
- ◇ Solving a word problem with two unknowns using a linear equation
- ◇ Solving a decimal word problem using a linear equation of the form  $Ax + B = C$
- ◇ Solving a word problem with three unknowns using a linear equation
- ◇ Writing a multi-step equation for a real-world situation
- ◇ Solving a value mixture problem using a linear equation
- ◇ Solving a one-step word problem using the formula  $d = rt$
- ◇ Solving a distance, rate, time problem using a linear equation
- ◇ Finding the perimeter or area of a rectangle given one of these values
- ◇ Finding the multiplier to give a final amount after a percentage increase or decrease
- ◇ Finding the sale price given the original price and percent discount
- ◇ Computing a percent mixture
- ◇ Solving a percent mixture problem using a linear equation
- ◇ Finding simple interest without a calculator
- ◆ Absolute Value Equations (4 topics)
  - ◇ Solving an absolute value equation: Problem type 1
  - ◇ Solving an absolute value equation: Problem type 2
  - ◇ Solving an absolute value equation: Problem type 3
  - ◇ Solving an absolute value equation: Problem type 4
- ◆ Linear Inequalities and Applications (21 topics)
  - ◇ Translating a sentence into a one-step inequality
  - ◇ Translating a sentence into a multi-step inequality
  - ◇ Writing an inequality for a real-world situation
  - ◇ Graphing a linear inequality on the number line
  - ◇ Translating a sentence into a compound inequality
  - ◇ Graphing a compound inequality on the number line
  - ◇ Set builder and interval notation
  - ◇ Union and intersection of finite sets
  - ◇ Union and intersection of intervals
  - ◇ Identifying solutions to a two-step linear inequality in one variable

- ◇ Additive property of inequality with signed fractions
- ◇ Multiplicative property of inequality with signed fractions
- ◇ Solving a two–step linear inequality: Problem type 1
- ◇ Solving a two–step linear inequality: Problem type 2
- ◇ Solving a two–step linear inequality with a fractional coefficient
- ◇ Solving a linear inequality with multiple occurrences of the variable: Problem type 1
- ◇ Solving a linear inequality with multiple occurrences of the variable: Problem type 2
- ◇ Solving a linear inequality with multiple occurrences of the variable: Problem type 3
- ◇ Solving a compound linear inequality: Graph solution, basic
- ◇ Solving a decimal word problem using a two–step linear inequality
- ◇ Solving a decimal word problem using a linear inequality with the variable on both sides
- ◆ Absolute Value Inequalities (5 topics)
  - ◇ Solving an absolute value inequality: Problem type 1
  - ◇ Solving an absolute value inequality: Problem type 2
  - ◇ Solving an absolute value inequality: Problem type 3
  - ◇ Solving an absolute value inequality: Problem type 4
  - ◇ Solving an absolute value inequality: Problem type 5
- ◆ Rational Equations that Simplify to Linear (9 topics)
  - ◇ Solving a proportion of the form  $a/(x+b) = c/x$
  - ◇ Solving a rational equation that simplifies to linear: Denominator  $x$
  - ◇ Solving a rational equation that simplifies to linear: Denominator  $x+a$
  - ◇ Solving a rational equation that simplifies to linear: Denominators  $a$ ,  $x$ , or  $ax$
  - ◇ Solving a rational equation that simplifies to linear: Denominators  $ax$  and  $bx$
  - ◇ Solving a rational equation that simplifies to linear: Like binomial denominators
  - ◇ Solving a rational equation that simplifies to linear: Unlike binomial denominators
  - ◇ Solving for a variable in terms of other variables in a rational equation: Problem type 1
  - ◇ Solving for a variable in terms of other variables in a rational equation: Problem type 2
- ◆ Complex Numbers (6 topics)
  - ◇ Using  $i$  to rewrite square roots of negative numbers
  - ◇ Simplifying a product and quotient involving square roots of negative numbers
  - ◇ Adding or subtracting complex numbers
  - ◇ Multiplying complex numbers
  - ◇ Dividing complex numbers
  - ◇ Simplifying a power of  $i$
- ◆ Quadratic Equations (20 topics)
  - ◇ Solving an equation written in factored form
  - ◇ Finding the roots of a quadratic equation of the form  $ax^2 + bx = 0$
  - ◇ Finding the roots of a quadratic equation with leading coefficient 1
  - ◇ Finding the roots of a quadratic equation with leading coefficient greater than 1
  - ◇ Solving a quadratic equation needing simplification
  - ◇ Roots of a product of polynomials
  - ◇ Writing a quadratic equation given the roots and the leading coefficient
  - ◇ Solving a word problem using a quadratic equation with rational roots
  - ◇ Solving an equation of the form  $x^2 = a$  using the square root property
  - ◇ Solving a quadratic equation using the square root property: Exact answers, basic
  - ◇ Solving a quadratic equation using the square root property: Exact answers, advanced
  - ◇ Completing the square
  - ◇ Solving a quadratic equation by completing the square: Exact answers
  - ◇ Applying the quadratic formula: Exact answers
  - ◇ Applying the quadratic formula: Decimal answers
  - ◇ Solving a quadratic equation with complex roots
  - ◇ Discriminant of a quadratic equation
  - ◇ Solving a word problem using a quadratic equation with irrational roots

- ◊ Solving an equation using the odd–root property: Problem type 1
- ◊ Solving an equation using the odd–root property: Problem type 2
- ◆ Rational Equations that Simplify to Quadratic (6 topics)
  - ◊ Restriction on a variable in a denominator: Quadratic
  - ◊ Solving a rational equation that simplifies to linear: Factorable quadratic denominator
  - ◊ Solving a rational equation that simplifies to quadratic: Proportional form, basic
  - ◊ Solving a rational equation that simplifies to quadratic: Denominator  $x$
  - ◊ Solving a rational equation that simplifies to quadratic: Binomial denominators, constant numerators
  - ◊ Solving a rational equation that simplifies to quadratic: Binomial denominators and numerators
- ◆ Radical Equations (13 topics)
  - ◊ Introduction to solving a radical equation
  - ◊ Solving a radical equation that simplifies to a linear equation: One radical, basic
  - ◊ Solving a radical equation that simplifies to a linear equation: One radical, advanced
  - ◊ Solving a radical equation that simplifies to a linear equation: Two radicals
  - ◊ Solving a radical equation that simplifies to a quadratic equation: One radical, basic
  - ◊ Solving a radical equation that simplifies to a quadratic equation: One radical, advanced
  - ◊ Solving a radical equation that simplifies to a quadratic equation: Two radicals
  - ◊ Algebraic symbol manipulation with radicals
  - ◊ Word problem involving radical equations: Basic
  - ◊ Word problem involving radical equations: Advanced
  - ◊ Solving an equation with a root index greater than 2: Problem type 1
  - ◊ Solving an equation with a root index greater than 2: Problem type 2
  - ◊ Solving an equation that can be written in quadratic form: Problem type 1
- Graphs and Functions (116 topics)
  - ◆ Graphs of Equations (20 topics)
    - ◊ Reading a point in the coordinate plane
    - ◊ Plotting a point in the coordinate plane
    - ◊ Table for a linear equation
    - ◊ Identifying solutions to a linear equation in two variables
    - ◊ Finding a solution to a linear equation in two variables
    - ◊ Graphing a linear equation of the form  $y = mx$
    - ◊ Graphing a line given its equation in slope–intercept form: Integer slope
    - ◊ Graphing a line given its equation in slope–intercept form: Fractional slope
    - ◊ Graphing a line given its equation in standard form
    - ◊ Graphing a vertical or horizontal line
    - ◊ Finding  $x$ – and  $y$ –intercepts given the graph of a line on a grid
    - ◊ Finding  $x$ – and  $y$ –intercepts of a line given the equation: Basic
    - ◊ Finding  $x$ – and  $y$ –intercepts of a line given the equation: Advanced
    - ◊ Graphing a line given its  $x$ – and  $y$ –intercepts
    - ◊ Graphing a line by first finding its  $x$ – and  $y$ –intercepts
    - ◊ Finding intercepts of a nonlinear function given its graph
    - ◊ Graphing an absolute value equation of the form  $y = A|x|$
    - ◊ Graphing a parabola of the form  $y = ax^2$
    - ◊ Graphing a parabola of the form  $y = ax^2 + c$
    - ◊ Graphing a cubic function of the form  $y = ax^3$
  - ◆ Slope and Equations of Lines (20 topics)
    - ◊ Classifying slopes given graphs of lines
    - ◊ Finding slope given the graph of a line on a grid
    - ◊ Finding slope given two points on the line
    - ◊ Finding the slope of horizontal and vertical lines
    - ◊ Graphing a line given its slope and  $y$ –intercept
    - ◊ Graphing a line through a given point with a given slope
    - ◊ Rewriting a linear equation in the form  $Ax + By = C$

- ◇ Finding the slope and  $y$ -intercept of a line given its equation in the form  $y = mx + b$
- ◇ Finding the slope and  $y$ -intercept of a line given its equation in the form  $Ax + By = C$
- ◇ Graphing a line by first finding its slope and  $y$ -intercept
- ◇ Writing an equation of a line given its slope and  $y$ -intercept
- ◇ Writing an equation in slope-intercept form given the slope and a point
- ◇ Writing an equation in point-slope form given the slope and a point
- ◇ Writing an equation of a line given the  $y$ -intercept and another point
- ◇ Writing the equation of the line through two given points
- ◇ Writing the equations of vertical and horizontal lines through a given point
- ◇ Finding slopes of lines parallel and perpendicular to a line given in slope-intercept form
- ◇ Finding slopes of lines parallel and perpendicular to a line given in the form  $Ax + By = C$
- ◇ Identifying parallel and perpendicular lines from equations
- ◇ Writing equations of lines parallel and perpendicular to a given line through a point
- ◆ Linear Applications (5 topics)
  - ◇ Writing and evaluating a function that models a real-world situation: Advanced
  - ◇ Writing an equation and drawing its graph to model a real-world situation: Advanced
  - ◇ Interpreting the parameters of a linear function that models a real-world situation
  - ◇ Application problem with a linear function: Finding a coordinate given the slope and a point
  - ◇ Application problem with a linear function: Finding a coordinate given two points
- ◆ Distance and Midpoint Formulas; Circles (6 topics)
  - ◇ Distance between two points in the plane
  - ◇ Midpoint of a line segment in the plane
  - ◇ Graphing a circle given its equation in standard form
  - ◇ Graphing a circle given its equation in general form: Basic
  - ◇ Writing an equation of a circle given its center and a point on the circle
  - ◇ Writing an equation of a circle given the endpoints of a diameter
- ◆ Functions (21 topics)
  - ◇ Identifying functions from relations
  - ◇ Vertical line test
  - ◇ Table for a linear function
  - ◇ Evaluating functions: Linear and quadratic or cubic
  - ◇ Evaluating a rational function: Problem type 1
  - ◇ Evaluating a rational function: Problem type 2
  - ◇ Table for a square root function
  - ◇ Evaluating functions: Absolute value, rational, radical
  - ◇ Evaluating a piecewise-defined function
  - ◇ Variable expressions as inputs of functions
  - ◇ Domain and range from ordered pairs
  - ◇ Domain of a rational function
  - ◇ Domain of a square root function: Basic
  - ◇ Domain of a square root function: Advanced
  - ◇ Finding the domain of a fractional function involving radicals
  - ◇ Determining whether an equation defines a function: Basic
  - ◇ Determining whether an equation defines a function: Advanced
  - ◇ Finding outputs of a one-step function that models a real-world situation: Function notation
  - ◇ Finding outputs of a two-step function with decimals that models a real-world situation: Function notation
  - ◇ Finding inputs and outputs of a two-step function that models a real-world situation: Function notation
  - ◇ Finding a difference quotient for a function
- ◆ Graphs of Functions (20 topics)
  - ◇ Finding an output of a function from its graph
  - ◇ Finding inputs and outputs of a function from its graph



- ◇ Domain and range from the graph of a discrete relation
- ◇ Domain and range from the graph of a continuous function
- ◇ Domain and range from the graph of a piecewise function
- ◇ Finding where a function is increasing, decreasing, or constant given the graph
- ◇ Finding where a function is increasing, decreasing, or constant given the graph: Interval notation
- ◇ Finding local maxima and minima of a function given the graph
- ◇ Graphing a function of the form  $f(x) = ax + b$ : Integer slope
- ◇ Graphing a function of the form  $f(x) = ax + b$ : Fractional slope
- ◇ Graphing an absolute value equation in the plane: Basic
- ◇ Graphing an absolute value equation in the plane: Advanced
- ◇ Graphing a function of the form  $f(x) = ax^2$
- ◇ Graphing a function of the form  $f(x) = ax^2 + c$
- ◇ Graphing a parabola of the form  $y = (x-a)^2 + c$
- ◇ Graphing a square root function: Problem type 1
- ◇ Graphing a square root function: Problem type 2
- ◇ Graphing a piecewise-defined function
- ◇ Finding the average rate of change of a function
- ◇ Finding the average rate of change of a function given its graph
- ◆ Transformations (12 topics)
  - ◇ Even and odd functions
  - ◇ Translating the graph of a parabola: One step
  - ◇ How the leading coefficient affects the shape of a parabola
  - ◇ Translating the graph of an absolute value function: One step
  - ◇ Translating the graph of an absolute value function: Two steps
  - ◇ Writing an equation for a function after a vertical translation
  - ◇ Translating the graph of a function: One step
  - ◇ Translating the graph of a function: Two steps
  - ◇ Transforming the graph of a function by reflecting over an axis
  - ◇ Transforming the graph of a function by shrinking or stretching
  - ◇ Transforming the graph of a function using more than one transformation
  - ◇ Writing an equation for a function after a vertical and horizontal translation
- ◆ Combining Functions; Composite Functions; Inverse Functions (12 topics)
  - ◇ Sum, difference, and product of two functions
  - ◇ Quotient of two functions
  - ◇ Combining functions: Advanced
  - ◇ Composition of two functions: Basic
  - ◇ Expressing a function as a composition of two functions
  - ◇ Composition of two functions: Domain and range
  - ◇ Composition of two functions: Advanced
  - ◇ Horizontal line test
  - ◇ Determining whether two functions are inverses of each other
  - ◇ Inverse functions: Problem type 1
  - ◇ Inverse functions: Problem type 2
  - ◇ Inverse functions: Problem type 3
- Polynomial and Rational Functions (52 topics)
  - ◆ Quadratic Functions (11 topics)
    - ◇ Finding the vertex, x-intercepts, and axis of symmetry from the graph of a parabola
    - ◇ Graphing a parabola of the form  $y = x^2 + bx + c$
    - ◇ Graphing a parabola of the form  $y = ax^2 + bx + c$ : Integer coefficients
    - ◇ Finding the x-intercept(s) and the vertex of a parabola
    - ◇ Using a graphing calculator to find the x-intercept(s) and vertex of a quadratic function
    - ◇ Rewriting a quadratic function to find the vertex of its graph
    - ◇ Finding the maximum or minimum of a quadratic function

- ◇ Word problem involving the maximum or minimum of a quadratic function
- ◇ Domain and range from the graph of a parabola
- ◇ Range of a quadratic function
- ◇ Writing the equation of a quadratic function given its graph
- ◆ Polynomial Functions (8 topics)
  - ◇ Finding zeros of a polynomial function written in factored form
  - ◇ Finding a polynomial of a given degree with given zeros: Real zeros
  - ◇ Finding x- and y-intercepts given a polynomial function
  - ◇ Determining the end behavior of the graph of a polynomial function
  - ◇ Matching graphs with polynomial functions
  - ◇ Inferring properties of a polynomial function from its graph
  - ◇ Using a graphing calculator to find local extrema of a polynomial function
  - ◇ Using a graphing calculator to solve a word problem involving a local extremum of a polynomial function
- ◆ Division of Polynomials; Remainder and Factor Theorems (6 topics)
  - ◇ Polynomial long division: Problem type 1
  - ◇ Polynomial long division: Problem type 2
  - ◇ Polynomial long division: Problem type 3
  - ◇ Synthetic division
  - ◇ Using the remainder theorem to evaluate a polynomial
  - ◇ The Factor Theorem
- ◆ Real Zeros of Polynomial Functions (7 topics)
  - ◇ Using a given zero to write a polynomial as a product of linear factors: Real zeros
  - ◇ Finding all possible rational zeros using the rational zeros theorem: Problem type 1
  - ◇ Finding all possible rational zeros using the rational zeros theorem: Problem type 2
  - ◇ Using the rational zeros theorem to find all zeros of a polynomial: Rational zeros
  - ◇ Using the rational zeros theorem to find all zeros of a polynomial: Irrational zeros
  - ◇ Using a graphing calculator to find zeros of a polynomial function
  - ◇ Using a graphing calculator to solve a word problem involving a polynomial of degree 3
- ◆ Complex Zeros of Polynomials Functions (6 topics)
  - ◇ Multiplying expressions involving complex conjugates
  - ◇ Finding a polynomial of a given degree with given zeros: Complex zeros
  - ◇ Using a given zero to write a polynomial as a product of linear factors: Complex zeros
  - ◇ Using the rational zeros theorem to find all zeros of a polynomial: Complex zeros
  - ◇ Using the conjugate zeros theorem to find all zeros of a polynomial
  - ◇ Linear factors theorem and conjugate zeros theorem
- ◆ Rational Functions (9 topics)
  - ◇ Finding the asymptotes of a rational function: Constant over linear
  - ◇ Finding the asymptotes of a rational function: Linear over linear
  - ◇ Finding the asymptotes of a rational function: Advanced
  - ◇ Graphing a rational function: Constant over linear
  - ◇ Graphing a rational function: Linear over linear
  - ◇ Graphing a rational function: Problem type 2
  - ◇ Graphing rational functions with holes
  - ◇ Matching graphs with rational functions: Two vertical asymptotes
  - ◇ Writing the equation of a rational function given its graph
- ◆ Polynomial and Rational Inequalities (5 topics)
  - ◇ Solving a quadratic inequality written in factored form
  - ◇ Solving a quadratic inequality
  - ◇ Solving a polynomial inequality
  - ◇ Solving a rational inequality: Problem type 1
  - ◇ Solving a rational inequality: Problem type 2
- Exponential and Logarithmic Functions (34 topics)

- ◆ Graphing Exponential Functions (5 topics)
  - ◇ Table for an exponential function
  - ◇ Graphing an exponential function and its asymptote:  $f(x) = a(b)^x$
  - ◇ Translating the graph of an exponential function
  - ◇ The graph, domain, and range of an exponential function
  - ◇ Graphing an exponential function and its asymptote:  $f(x) = a(e)^{x-b} + c$
- ◆ Applications of Exponential Functions (5 topics)
  - ◇ Evaluating an exponential function that models a real–world situation
  - ◇ Evaluating an exponential function with base  $e$  that models a real–world situation
  - ◇ Introduction to compound interest
  - ◇ Finding a final amount in a word problem on exponential growth or decay
  - ◇ Compound interest
- ◆ Logarithmic Functions (7 topics)
  - ◇ Converting between logarithmic and exponential equations
  - ◇ Converting between natural logarithmic and exponential equations
  - ◇ Evaluating a logarithmic expression
  - ◇ Solving an equation of the form  $\log_b a = c$
  - ◇ Translating the graph of a logarithmic function
  - ◇ Graphing a logarithmic function: Basic
  - ◇ The graph, domain, and range of a logarithmic function
- ◆ Properties of Logarithms (5 topics)
  - ◇ Basic properties of logarithms
  - ◇ Expanding a logarithmic expression: Problem type 1
  - ◇ Expanding a logarithmic expression: Problem type 2
  - ◇ Writing an expression as a single logarithm
  - ◇ Change of base for logarithms: Problem type 1
- ◆ Logarithmic and Exponential Equations and Applications (12 topics)
  - ◇ Solving a multi–step equation involving a single logarithm
  - ◇ Solving a multi–step equation involving natural logarithms
  - ◇ Solving an equation involving logarithms on both sides: Problem type 1
  - ◇ Solving an equation involving logarithms on both sides: Problem type 2
  - ◇ Solving an exponential equation by finding common bases: Linear exponents
  - ◇ Solving an exponential equation by finding common bases: Linear and quadratic exponents
  - ◇ Solving an exponential equation by using logarithms: Decimal answers
  - ◇ Solving an exponential equation by using natural logarithms: Decimal answers
  - ◇ Solving an exponential equation by using logarithms: Exact answers in logarithmic form
  - ◇ Finding the time to reach a limit in a word problem on exponential growth or decay
  - ◇ Finding the initial or final amount in a word problem on exponential growth or decay
  - ◇ Finding the rate or time in a word problem on exponential growth or decay
- Trigonometric Functions (45 topics)
  - ◆ Angles and Their Measure (5 topics)
    - ◇ Converting between degree and radian measure: Problem type 1
    - ◇ Converting between degree and radian measure: Problem type 2
    - ◇ Sketching an angle in standard position
    - ◇ Coterminal angles
    - ◇ Arc length and central angle measure
  - ◆ The Unit Circle and Right Triangle Trigonometry (15 topics)
    - ◇ Finding coordinates on the unit circle for special angles
    - ◇ Finding a point on the unit circle given one coordinate
    - ◇ Sine, cosine, and tangent ratios: Variables for side lengths
    - ◇ Trigonometric functions and special angles: Problem type 1
    - ◇ Finding trigonometric ratios from a point on the unit circle
    - ◇ Trigonometric functions and special angles: Problem type 2

- ◇ Trigonometric functions and special angles: Problem type 3
- ◇ Using a calculator to approximate sine, cosine, and tangent values
- ◇ Using the Pythagorean Theorem to find a trigonometric ratio
- ◇ Finding trigonometric ratios given a right triangle
- ◇ Using a trigonometric ratio to find a side length in a right triangle
- ◇ Using trigonometry to find distances
- ◇ Using a trigonometric ratio to find an angle measure in a right triangle
- ◇ Using trigonometry to find angles of elevation or depression
- ◇ Solving a right triangle
- ◆ Trigonometric Functions of Angles (6 topics)
  - ◇ Reference angles: Problem type 1
  - ◇ Reference angles: Problem type 2
  - ◇ Determining the location of a terminal point given the signs of trigonometric values
  - ◇ Finding values of trigonometric functions given information about an angle: Problem type 1
  - ◇ Finding values of trigonometric functions given information about an angle: Problem type 2
  - ◇ Finding values of trigonometric functions given information about an angle: Problem type 3
- ◆ Graphs of Sine and Cosine Functions (9 topics)
  - ◇ Sketching the graph of a sine or cosine function: Problem type 1
  - ◇ Sketching the graph of a sine or cosine function: Problem type 2
  - ◇ Sketching the graph of a sine or cosine function: Problem type 3
  - ◇ Amplitude and period of sine and cosine functions
  - ◇ Amplitude, period, and phase shift of sine and cosine functions
  - ◇ Writing the equation of a sine or cosine function given its graph: Problem type 1
  - ◇ Writing the equation of a sine or cosine function given its graph: Problem type 2
  - ◇ Word problem involving a sine or cosine function: Problem type 1
  - ◇ Word problem involving a sine or cosine function: Problem type 2
- ◆ Graphs of Other Trigonometric Functions (5 topics)
  - ◇ Matching graphs and equations for secant, cosecant, tangent, and cotangent functions
  - ◇ Sketching the graph of a secant or cosecant function: Problem type 1
  - ◇ Sketching the graph of a secant or cosecant function: Problem type 2
  - ◇ Sketching the graph of a tangent or cotangent function: Problem type 1
  - ◇ Sketching the graph of a tangent or cotangent function: Problem type 2
- ◆ Inverse Trigonometric Functions (5 topics)
  - ◇ Values of inverse trigonometric functions
  - ◇ Composition of a trigonometric function and an inverse trigonometric function: Problem type 1
  - ◇ Composition of a trigonometric function and an inverse trigonometric function: Problem type 2
  - ◇ Composition of a trigonometric function and an inverse trigonometric function: Problem type 3
  - ◇ Composition of a trigonometric function and an inverse trigonometric function: Problem type 4
- Trigonometric Identities and Equations (28 topics)
  - ◆ Verifying Trigonometric Identities (6 topics)
    - ◇ Simplifying trigonometric expressions
    - ◇ Using cofunction identities
    - ◇ Verifying a trigonometric identity
    - ◇ Proving trigonometric identities: Problem type 1
    - ◇ Proving trigonometric identities: Problem type 2
    - ◇ Proving trigonometric identities: Problem type 3
  - ◆ Sum and Difference Formulas (4 topics)
    - ◇ Sum and difference identities: Problem type 1
    - ◇ Sum and difference identities: Problem type 2
    - ◇ Sum and difference identities: Problem type 3
    - ◇ Proving trigonometric identities using sum and difference properties
  - ◆ Double–Angle, Half–Angle, and Product–to–Sum Formulas (6 topics)
    - ◇ Double–angle identities: Problem type 1

- ◇ Double–angle identities: Problem type 2
- ◇ Half–angle identities: Problem type 1
- ◇ Product–to–sum and sum–to–product identities: Problem type 1
- ◇ Product–to–sum and sum–to–product identities: Problem type 2
- ◇ Proving trigonometric identities using double–angle properties
- ◆ Trigonometric Equations (12 topics)
  - ◇ Finding solutions in an interval for a basic equation involving sine or cosine
  - ◇ Finding solutions in an interval for a basic tangent, cotangent, secant, or cosecant equation
  - ◇ Solving a basic trigonometric equation using a calculator
  - ◇ Solving a basic trigonometric equation involving sine or cosine
  - ◇ Solving a basic trigonometric equation involving tangent, cotangent, secant, or cosecant
  - ◇ Finding solutions in an interval for a trigonometric equation in factored form
  - ◇ Finding solutions in an interval for a trigonometric equation with a squared function: Problem type 1
  - ◇ Finding solutions in an interval for a trigonometric equation with a squared function: Problem type 2
  - ◇ Finding solutions in an interval for a trigonometric equation using Pythagorean identities
  - ◇ Finding solutions in an interval for an equation with sine and cosine using double–angle identities
  - ◇ Solving a trigonometric equation modeling a real–world situation
  - ◇ Finding solutions in an interval for a trigonometric equation with an angle multiplied by a constant
- Additional Topics in Trigonometry (5 topics)
  - ◆ Laws of Sines and Cosines (5 topics)
    - ◇ Solving a triangle with the law of sines: Problem type 1
    - ◇ Solving a triangle with the law of sines: Problem type 2
    - ◇ Solving a word problem using the law of sines
    - ◇ Solving a triangle with the law of cosines
    - ◇ Solving a word problem using the law of cosines