Liberal Arts Math/Quantitative Reasoning with Corequisite Support

This course covers the topics shown below. Students navigate learning paths based on their level of readiness. Institutional users may customize the scope and sequence to meet curricular needs.

Curriculum (654 topics + 783 additional topics)

• Review of Essential Skills and Problem Solving (122 topics)
  ◆ Place Value, Ordering, and Rounding (17 topics)
    ◊ Whole number place value: Problem type 1
    ◊ Whole number place value: Problem type 2
    ◊ Expanded form: 2 and 3–digit numbers
    ◊ Expanded form: 4 and 5–digit numbers
    ◊ Introduction to inequalities
    ◊ Even and odd numbers
    ◊ Multiplication as repeated addition
    ◊ Introduction to parentheses
    ◊ Rounding to tens or hundreds
    ◊ Rounding to hundreds or thousands
    ◊ Decimal place value: Tenths and hundredths
    ◊ Introduction to non–unit fractions
    ◊ Converting a fraction with a denominator of 10 or 100 to a decimal
    ◊ Introduction to ordering decimals
    ◊ Ordering decimals
    ◊ Rounding decimals
    ◊ Using a calculator to convert a fraction to a rounded decimal
  ◆ Operations with Decimals (13 topics)
    ◊ Decimal addition with 2 numbers
    ◊ Subtraction of aligned decimals
    ◊ Decimal subtraction: Basic
    ◊ Decimal subtraction: Advanced
    ◊ Multiplying a decimal less than 1 by a whole number
    ◊ Multiplying a decimal by a whole number
    ◊ Multiplying decimals less than 1: Problem type 1
    ◊ Decimal multiplication: Problem type 1
    ◊ Multiplication of a decimal by a power of ten
    ◊ Multiplication of a decimal by a power of 0.1
    ◊ Division of a decimal by a whole number
    ◊ Division of a decimal by a 1–digit decimal: Problem type 1
    ◊ Division of a decimal by a power of ten
  ◆ Integers (8 topics)
    ◊ Plotting integers on a number line
    ◊ Ordering integers
    ◊ Integer addition: Problem type 1
    ◊ Integer addition: Problem type 2
    ◊ Integer subtraction: Problem type 1
Integer subtraction: Problem type 2
Integer subtraction: Problem type 3
Integer multiplication and division

Order of Operations and Evaluating Expressions (13 topics)
- Writing expressions using exponents
- Introduction to exponents
- Power of 10: Positive exponent
- Introduction to order of operations
- Order of operations with whole numbers
- Order of operations with whole numbers and grouping symbols
- Order of operations with whole numbers and exponents: Basic
- Evaluating an algebraic expression: Whole number addition or subtraction
- Evaluating an algebraic expression: Whole number multiplication or division
- Evaluating an algebraic expression: Whole numbers with two operations
- Evaluating an algebraic expression: Whole numbers with one operation and an exponent
- Evaluating a formula
- Evaluating a linear expression: Integer multiplication with addition or subtraction

Review of Basic Algebra (25 topics)
- Combining like terms: Whole number coefficients
- Combining like terms: Integer coefficients
- Multiplying a constant and a linear monomial
- Distributive property: Whole number coefficients
- Distributive property: Integer coefficients
- Using distribution and combining like terms to simplify: Univariate
- Identifying solutions to a one–step linear equation: Problem type 1
- Identifying solutions to a one–step linear equation: Problem type 2
- Additive property of equality with whole numbers
- Additive property of equality with integers
- Multiplicative property of equality with whole numbers
- Multiplicative property of equality with integers
- Introduction to solving an equation with variables on the same side
- Identifying solutions to a linear equation in one variable: Two–step equations
- Using two steps to solve an equation with whole numbers
- Solving a two–step equation with integers
- Introduction to solving an equation with parentheses
- Writing a one–step expression for a real–world situation
- Translating a phrase into a one–step expression
- Translating a sentence into a one–step equation
- Writing a function rule given a table of ordered pairs: One–step rules
- Translating a sentence by using an inequality symbol
- Introduction to identifying solutions to an inequality
- Reading a point in the coordinate plane
- Plotting a point in the coordinate plane

Problem Solving (14 topics)
- Word problem with multiplication and addition or subtraction of whole numbers
- Word problem on unit rates associated with ratios of whole numbers: Whole number answers
- Writing an equation and solving a multiplicative comparison word problem
- Time unit conversion with whole number values
- Word problem with addition or subtraction of 2 decimals
- Word problem with addition of 3 or 4 decimals and whole numbers
- Word problem with multiplication of a decimal and a whole number
- Word problem with decimal addition and multiplication
- Word problem with division of a decimal and a whole number
◊ Word problem with decimal subtraction and division
◊ Finding a unit price
◊ Using tables to compare ratios
◊ Computing unit prices to find the better buy
◊ Solving a word problem on proportions using a unit rate

♦ Introduction to Perimeter and Area (4 topics)
  ◊ Perimeter of a polygon
  ◊ Perimeter of a square or a rectangle
  ◊ Area of a square or a rectangle
  ◊ Square root of a perfect square

♦ Introduction to Percentages (20 topics)
  ◊ Converting a fraction with a denominator of 100 to a percentage
  ◊ Converting a percentage to a fraction with a denominator of 100
  ◊ Finding the percentage of a grid that is shaded
  ◊ Representing benchmark percentages on a grid
  ◊ Introduction to converting a percentage to a decimal
  ◊ Introduction to converting a decimal to a percentage
  ◊ Converting between percentages and decimals
  ◊ Equivalent fractions
  ◊ Converting a fraction to a percentage: Denominator of 4, 5, or 10
  ◊ Converting a proper fraction with a denominator of 2, 4, or 5 to a decimal
  ◊ Converting a fraction to a percentage: Denominator of 20, 25, or 50
  ◊ Using a calculator to convert a fraction to a rounded percentage
  ◊ Finding a percentage of a whole number
  ◊ Finding a percentage of a whole number without a calculator: Basic
  ◊ Finding a percentage of a total amount: Real-world situations
  ◊ Finding a percentage of a total amount without a calculator: Sales tax, commission, discount
  ◊ Applying the percent equation: Problem type 1
  ◊ Finding the multiplier to give a final amount after a percentage increase or decrease
  ◊ Finding the final amount given the original amount and a percentage increase or decrease
  ◊ Finding the sale price given the original price and percent discount

♦ Estimation (1 topics)
  ◊ Estimating a tip without a calculator

♦ Interpreting Graphs (7 topics)
  ◊ Constructing a bar graph for non-numerical data
  ◊ Interpreting a bar graph
  ◊ Interpreting a double bar graph
  ◊ Interpreting a pictograph table
  ◊ Interpreting a pie chart
  ◊ Interpreting a line graph
  ◊ Interpreting the graphs of two functions

• Sets (31 topics)
  ♦ Introduction to Sets (6 topics)
    ◊ Identifying elements of sets for a real world situation
    ◊ Writing sets of numbers using descriptive and roster forms
    ◊ Writing sets of numbers using set-builder and roster forms
    ◊ Identifying well defined sets
    ◊ Membership and cardinality of sets
    ◊ Identifying equivalent and equal sets for a real-world situation
  ♦ Subsets (6 topics)
    ◊ Identifying true statements involving subsets and proper subsets
    ◊ Identifying true statements about set membership and subsets
    ◊ Writing subsets
Writing subsets for a real–world situation
Determining the total number of subsets of a set
Determining the number of subsets for a real–world situation

Operations with Sets (6 topics)
Finding sets and complements of sets
Finding sets and complements of sets for a real–world situation
Union and intersection of finite sets
Unions, intersections, and complements involving 2 sets
Unions and intersections involving the empty set or universal set
Unions, intersections, and complements involving 3 sets

Venn Diagrams (13 topics)
Interpreting a Venn diagram with 2 sets for a real–world situation
Interpreting a Venn diagram with 3 sets for a real–world situation
Interpreting Venn diagram cardinalities with 2 sets for a real–world situation
Constructing a Venn diagram with 2 sets
Constructing a Venn diagram with 2 sets to solve a word problem
Interpreting Venn diagram cardinalities with 3 sets for a real–world situation
Constructing a Venn diagram with 3 sets
Shading a Venn diagram with 2 sets: Unions, intersections, and complements
Shading Venn diagrams to determine if sets are equal
Venn diagram with 2 sets: Unions, intersections, and complements
Venn diagram with 2 sets: Unions, intersections, and complements for a real–world situation
Shading a Venn diagram with 3 sets: Unions, intersections, and complements
Venn diagram with 3 sets: Unions, intersections, and complements

Logic (30 topics)
Logical Statements (5 topics)
Identifying statements
Identifying simple and compound statements
Negation of a statement
Understanding quantifiers
Negation of a quantified statement

Conjunctions and Disjunctions (7 topics)
Symbolic translation of negations, conjunctions, and disjunctions: Basic
Symbolic translation of negations, conjunctions, and disjunctions: Advanced
Introduction to truth tables with negations, conjunctions, or disjunctions
Truth tables with conjunctions or disjunctions
Using logic to test a claim: Conjunction or disjunction
Using De Morgan's Laws to identify negations and equivalent statements
Completing rows of truth tables: Conjunctions and disjunctions

Conditional Statements (12 topics)
Symbolic translation of conditional and biconditional statements: Basic
Symbolic translation involving three statements
Introduction to truth tables with conditional statements
Using logic to test a claim: Conditional statement, basic
Truth tables with conjunctions, disjunctions, and conditional statements
The converse, inverse, and contrapositive of a conditional statement
Writing the converse, inverse, and contrapositive of a conditional statement and determining their truth values
Identifying equivalent statements and negations of a conditional statement
Introduction to truth tables with biconditional statements
Writing a biconditional statement as a conditional statement and its converse and determining truth values
Completing rows of truth tables: Conjunctions, disjunctions, and conditional statements
Using logic to test a claim: Conditional statement, advanced

Logical Arguments (6 topics)
- Determining if a statement is a tautology, contradiction, or neither
- Determining if statements are logically equivalent
- Using truth tables to determine the validity of an argument
- Conditional statements and deductive reasoning
- Validity of an argument
- Translating an argument and determining its validity

Numeration Systems (13 topics)
- Expanded Form with Powers of Ten (2 topics)
  - Expanded forms of numbers less than 10,000 using powers of ten
  - Expanded forms of numbers greater than 10,000 using powers of ten
- Base Number Systems (7 topics)
  - Converting from base two to base ten
  - Converting from a base less than ten to base ten
  - Converting from base ten to base two
  - Converting from base ten to a base less than ten: Basic
  - Converting from base ten to a base less than ten: Advanced
  - Counting in bases less than ten
  - Converting between base two and base eight
- Operations in Base Number Systems (4 topics)
  - Adding numbers in bases less than ten
  - Subtracting numbers in bases less than ten
  - Multiplying numbers in bases less than ten: Single-digit times multi-digit
  - Division in a base less than ten: One-digit divisor

Number Theory and the Real Number System (71 topics)
- Divisibility, Prime Numbers, and Prime Factorization (6 topics)
  - Divisibility rules for 2, 5, and 10
  - Factors
  - Prime numbers
  - Prime factorization
  - Greatest common factor of 2 numbers
  - Least common multiple of 2 numbers
- More on Integers and Order of Operations (9 topics)
  - Writing a signed number for a real-world situation
  - Addition and subtraction with 3 integers
  - Signed decimal addition and subtraction
  - Division involving zero
  - Multiplication of 3 or 4 integers
  - Absolute value of a number
  - Computing the distance between two integers on a number line
  - Exponents and integers: Problem type 1
  - Order of operations with integers
- Fractions (6 topics)
  - Understanding equivalent fractions
  - Introduction to simplifying a fraction
  - Simplifying a fraction
  - Plotting fractions on a number line
  - Ordering fractions with the same denominator
  - Using a common denominator to order fractions
- Multiplication and Division with Fractions (8 topics)
  - Product of a unit fraction and a whole number
  - Product of a fraction and a whole number: Problem type 1
◊ Introduction to fraction multiplication
◊ Fraction multiplication
◊ Product of a fraction and a whole number: Problem type 2
◊ Multiplication of 3 fractions
◊ Signed fraction multiplication: Basic
◊ Exponents and fractions
♦ Addition and Subtraction with Fractions (6 topics)
  ◊ Addition or subtraction of fractions with the same denominator
  ◊ Addition or subtraction of fractions with the same denominator and simplification
  ◊ Finding the LCD of two fractions
  ◊ Writing fractions with a common denominator to add or subtract
  ◊ Addition or subtraction of fractions with different denominators
  ◊ Signed fraction addition or subtraction: Basic
♦ Converting Between Fractions and Decimals (5 topics)
  ◊ Converting a decimal to a proper fraction without simplifying: Basic
  ◊ Converting a decimal to a proper fraction in simplest form: Basic
  ◊ Converting a fraction to a terminating decimal: Basic
  ◊ Converting a fraction to a repeating decimal: Basic
  ◊ Identifying rational decimal numbers
♦ Real Numbers (12 topics)
  ◊ Identifying numbers as integers or non–integers
  ◊ Identifying numbers as rational or irrational
  ◊ Constructing a Venn diagram to classify real numbers
  ◊ Constructing a Venn diagram to describe relationships between sets of real numbers
  ◊ Introduction to properties of addition
  ◊ Introduction to properties of multiplication
  ◊ Square roots of perfect squares with signs
  ◊ Using a calculator to approximate a square root
  ◊ Estimating a square root
  ◊ Square root of a rational perfect square
  ◊ Introduction to square root addition or subtraction
  ◊ Introduction to square root multiplication
♦ Product, Power, and Quotient Rules of Exponents (10 topics)
  ◊ Understanding the product rule of exponents
  ◊ Introduction to the product rule of exponents
  ◊ Product rule with positive exponents: Univariate
  ◊ Product rule with positive exponents: Multivariate
  ◊ Introduction to the power of a power rule of exponents
  ◊ Introduction to the power of a product rule of exponents
  ◊ Power rules with positive exponents: Multivariate products
  ◊ Power rules with positive exponents: Multivariate quotients
  ◊ Introduction to the quotient rule of exponents
  ◊ Simplifying a ratio of univariate monomials
♦ Negative Exponents (4 topics)
  ◊ Evaluating expressions with exponents of zero
  ◊ Evaluating an expression with a negative exponent: Whole number base
  ◊ Evaluating an expression with a negative exponent: Positive fraction base
  ◊ Rewriting an algebraic expression without a negative exponent
♦ Scientific Notation (5 topics)
  ◊ Introduction to scientific notation with positive exponents
  ◊ Scientific notation with positive exponent
  ◊ Introduction to scientific notation with negative exponents
  ◊ Scientific notation with negative exponent
Converting between scientific notation and standard form in a real-world situation

- **Algebraic Equations and Inequalities (74 topics)**
  - **Algebraic Expressions (6 topics)**
    - Evaluating a quadratic expression: Integers
    - Function tables with two-step rules
    - Table for a linear equation
    - Combining like terms in a quadratic expression
    - Identifying equivalent algebraic expressions
    - Identifying properties used to simplify an algebraic expression
  - **One-Step Linear Equations (5 topics)**
    - Additive property of equality with decimals
    - Additive property of equality with signed fractions
    - Multiplicative property of equality with fractions
    - Multiplicative property of equality with decimals
    - Multiplicative property of equality with signed fractions
  - **Multi-Step Linear Equations (10 topics)**
    - Introduction to using substitution to solve a linear equation
    - Solving a multi-step equation given in fractional form
    - Identifying properties used to solve a linear equation
    - Solving a linear equation with several occurrences of the variable: Variables on the same side
    - Introduction to solving a linear equation with a variable on each side
    - Solving a linear equation with several occurrences of the variable: Variables on both sides
    - Solving a linear equation with several occurrences of the variable: Variables on the same side and distribution
    - Solving a linear equation with several occurrences of the variable: Variables on both sides and distribution
    - Solving a linear equation with several occurrences of the variable: Variables on both sides and two distributions
    - Solving equations with zero, one, or infinitely many solutions
  - **Solving Formulas for a Variable (4 topics)**
    - Solving for a variable in terms of other variables using addition or subtraction: Basic
    - Solving for a variable in terms of other variables using multiplication or division: Basic
    - Solving for a variable in terms of other variables using multiplication or division: Advanced
    - Solving for a variable in terms of other variables using addition or subtraction with division
  - **Applications of Linear Equations (12 topics)**
    - Translating a phrase into a two-step expression
    - Translating a sentence into a multi-step equation
    - Writing an equation to represent a proportional relationship
    - Solving a fraction word problem using a linear equation of the form $Ax = B$
    - Solving a word problem with two unknowns using a linear equation
    - Writing an equation of the form $Ax + B = C$ to solve a word problem
    - Solving a decimal word problem using a linear equation of the form $Ax + B = C$
    - Writing an equation to represent a real-world problem: Variable on both sides
    - Solving a one-step word problem using the formula $d = rt$
    - Finding outputs of a one-step function that models a real-world situation: Two variable equation
    - Finding outputs of a two-step function with decimals that models a real-world situation: Two variable equation
    - Finding inputs and outputs of a two-step function that models a real-world situation: Two variable equation
  - **Ratio and Proportion (9 topics)**
    - Simplifying a ratio of whole numbers: Problem type 1
    - Simplifying a ratio of whole numbers: Problem type 2
    - Finding missing values in a table of equivalent ratios
Solving a proportion of the form $x/a = b/c$: Basic
Solving a proportion of the form $x/a = b/c$
Introduction to solving a rational equation
Word problem on proportions: Problem type 1
Word problem on proportions: Problem type 2
Finding lengths using scale models

Proportional Relationships and Variation (1 topics)
Finding outputs and rate of increase given the graph of a line that models a real-world situation

Linear Inequalities (10 topics)
Identifying solutions to a one-step linear inequality
Additive property of inequality with whole numbers
Additive property of inequality with integers
Multiplicative property of inequality with whole numbers
Multiplicative property of inequality with integers
Multiplicative property of inequality with signed fractions
Solving a two-step linear inequality with whole numbers
Solving a two-step linear inequality: Problem type 1
Solving a two-step linear inequality: Problem type 2
Graphing a linear inequality on the number line

Applications of Linear Inequalities (5 topics)
Translating a sentence into a one-step inequality
Writing an inequality for a real-world situation
Solving a word problem using a one-step linear inequality
Solving a word problem using a two-step linear inequality
Solving a decimal word problem using a two-step linear inequality

Operations with Polynomials (4 topics)
Simplifying a sum or difference of two univariate polynomials
Multiplying binomials with leading coefficients of 1
Multiplying binomials with leading coefficients greater than 1
Squaring a binomial: Univariate

Factoring (4 topics)
Factoring a linear binomial
Factoring a quadratic with leading coefficient 1
Factoring a quadratic with leading coefficient greater than 1: Problem type 1
Factoring a perfect square trinomial with leading coefficient 1

Quadratic Equations (4 topics)
Solving an equation written in factored form
Finding the roots of a quadratic equation with leading coefficient 1
Applying the quadratic formula: Exact answers
Solving a word problem using a quadratic equation with irrational roots

Graphs, Functions, and Systems (56 topics)
Graphing and Intercepts (12 topics)
Finding distances between points that share a common coordinate given the graph
Identifying solutions to a linear equation in two variables
Finding a solution to a linear equation in two variables
Graphing a linear equation of the form $y = mx$
Graphing a line given its equation in slope-intercept form: Integer slope
Graphing a line given its equation in slope-intercept form: Fractional slope
Graphing a line given its equation in standard form
Graphing a vertical or horizontal line
Finding x- and y-intercepts given the graph of a line on a grid
Finding x- and y-intercepts of a line given the equation: Basic
Graphing a line given its x- and y-intercepts
◊ Graphing a line by first finding its x- and y-intercepts

♦ Slope (6 topics)
- Finding slope given the graph of a line in quadrant 1 that models a real-world situation
- Classifying slopes given graphs of lines
- Finding slope given the graph of a line on a grid
- Finding slope given two points on the line
- Finding the slope of horizontal and vertical lines
- Graphing a line given its slope and y-intercept

♦ Equations of Lines (13 topics)
- Finding the slope and y-intercept of a line given its equation in the form \( y = mx + b \)
- Finding the slope and y-intercept of a line given its equation in the form \( Ax + By = C \)
- Writing an equation of a line given its slope and y-intercept
- Writing an equation in slope-intercept form given the slope and a point
- Writing an equation of a line given the y-intercept and another point
- Writing the equation of the line through two given points
- Writing and evaluating a function that models a real-world situation: Basic
- Writing and evaluating a function that models a real-world situation: Advanced
- Writing an equation and drawing its graph to model a real-world situation: Basic
- Writing an equation and drawing its graph to model a real-world situation: Advanced
- Finding the intercepts and rate of change given a graph of a linear function
- Interpreting the parameters of a linear function that models a real-world situation
- Identifying parallel and perpendicular lines

♦ Systems of Linear Equations (14 topics)
- Identifying solutions to a system of linear equations
- Identifying the solution of systems of linear equations from graphs
- Classifying systems of linear equations from graphs
- Graphically solving a system of linear equations both of the form \( y = mx + b \)
- Graphically solving a system of linear equations
- Solving a system of linear equations of the form \( y = mx + b \)
- Solving a system of linear equations using substitution
- Solving a system of linear equations using elimination with addition
- Solving a system of linear equations using elimination with multiplication and addition
- Solving a word problem involving a sum and another basic relationship using a system of linear equations
- Solving a word problem using a system of linear equations of the form \( Ax + By = C \)
- Writing and solving a system of two linear equations given a table of values
- Solving a word problem using a system of linear equations of the form \( y = mx + b \)
- Solving a value mixture problem using a system of linear equations

♦ Functions (6 topics)
- Vertical line test
- Table for a linear function
- Evaluating functions: Linear and quadratic or cubic
- Finding outputs of a one-step function that models a real-world situation: Function notation
- Finding outputs of a two-step function with decimals that models a real-world situation: Function notation
- Finding inputs and outputs of a two-step function that models a real-world situation: Function notation

♦ Exponential Functions (5 topics)
- Table for an exponential function
- Using a calculator to evaluate exponential expressions
- Evaluating an exponential function that models a real-world situation
- Introduction to compound interest
- Finding a final amount in a word problem on exponential growth or decay
• Consumer Mathematics (39 topics)
  ♦ Applications Involving Percentages (12 topics)
    ◊ Writing a ratio as a percentage
    ◊ Computing a percentage from a table of values
    ◊ Finding the rate of a tax or commission
    ◊ Computing percentages for categories of a budget
    ◊ Comparing discounts
    ◊ Finding the total amount given the percentage of a partial amount
    ◊ Finding the total cost including tax or markup
    ◊ Combined effect of more than one markup or discount
    ◊ Finding the original amount given the result of a percentage increase or decrease
    ◊ Finding the original price given the sale price and percent discount
    ◊ Finding the percentage increase or decrease: Basic
    ◊ Finding the percentage increase or decrease: Advanced
  ♦ Gross Pay and FICA (5 topics)
    ◊ Hourly gross pay with overtime
    ◊ Gross pay with commission and salary
    ◊ Gross pay with variable commission scale
    ◊ Calculating income tax
    ◊ Calculating income tax using a tax bracket table
  ♦ Simple Interest (5 topics)
    ◊ Finding the interest and future value of a simple interest loan or investment
    ◊ Computing the total cost and interest for a loan
    ◊ Finding the principal, rate, or time of a simple interest loan or investment
    ◊ Computing the interest and repayment amount for a simple interest loan whose term is given in months or days
    ◊ Finding the principal, rate, or time for a simple interest loan whose term is given in months or days
  ♦ Compound Interest (2 topics)
    ◊ Calculating and comparing simple interest and compound interest
    ◊ Finding the future value and interest for an investment earning compound interest
  ♦ Present Values and Annuities (4 topics)
    ◊ Finding the present value of an investment earning compound interest
    ◊ Finding the future value of an annuity
    ◊ Computing the value of an annuity for its first few years
    ◊ Finding the periodic payment needed to meet an investment goal
  ♦ Installment Buying (5 topics)
    ◊ Finding the monthly payment, total payment, and interest for a loan
    ◊ Finding the effective annual interest rate of a loan or investment
    ◊ Computing the unpaid balance for a credit card statement
    ◊ Mean of a data set
    ◊ Computing the average daily balance, interest, and balance for a credit card statement
  ♦ Mortgages (4 topics)
    ◊ Finding the down payment, loan amount, and monthly payment for a loan
    ◊ Comparing monthly payments and total costs of two loans
    ◊ Finding the interest paid, principal reduction, and new balance after a mortgage payment
    ◊ Completing a few rows of an amortization table
  ♦ Stocks and Bonds (2 topics)
    ◊ Reading stock quotations
    ◊ Calculating return on stock investment
• Measurement (39 topics)
  ♦ U.S. Customary Units of Length (7 topics)
    ◊ Choosing U.S. Customary measurement units
    ◊ U.S. Customary length conversion with whole number values
Conversions involving measurements in feet and inches
◊ U.S. Customary length conversions involving rounding decimals
◊ Word problem involving a U.S. Customary length conversion
◊ U.S. Customary length conversions involving dimensional analysis
◊ Word problem involving U.S. Customary length conversions using dimensional analysis
♦ Perimeter, Area, and Volume (10 topics)
◊ Finding the missing length in a figure
◊ Perimeter of a piecewise rectangular figure
◊ Word problem involving the area of a rectangle: Problem type 2
◊ Area of a piecewise rectangular figure
◊ Area between two rectangles
◊ Volume of a rectangular prism
◊ Volume of a rectangular prism made of unit cubes
◊ Word problem involving the volume of a rectangular prism
◊ Surface area of a cube or a rectangular prism
◊ Word problem involving the surface area of a rectangular prism
♦ U.S. Customary Units of Area and Volume (4 topics)
◊ Word problem on area involving conversions of U.S. Customary units: Problem type 1
◊ Word problem on area involving conversions of U.S. Customary units: Problem type 2
◊ Word problem on volume involving conversions of U.S. Customary units
◊ Word problem involving U.S. Customary conversions, surface area, and cost
♦ U.S. Customary Units of Weight and Volume (3 topics)
◊ U.S. Customary weight conversions with whole number values
◊ U.S. Customary volume conversion with whole number values
◊ U.S. Customary unit conversion with whole number values: Two-step conversion
♦ Metric Units of Measurement (7 topics)
◊ Choosing metric measurement units
◊ Metric distance conversion with whole number values
◊ Metric distance conversion with decimal values
◊ Metric mass or volume conversion with whole numbers
◊ Metric conversion with decimal values: Two-step problem
◊ Metric area unit conversion with decimal values
◊ Converting between metric units of volume and capacity
♦ Converting Between Measurement Systems (7 topics)
◊ Converting between metric and U.S. Customary unit systems
◊ Word problem on area involving conversions between systems
◊ Word problem involving a conversion between U.S. Customary units of weight and metric units of mass
◊ Converting between compound units: Basic
◊ Converting between compound units: Advanced
◊ Conversions with currency
◊ Word problem involving conversion between compound units using dimensional analysis
♦ Time and Temperature (1 topics)
◊ Converting between temperatures in Fahrenheit and Celsius
• Geometry (48 topics)
♦ Lines and Angles (8 topics)
◊ Measuring an angle with the protractor
◊ Acute, obtuse, and right angles
◊ Finding supplementary and complementary angles
◊ Finding the complement or supplement of an angle given a figure
◊ Identifying supplementary and vertical angles
◊ Finding angle measures given two intersecting lines
◊ Identifying corresponding and alternate angles
Finding angle measures given two parallel lines cut by a transversal

Triangles (6 topics)
- Acute, obtuse, and right triangles
- Classifying scalene, isosceles, and equilateral triangles by side lengths
- Classifying scalene, isosceles, and equilateral triangles by side lengths or angles
- Finding an angle measure of a triangle given two angles
- Finding an angle measure for a triangle with an extended side
- Finding an angle measure given a triangle and parallel lines

The Pythagorean Theorem and Distance Formula (3 topics)
- Introduction to the Pythagorean Theorem
- Pythagorean Theorem
- Word problem involving the Pythagorean Theorem

Perimeter and Angles of Polygons (3 topics)
- Sum of the angle measures of a quadrilateral
- Identifying parallelograms, rectangles, and squares
- Properties of quadrilaterals

Area of Polygons (4 topics)
- Area of a triangle
- Area involving rectangles and triangles
- Area of a parallelogram
- Area of a trapezoid

Circumference and Area of Circles (4 topics)
- Circumference of a circle
- Perimeter involving rectangles and circles
- Area of a circle
- Area involving rectangles and circles

Volume (7 topics)
- Classifying solids
- Vertices, edges, and faces of a solid
- Volume of a triangular prism
- Volume of a pyramid
- Volume of a cylinder
- Volume of a cone
- Volume of a sphere

Surface Area (2 topics)
- Surface area of a cylinder
- Surface area of a sphere

Congruent and Similar Figures (5 topics)
- Identifying congruent shapes on a grid
- Finding a missing side length given two similar triangles
- Similar polygons
- Similar right triangles
- Indirect measurement

Right Triangle Trigonometry (6 topics)
- Sine, cosine, and tangent ratios: Numbers for side lengths
- Using a calculator to approximate sine, cosine, and tangent values
- Using a trigonometric ratio to find a side length in a right triangle
- Using trigonometry to find a length in a word problem with one right triangle
- Using a trigonometric ratio to find an angle measure in a right triangle
- Using trigonometry to find angles of elevation or depression in a word problem

Counting and Probability (38 topics)
- Fundamental Counting Principle (6 topics)
  - Interpreting a tree diagram
◊ Introduction to the counting principle
◊ Counting principle
◊ Counting principle with repetition allowed
◊ Counting principle involving a specified arrangement
◊ Counting arrangements of objects that are not all distinct

♦ Permutations and Combinations (7 topics)
  ◊ Factorial expressions
  ◊ Computing permutations and combinations
  ◊ Introduction to permutations and combinations
  ◊ Permutations and combinations: Problem type 1
  ◊ Permutations and combinations: Problem type 2
  ◊ Permutations and combinations: Problem type 3
  ◊ Counting using combinations and addition

♦ Probability and Odds of an Event (12 topics)
  ◊ Determining a sample space and outcomes for a simple event
  ◊ Determining a sample space and outcomes for a compound event
  ◊ Introduction to the probability of an event
  ◊ Probability involving one die or choosing from n distinct objects
  ◊ Probability involving choosing from objects that are not distinct
  ◊ Probability of selecting one card from a standard deck
  ◊ Understanding likelihood
  ◊ Probabilities of an event and its complement
  ◊ Outcomes and event probability
  ◊ Experimental and theoretical probability
  ◊ Finding the odds in favor and against
  ◊ Converting between probability and odds

♦ Expected Value (2 topics)
  ◊ Introduction to expectation
  ◊ Computing expected value in a game of chance

♦ Probability of Independent and Dependent Events (9 topics)
  ◊ Probability of independent events: Decimal answers
  ◊ Probability of dependent events: Decimal answers
  ◊ Probabilities involving two rolls of a die: Decimal answers
  ◊ Probability of independent events involving a standard deck of cards
  ◊ Probabilities of draws without replacement
  ◊ Determining outcomes for compound events and complements of events
  ◊ Computing conditional probability using a sample space
  ◊ Computing conditional probability using a two−way frequency table
  ◊ Conditional probability: Basic

♦ Probability Involving a Union of Events (2 topics)
  ◊ Word problem involving the probability of a union
  ◊ Computing probability involving the addition rule using a two−way frequency table

♦ Statistics (50 topics)
  ◊ Interpreting and Displaying Data (14 topics)
    ◊ Choosing an appropriate method for gathering data: Problem type 2
    ◊ Classifying samples
    ◊ Finding a percentage of a total amount in a circle graph
    ◊ Computations from pie charts
    ◊ Angle measure in a circle graph
    ◊ Constructing a frequency distribution for non−grouped data
    ◊ Constructing a frequency distribution for grouped data
    ◊ Constructing a frequency distribution and a histogram
    ◊ Constructing a relative frequency distribution for grouped data
• Histograms for grouped data
• Interpreting a histogram
• Constructing a frequency distribution and a frequency polygon
• Frequency polygons for grouped data
• Interpreting a stem–and–leaf display

♦ Measures of Average (14 topics)
  ◊ Computations involving the mean, sample size, and sum of a data set
  ◊ Finding the value for a new score that will yield a given mean
  ◊ Rejecting unreasonable claims based on average statistics
  ◊ Weighted mean: Tabular data
  ◊ Introduction to summation notation
  ◊ Approximating the mean of a data set given a frequency distribution
  ◊ Approximating the mean of a data set given a histogram
  ◊ Median of a data set
  ◊ Mode of a data set
  ◊ Mean, median, and mode: Computations
  ◊ How changing a value affects the mean and median
  ◊ Finding outliers in a data set
  ◊ Choosing the best measure to describe data
  ◊ Mean, median, and mode: Comparisons

♦ Measures of Variation (5 topics)
  ◊ Range of a data set
  ◊ Comparing measures of center and variation
  ◊ Identifying the center, spread, and shape of a data set
  ◊ Using back–to–back stem–and–leaf displays to compare data sets
  ◊ Population standard deviation

♦ Measures of Position (5 topics)
  ◊ Percentage of data below a specified value
  ◊ Percentiles
  ◊ Interpreting percentile ranks
  ◊ Five–number summary and interquartile range
  ◊ Box–and–whisker plots

♦ The Normal Distribution (6 topics)
  ◊ Using the graph of a distribution to find probabilities: Basic
  ◊ Using the empirical rule to identify values and percentages of a normal distribution
  ◊ Word problem involving calculations from a normal distribution
  ◊ Shading a region and finding its standard normal probability
  ◊ Computing standard normal probabilities
  ◊ Finding a probability given a normal distribution: Basic

♦ Correlation and Regression (6 topics)
  ◊ Constructing a scatter plot
  ◊ Sketching the line of best fit
  ◊ Scatter plots and correlation
  ◊ Predictions from the line of best fit
  ◊ Approximating the equation of a line of best fit and making predictions
  ◊ Linear relationship and the correlation coefficient

• Voting and Apportionment (22 topics)
  ♦ Voting Methods (6 topics)
    ◊ Interpreting a preference table
    ◊ Plurality method
    ◊ Borda count method
    ◊ Plurality–with–elimination method: One elimination
    ◊ Pairwise comparison method
Comparing voting methods

- Flaws of Voting Methods (4 topics)
  - Borda count method and the majority criterion
  - Plurality method and the head-to-head criterion
  - Plurality-with-elimination and the monotonicity criterion
  - Pairwise comparison and the irrelevant alternatives criterion

- Apportionment Methods (8 topics)
  - Standard divisor and standard quota
  - Lower and upper quotas
  - Hamilton's method
  - Jefferson's method
  - Adams' method
  - Webster's method
  - Geometric mean of two whole numbers
  - Huntington–Hill method

- Flaws of Apportionment Methods (4 topics)
  - Hamilton's method and the Alabama paradox
  - Hamilton's method and the population paradox
  - Hamilton's method and the new states paradox
  - Jefferson's, Adams’, and Webster’s methods and the quota rule

- Graph Theory (21 topics)
  - Graphs, Paths, and Circuits (7 topics)
    - Counting vertices, edges, and loops
    - Degree of a vertex, even and odd vertices, and adjacent vertices
    - Drawing a graph
    - Drawing an equivalent graph
    - Drawing a graph to represent a figure
    - Paths and circuits
    - Connected, disconnected, and bridges: Interpreting
  - Euler Paths and Euler Circuits (4 topics)
    - Euler paths and Euler circuits
    - Euler’s theorem
    - Fleury’s algorithm
    - Fleury’s algorithm in context
  - Hamilton Paths and Hamilton Circuits (6 topics)
    - Hamilton paths and circuits
    - Drawing a complete graph
    - Number of Hamilton circuits in a complete graph
    - Weighted graphs
    - Using the brute force method to find an optimal Hamilton circuit
    - Using the nearest neighbor method to approximate an optimal Hamilton circuit
  - Trees (4 topics)
    - Drawing a tree
    - Properties of trees
    - Spanning trees
    - Using Kruskal's algorithm to find a minimum spanning tree

- Other Topics Available(*) (783 additional topics)
  - Review of Essential Skills and Problem Solving (68 topics)
    - Numeral translation: Problem type 1
    - Numeral translation: Problem type 2
    - Expanded form with zeros
◊ Ordering large numbers
◊ Comparing numerical expressions with parentheses
◊ Rounding to thousands, ten thousands, or hundred thousands
◊ Decimal place value: Hundreds to ten thousandths
◊ Writing a decimal number less than 1 given its name
◊ Writing a decimal number greater than 1 given its name
◊ Writing a decimal number given its name: Advanced
◊ Converting a fraction with a denominator of 100 or 1000 to a decimal
◊ Writing a decimal and a fraction for a shaded region
◊ Reading decimal position on a number line: Tenths
◊ Reading decimal position on a number line: Hundredths
◊ Understanding decimal position on a number line using zoom: Hundredths
◊ Understanding decimal position on a number line using zoom: Thousandths
◊ Decimal addition with 3 numbers
◊ Decimal addition and subtraction with 3 or more numbers
◊ Average of two numbers
◊ Decimal multiplication: Problem type 2
◊ Multiplying decimals less than 1: Problem type 2
◊ Whole number division with decimal answers
◊ Division of a decimal by a 2-digit decimal
◊ Division of a decimal by a power of 0.1
◊ Decimal division with rounding
◊ Plotting opposite integers on a number line
◊ Identifying like terms
◊ Introduction to the distributive property
◊ Understanding the distributive property
◊ Introduction to factoring with numbers
◊ Using algebra tiles to determine if two expressions are equivalent
◊ Plotting the solution for a one-step equation on a number line
◊ Distinguishing between expressions and equations
◊ Introduction to the product rule with positive exponents: Whole number base
◊ Finding the next terms of an arithmetic sequence with whole numbers
◊ Finding the next terms of a geometric sequence with whole numbers
◊ Finding patterns in shapes
◊ Describing an increasing or decreasing pattern from a table of values
◊ Word problem with division of whole numbers and rounding: Problem type 1
◊ Examining a savings plan for college
◊ Calculations involving paying for college
◊ Calculations involving purchases with debit and credit cards
◊ Reading a credit report
◊ Distinguishing between fixed and variable expenses
◊ Word problem with subtraction of a whole number and a decimal: Regrouping with zeros
◊ Balancing a check register
◊ Word problem with multiplication of two decimals
◊ Comparing costs of checking accounts
◊ Word problem with division of two decimals
◊ Word problem on unit rates associated with ratios of whole numbers: Decimal answers
◊ Word problem on finding the perimeter of a rectangle
◊ Writing algebraic expressions for the perimeter of a figure
◊ Area of a rectangle on a grid
◊ Finding side lengths of rectangles given one dimension and an area or a perimeter
◊ Finding side lengths of squares given an area and a perimeter
◊ Converting between percentages and decimals in a real-world situation
Finding benchmark fractions and percentages for a figure
Converting a fraction to a percentage in a real−world situation
Finding a percentage of a whole number without a calculator: Advanced
Applying the percent equation: Problem type 2
Estimating a sum of whole numbers: Problem type 2
Estimating a difference of whole numbers: Problem type 2
Estimating a product or quotient of whole numbers
Estimating a decimal sum or difference
Estimating a product of decimals
Interpreting a tally table
Constructing a two−way frequency table: Advanced
Constructing a line plot

Sets (8 topics)
Writing sets for a real−world situation using descriptive and roster forms
Writing sets of integers using set−builder and roster forms
Identifying infinite sets and determining cardinalities of finite sets
Identifying equivalent and equal sets
Constructing a Venn diagram with 3 sets to solve a word problem
Introduction to shading a Venn diagram with 2 sets
Introduction to shading a Venn diagram with 3 sets
Venn diagram with 3 sets: Unions, intersections, and complements for a real−world situation

Logic (2 topics)
Symbolic translation of conditional and biconditional statements: Advanced
Completing rows of truth tables: Conjunctions, disjunctions, conditional and biconditional statements

Numeration Systems (8 topics)
Converting from a base greater than ten to base ten
Counting in bases greater than ten
Converting from base ten to a base greater than ten
Converting between base two and base sixteen
Congruence in a modular arithmetic system
Addition, subtraction, and multiplication in a modular arithmetic system
Negative numbers and subtraction in a modular arithmetic system
Word problem involving a modular arithmetic system

Number Theory and the Real Number System (149 topics)
Divisibility rules for 3 and 9
Greatest common factor of 3 numbers
Least common multiple of 3 numbers
Word problem involving the least common multiple of 2 numbers
Word problem with common multiples
Using a number line to compare integers
Reading the temperature from a thermometer
Interpreting a table of signed numbers that relate to a real−world situation: Problem type 1
Interpreting a table of signed numbers that relate to a real−world situation: Problem type 2
Comparing signed numbers relating to a real−world situation
Identifying a sum as a point located a given distance from another point
Identifying relative change when combining two quantities
Addition and subtraction with 4 or 5 integers
Signed decimal addition and subtraction with 3 numbers
Word problem with addition or subtraction of integers
Word problem with multiplication or division of integers
Signed decimal multiplication
Signed decimal division
Finding opposites of integers
Finding all numbers with a given absolute value
Operations with absolute value: Problem type 1
Operations with absolute value: Problem type 2
Computing and understanding distances between integers on a number line
Order of operations with whole numbers and exponents: Advanced
Exponents and integers: Problem type 2
Order of operations with integers and exponents
Squaring decimal bases: Products greater than 0.1
Exponents and decimals: Products less than 0.1
Order of operations with decimals: Problem type 1
Order of operations with decimals: Problem type 2
Order of operations with decimals: Problem type 3
Modeling and writing equivalent fractions
Fractional position on a number line
Ordering fractions with the same numerator
Identifying equivalent signed fractions
Modeling multiplication of proper fractions
Word problem involving multiplying a fraction and a whole number
Signed fraction multiplication: Advanced
Word problem involving fractions and multiplication
Multi-step word problem involving fractions and multiplication
Determining if a quantity is increased or decreased when multiplied by a fraction
The reciprocal of a number
Division involving a whole number and a fraction
Fraction division
Modeling division of a whole number by a fraction
Signed fraction division
Word problem involving fractions and division
Exponents and signed fractions
Complex fraction without variables: Problem type 1
Introduction to adding fractions with variables and common denominators
Decomposing a fraction into a sum of fractions with the same denominator
Word problem involving addition or subtraction of fractions with the same denominator
Addition or subtraction of unit fractions
Addition and subtraction of 3 fractions with different denominators
Signed fraction subtraction involving double negation
Signed fraction addition or subtraction: Advanced
Addition and subtraction of 3 fractions involving signs
Word problem involving addition or subtraction of fractions with different denominators
Fractional part of a circle
Adding rational expressions with different denominators and a single occurrence of a variable
Order of operations with fractions: Problem type 1
Order of operations with fractions: Problem type 2
Order of operations with fractions: Problem type 3
Writing a mixed number and an improper fraction for a shaded region
Writing an improper fraction as a mixed number
Writing a mixed number as an improper fraction
Plotting rational numbers on a number line
Addition or subtraction of mixed numbers with the same denominator
Mixed number addition with the same denominator and renaming
Mixed number subtraction with the same denominator and renaming
Addition or subtraction of mixed numbers with different denominators without renaming
Addition of mixed numbers with different denominators and renaming
Subtraction of mixed numbers with different denominators and renaming
Addition and subtraction of 3 mixed numbers with different denominators
Word problem involving addition or subtraction of mixed numbers with different denominators
Mixed number multiplication
Multiplication of a mixed number and a whole number
Division with a mixed number and a whole number
Mixed number division
Word problem involving multiplication or division with mixed numbers
Converting a decimal to a proper fraction without simplifying: Advanced
Converting a decimal to a proper fraction in simplest form: Advanced
Converting a decimal to a mixed number and an improper fraction without simplifying
Converting a decimal to a mixed number and an improper fraction in simplest form: Basic
Converting a decimal to a mixed number and an improper fraction in simplest form: Advanced
Converting a mixed number with a denominator of 2, 4, or 5 to a decimal
Converting a fraction to a terminating decimal: Advanced
Converting a fraction to a repeating decimal: Advanced
Multiplicative property of equality with whole numbers: Fractional answers
Converting a repeating decimal to a fraction
Converting a mixed number to a terminating decimal: Basic
Converting a mixed number to a terminating decimal: Advanced
Converting a fraction or mixed number to a rounded decimal
Ordering fractions and decimals
Addition or subtraction with a decimal and a mixed number
Multiplication with a decimal and a fraction
Constructing a Venn diagram to classify rational numbers
Constructing a Venn diagram to describe relationships between sets of rational numbers
Properties of addition
Properties of real numbers
Ordering real numbers
Using numerical methods to approximate a square root to the nearest tenth
Using numerical methods to approximate a square root to the nearest hundredth
Approximating the location of irrational numbers on a number line
Simplifying the square root of a whole number less than 100
Simplifying the square root of a whole number greater than 100
Square root addition or subtraction
Square root addition or subtraction with three terms
Square root multiplication: Basic
Rationalizing a denominator: Quotient involving square roots
Rationalizing a denominator: Square root of a fraction
Cube root of an integer
Finding \( n \)th roots of perfect \( n \)th powers with signs
Ordering numbers with positive exponents
Introduction to the power of a power rule with positive exponents: Whole number base
Understanding the power rules of exponents
Power and product rules with positive exponents
Simplifying a ratio of multivariate monomials: Basic
Introduction to the quotient rule with positive exponents: Whole number base
Quotient of expressions involving exponents
Simplifying a ratio of multivariate monomials: Advanced
Power and quotient rules with positive exponents
Power of 10: Negative exponent
Evaluating an expression with a negative exponent: Negative integer base
Ordering numbers with negative exponents
Introduction to the product rule with negative exponents: Whole number base
Introduction to the product rule with negative exponents
Introduction to the quotient rule with negative exponents: Whole number base
Quotient rule with negative exponents: Problem type 1
Introduction to the power of a power rule with negative exponents: Whole number base
Product rule with negative exponents
Quotient rule with negative exponents: Problem type 2
Power of a power rule with negative exponents
Power rules with negative exponents
Power and quotient rules with negative exponents: Problem type 1
Power and quotient rules with negative exponents: Problem type 2
Power, product, and quotient rules with negative exponents
Estimating numbers using scientific notation
Expressing calculator notation as scientific notation
Multiplying numbers written in scientific notation: Basic
Multiplying numbers written in scientific notation: Advanced
Multiplying numbers written in decimal form or scientific notation in a real-world situation
Dividing numbers written in scientific notation: Basic
Dividing numbers written in scientific notation: Advanced
Finding the scale factor between numbers given in scientific notation in a real-world situation
Adding or subtracting numbers written in scientific notation: Same exponents, basic
Adding or subtracting numbers written in scientific notation: Same exponents, advanced
Adding or subtracting numbers written in scientific notation: Different exponents
Estimating the sum or difference of two numbers written in scientific notation

Algebraic Equations and Inequalities (149 topics)
Evaluating an algebraic expression: Whole number operations and exponents
Evaluating a linear expression: Signed fraction multiplication with addition or subtraction
Evaluating a linear expression: Signed decimal addition and subtraction
Evaluating a linear expression: Signed decimal multiplication with addition or subtraction
Combining like terms: Decimal coefficients
Combining like terms: Fractional coefficients
Identifying parts in an algebraic expression
Distributive property: Fractional coefficients
Using distribution with double negation and combining like terms to simplify: Multivariate
Additive property of equality with fractions and mixed numbers
Additive property of equality with a negative coefficient
Solving an equation to find the value of an expression
Solving a two-step equation with signed decimals
Clearing fractions in an equation
Solving a linear equation with several occurrences of the variable: Fractional forms with monomial numerators
Solving a two-step equation with signed fractions
Solving a linear equation with several occurrences of the variable: Variables on both sides and fractional coefficients
Solving a linear equation with several occurrences of the variable: Fractional forms with binomial numerators
Introduction to solving an absolute value equation
Solving an absolute value equation: Problem type 1
Solving for a variable in terms of other variables using addition or subtraction: Advanced
Solving for a variable inside parentheses in terms of other variables
Solving for a variable in terms of other variables in a linear equation with fractions
Comparing arithmetic and algebraic solutions to a word problem
Writing an equation of the form A(x + B) = C to solve a word problem
◊ Writing a multi−step equation for a real−world situation
◊ Writing and solving a real−world problem given an equation with the variable on both sides
◊ Solving a decimal word problem using a linear equation with the variable on both sides
◊ Solving a fraction word problem using a linear equation with the variable on both sides
◊ Solving a word problem with three unknowns using a linear equation
◊ Solving a word problem involving consecutive integers
◊ Solving a value mixture problem using a linear equation
◊ Solving a word problem involving rates and time conversion
◊ Solving a distance, rate, time problem using a linear equation
◊ Solving a percent mixture problem using a linear equation
◊ Finding the dimensions of a rectangle given its perimeter and a relationship between sides
◊ Finding the perimeter or area of a rectangle given one of these values
◊ Writing ratios using different notations
◊ Writing ratios for real−world situations
◊ Identifying statements that describe a ratio
◊ Simplifying a ratio of decimals
◊ Using a table of equivalent ratios to find a missing quantity in a ratio
◊ Word problem on unit rates associated with ratios of fractions
◊ Solving a proportion of the form (x+a)/b = c/d
◊ Solving a rational equation that simplifies to linear: Denominator x
◊ Word problem with powers of ten
◊ Finding a scale factor: Same units
◊ Using a scale drawing to find actual area
◊ Reproducing a scale drawing at a different scale
◊ Making a table and plotting points given a unit rate
◊ Identifying proportional relationships in equations
◊ Identifying proportional relationships in tables by calculating unit rates: Whole numbers
◊ Identifying proportional relationships in tables by calculating unit rates: Fractions
◊ Identifying proportional relationships in graphs: Basic
◊ Identifying proportional relationships in graphs: Advanced
◊ Comparing proportional relationships given in different forms
◊ Identifying direct variation equations
◊ Identifying direct variation from ordered pairs and writing equations
◊ Writing a direct variation equation
◊ Word problem on direct variation
◊ Writing an inverse variation equation
◊ Identifying direct and inverse variation equations
◊ Identifying direct and inverse variation from ordered pairs and writing equations
◊ Word problem on inverse variation
◊ Word problem on inverse proportions
◊ Writing an equation that models variation
◊ Word problem on combined variation
◊ Additive property of inequality with signed fractions
◊ Additive property of inequality with signed decimals
◊ Identifying solutions to a two−step linear inequality in one variable
◊ Solving a two−step linear inequality with a fractional coefficient
◊ Solving a linear inequality with multiple occurrences of the variable: Problem type 1
◊ Solving a linear inequality with multiple occurrences of the variable: Problem type 2
◊ Solving a linear inequality with multiple occurrences of the variable: Problem type 3
◊ Solving inequalities with no solution or all real numbers as solutions
◊ Writing an inequality given a graph on the number line
◊ Graphing a compound inequality on the number line
◊ Writing a compound inequality given a graph on the number line
◊ Set–builder and interval notation
◊ Solving a compound linear inequality: Graph solution, basic
◊ Solving a compound linear inequality: Interval notation
◊ Solving an absolute value inequality: Problem type 1
◊ Translating a sentence into a compound inequality
◊ Translating a sentence into a multi–step inequality
◊ Solving a word problem using a two–step linear inequality and describing the solution
◊ Solving a decimal word problem using a linear inequality with the variable on both sides
◊ Degree and leading coefficient of a univariate polynomial
◊ Degree of a multivariate polynomial
◊ Simplifying a sum or difference of three univariate polynomials
◊ Simplifying a sum or difference of multivariate polynomials
◊ Multiplying a univariate polynomial by a monomial with a positive coefficient
◊ Multiplying a univariate polynomial by a monomial with a negative coefficient
◊ Multiplying a multivariate polynomial by a monomial
◊ Multiplying binomials in two variables
◊ Multiplying conjugate binomials: Univariate
◊ Multiplying conjugate binomials: Multivariate
◊ Squaring a binomial: Multivariate
◊ Multiplying binomials with negative coefficients
◊ Multiplication involving binomials and trinomials in one variable
◊ Multiplication involving binomials and trinomials in two variables
◊ Dividing a polynomial by a monomial: Univariate
◊ Dividing a polynomial by a monomial: Multivariate
◊ Polynomial long division: Problem type 1
◊ Polynomial long division: Problem type 2
◊ Polynomial long division: Problem type 3
◊ Closure properties of integers and polynomials
◊ Introduction to the GCF of two monomials
◊ Greatest common factor of three univariate monomials
◊ Greatest common factor of two multivariate monomials
◊ Factoring out a monomial from a polynomial: Univariate
◊ Factoring out a monomial from a polynomial: Multivariate
◊ Factoring out a binomial from a polynomial: GCF factoring, basic
◊ Factoring a univariate polynomial by grouping: Problem type 1
◊ Factoring a univariate polynomial by grouping: Problem type 2
◊ Factoring a multivariate polynomial by grouping: Problem type 1
◊ Factoring a multivariate polynomial by grouping: Problem type 2
◊ Factoring a quadratic in two variables with leading coefficient 1
◊ Factoring out a constant before factoring a quadratic
◊ Factoring a quadratic with leading coefficient greater than 1: Problem type 2
◊ Factoring a quadratic with leading coefficient greater than 1: Problem type 3
◊ Factoring a quadratic by the ac–method
◊ Factoring a quadratic in two variables with leading coefficient greater than 1
◊ Factoring a quadratic with a negative leading coefficient
◊ Factoring a perfect square trinomial with leading coefficient greater than 1
◊ Factoring a perfect square trinomial in two variables
◊ Factoring a difference of squares in one variable: Basic
◊ Factoring a difference of squares in one variable: Advanced
◊ Factoring a difference of squares in two variables
◊ Factoring a polynomial involving a GCF and a difference of squares: Univariate
◊ Factoring a polynomial involving a GCF and a difference of squares: Multivariate
◊ Factoring a product of a quadratic trinomial and a monomial
Factoring with repeated use of the difference of squares formula
Factoring a sum or difference of two cubes
Finding the roots of a quadratic equation of the form \( ax^2 + bx = 0 \)
Finding the roots of a quadratic equation with leading coefficient greater than 1
Solving a quadratic equation needing simplification
Solving a word problem using a quadratic equation with rational roots
Solving an equation of the form \( x^2 = a \) using the square root property
Solving a quadratic equation using the square root property: Exact answers, basic
Solving a quadratic equation using the square root property: Exact answers, advanced
Applying the quadratic formula: Decimal answers
Discriminant of a quadratic equation
Completing the square
Solving a quadratic equation by completing the square: Exact answers
Introduction to solving a radical equation
Solving a radical equation that simplifies to a linear equation: One radical, basic
Word problem involving radical equations: Basic
Solving an equation of the form \( x^3 = a \) using integers
Solving an equation using the odd−root property: Problem type 1

Graphs, Functions, and Systems (171 topics)

Naming the quadrant or axis of a point given its graph
Naming the quadrant or axis of a point given its coordinates
Naming the quadrant or axis of a point given the signs of its coordinates
Finding distances between points that share a common coordinate given their coordinates
Finding \( x\)- and \( y\)-intercepts of a line given the equation: Advanced
Interpreting direct variation from a graph
Finding the coordinate that yields a given slope
Graphing a line through a given point with a given slope
Identifying linear equations: Basic
Identifying linear equations: Advanced
Identifying linear functions given ordered pairs
Rewriting a linear equation in the form \( Ax + By = C \)
Graphing a line by first finding its slope and \( y\)-intercept
Writing an equation and graphing a line given its slope and \( y\)-intercept
Finding the slope, \( y\)-intercept, and equation for a linear function given a table of values
Graphing a line given its equation in point−slope form
Writing an equation in point−slope form given the slope and a point
Writing the equations of vertical and horizontal lines through a given point
Graphing ordered pairs and writing an equation from a table of values in context
Writing a function rule given a table of ordered pairs: Two−step rules
Finding the initial amount and rate of change given a table for a linear function
Combining functions to write a new function that models a real−world situation
Comparing properties of linear functions given in different forms
Application problem with a linear function: Finding a coordinate given the slope and a point
Application problem with a linear function: Finding a coordinate given two points
Solving a linear equation by graphing
Finding slopes of lines parallel and perpendicular to a line given in slope−intercept form
Finding slopes of lines parallel and perpendicular to a line given in the form \( Ax + By = C \)
Identifying parallel and perpendicular lines from equations
Writing equations of lines parallel and perpendicular to a given line through a point
Identifying parallel and perpendicular lines from coordinates
Writing a system of linear equations given its graph
Solving a system of linear equations with fractional coefficients
Solving a system of linear equations with decimal coefficients
◊ Solving systems of linear equations with 0, 1, or infinitely many solutions
◊ Identifying the operations used to create equivalent systems of equations
◊ Introduction to solving a 3x3 system of linear equations
◊ Solving a 3x3 system of linear equations: Problem type 1
◊ Solving a percent mixture problem using a system of linear equations
◊ Solving a distance, rate, time problem using a system of linear equations
◊ Solving a tax rate or interest rate problem using a system of linear equations
◊ Solving a word problem using a 3x3 system of linear equations: Problem type 1
◊ Solving a word problem using a 3x3 system of linear equations: Problem type 2
◊ Scalar multiplication of a matrix
◊ Addition or subtraction of matrices
◊ Linear combination of matrices
◊ Multiplication of matrices: Basic
◊ Squaring and multiplying 2x2 matrices
◊ Word problem involving multiplication of matrices
◊ Completing Gauss–Jordan elimination with a 2x2 matrix
◊ Gauss–Jordan elimination with a 2x2 matrix
◊ Identifying solutions to a linear inequality in two variables
◊ Graphing a linear inequality in the plane: Vertical or horizontal line
◊ Graphing a linear inequality in the plane: Slope–intercept form
◊ Graphing a linear inequality in the plane: Standard form
◊ Graphing a system of two linear inequalities: Basic
◊ Graphing a system of two linear inequalities: Advanced
◊ Graphing a system of three linear inequalities
◊ Writing a multi–step inequality for a real–world situation
◊ Writing a linear inequality in two variables given a table of values
◊ Solving a word problem using a system of linear inequalities: Problem type 1
◊ Solving a word problem using a system of linear inequalities: Problem type 2
◊ Linear programming
◊ Solving a word problem using linear programming
◊ Identifying functions from relations
◊ Domain and range from ordered pairs
◊ Variable expressions as inputs of functions: Problem type 1
◊ Domain and range of a linear function that models a real–world situation
◊ Finding an output of a function from its graph
◊ Finding inputs and outputs of a function from its graph
◊ Domain and range from the graph of a discrete relation
◊ Finding domain and range from a linear graph in context
◊ Finding intercepts of a nonlinear function given its graph
◊ Finding where a function is increasing, decreasing, or constant given the graph
◊ Finding where a function is increasing, decreasing, or constant given the graph: Interval notation
◊ Finding local maxima and minima of a function given the graph
◊ Choosing a graph to fit a narrative: Basic
◊ Choosing a graph to fit a narrative: Advanced
◊ Graphing an integer function and finding its range for a given domain
◊ Domain and range from the graph of a continuous function
◊ Graphing a function of the form f(x) = ax + b: Integer slope
◊ Graphing a function of the form f(x) = ax + b: Fractional slope
◊ Graphing a function of the form f(x) = ax^2
◊ Graphing a function of the form f(x) = ax^2 + c
◊ Translating the graph of an absolute value function: One step
◊ Translating the graph of an absolute value function: Two steps
◊ Graphing an absolute value equation of the form y = A|x|
- Writing an expression as a single logarithm
- Change of base for logarithms: Problem type 1
- Solving a multi-step equation involving a single logarithm: Problem type 1
- Solving a multi-step equation involving a single logarithm: Problem type 2
- Solving a multi-step equation involving natural logarithms
- Solving an equation involving logarithms on both sides: Problem type 1
- Solving an equation involving logarithms on both sides: Problem type 2
- Solving an exponential equation by using logarithms: Decimal answers, basic
- Solving an exponential equation by using natural logarithms: Decimal answers
- Finding the time given an exponential function with base e that models a real-world situation
- Finding the final amount in a word problem on continuous exponential growth or decay
- Finding the first terms of an arithmetic sequence using an explicit rule
- Finding the first terms of a geometric sequence using an explicit rule
- Finding the first terms of a sequence using an explicit rule with multiple occurrences of n
- Finding the next terms of an arithmetic sequence with integers
- Finding the first terms of a sequence using a recursive rule
- Identifying arithmetic sequences and finding the common difference
- Finding a specified term of an arithmetic sequence given the first terms
- Finding a specified term of an arithmetic sequence given the common difference and first term
- Finding a specified term of an arithmetic sequence given two terms of the sequence
- Writing an explicit rule for an arithmetic sequence
- Writing a recursive rule for an arithmetic sequence
- Finding the next terms of a geometric sequence with signed numbers
- Identifying arithmetic and geometric sequences
- Identifying geometric sequences and finding the common ratio
- Finding a specified term of a geometric sequence given the first terms
- Finding a specified term of a geometric sequence given the common ratio and first term
- Finding a specified term of a geometric sequence given two terms of the sequence
- Arithmetic and geometric sequences: Identifying and writing an explicit rule
- Writing recursive rules for arithmetic and geometric sequences
- Identifying linear, quadratic, and exponential functions given ordered pairs

- Consumer Mathematics (26 topics)
  - Converting a mixed number percentage to a decimal
  - Converting a percentage to a fraction in simplest form
  - Converting a decimal percentage to a fraction
  - Calculating relative frequencies in a contingency table
  - Finding the absolute error and percent error of a measurement
  - Computing a percent mixture
  - FICA with no ceiling
  - FICA with ceiling
  - The U.S. Rule: Making partial note payments before due date
  - Finding the final amount of a loan or investment earning continuous compound interest
  - Finding the initial amount of an investment earning continuous compound interest
  - Finding the time required for an investment earning compound interest
  - Finding the rate or time in a word problem on continuous exponential growth or decay
  - Finding half-life or doubling time
  - Annuity due
  - Sinking funds
  - Using an annual percentage rate table to find the APR for an installment purchase
  - Comparing monthly payments for subsidized and unsubsidized student loans
  - Calculating and comparing monthly payments using the ALEKS loan calculator
  - Calculating monthly payment, total payment, and interest using the ALEKS loan calculator
  - Calculating and comparing total loan payments using the ALEKS loan calculator
Dod Using the ALEKS periodic deposit calculator to compute savings which include periodic deposits
◊ Stock yield, earnings per share, and price–earnings ratio
◊ Stock dividends
◊ Net asset value of a mutual fund
◊ Calculating bond yields
♦ Measurement (17 topics)
◊ Measuring length to the nearest inch
◊ Measuring length to the nearest quarter or half inch
◊ Adding measurements in feet and inches
◊ Perimeter of a rectangle on a grid
◊ Computations involving density, mass, and volume
◊ Word problem on density involving the volume of a rectangular solid
◊ Surface area of a rectangular prism made of unit cubes
◊ Unit conversions involving acres and hectares
◊ Converting between U.S. Customary units of volume: Problem type 1
◊ U.S. Customary unit conversion with mixed number values: One–step conversion
◊ U.S. Customary unit conversion with mixed number values: Two–step conversion
◊ Measuring length to the nearest centimeter
◊ Measuring length to the nearest millimeter
◊ Choosing metric units and converting to the base unit in scientific notation
◊ Metric distance conversions between the base unit m and dm, dam, hm
◊ Adding time
◊ Elapsed time
♦ Geometry (104 topics)
◊ Naming segments, rays, and lines
◊ Drawing an angle with the protractor
◊ Naming angles, sides of angles, and vertices
◊ Solving an equation involving complementary or supplementary angles
◊ Writing and solving an equation involving complementary or supplementary angles
◊ Solving equations involving vertical angles
◊ Solving equations involving angles and a pair of parallel lines
◊ Computing distances between decimals on a number line
◊ Finding a point on a number line given the length of a segment and another point
◊ Finding an angle measure given extended triangles
◊ Finding angle measures of a triangle given angles with variables
◊ Writing an equation to find angle measures of a triangle given angles with variables
◊ Finding side lengths and angle measures of isosceles and equilateral triangles
◊ Finding angle measures of an isosceles triangle given angles with variables
◊ Using the Pythagorean Theorem repeatedly
◊ Using the Pythagorean Theorem and a quadratic equation to find side lengths of a right triangle
◊ Using the Pythagorean Theorem to find distance on a grid
◊ Distance between two points in the plane: Exact answers
◊ Distance between two points in the plane: Decimal answers
◊ Midpoint of a line segment in the plane
◊ Sides of polygons having the same perimeter
◊ Perimeter of a polygon involving mixed numbers and fractions
◊ Finding a side length given the perimeter and side lengths with variables
◊ Naming polygons
◊ Shared attributes among categories of quadrilaterals
◊ Finding the sum of the interior angle measures of a convex polygon given the number of sides
◊ Finding a missing interior angle measure in a convex polygon
◊ Classifying parallelograms
◊ Area of a rectangle involving fractions
◊ Area of a rectangle involving mixed numbers and fractions
◊ Distinguishing between the area and perimeter of a rectangle
◊ Areas of rectangles with the same perimeter
◊ Word problem on optimizing an area or perimeter
◊ Word problem involving the area between two rectangles
◊ Investigating the effects on the area for non–proportional and proportional figures
◊ Solving a word problem involving area using a one–step linear inequality: Area and lengths
◊ Finding counterexamples to conjectures
◊ Introduction to a circle: Diameter, radius, and chord
◊ Finding the radius or the diameter of a circle given its circumference
◊ Circumference ratios
◊ Circumference and area of a circle
◊ Distinguishing between the area and circumference of a circle
◊ Area between two concentric circles
◊ Word problem involving the area between two concentric circles
◊ Area involving inscribed figures
◊ Counting the cubes in a solid made of cubes
◊ Word problem involving the rate of filling or emptying a rectangular prism
◊ Volume of a piecewise rectangular prism
◊ Word problem involving the volume of a piecewise rectangular prism
◊ Word problem involving the volume of a triangular prism
◊ Word problem involving the volume of a cylinder
◊ Word problem involving the rate of filling or emptying a cylinder
◊ Word problem on density involving the volume of a cylindrical solid
◊ Word problem involving the volume of a cone
◊ Word problem involving the volume of a sphere
◊ Ratio of volumes
◊ Nets of solids
◊ Side views of a solid made of cubes
◊ Distinguishing between surface area and volume
◊ Surface area of a piecewise rectangular prism made of unit cubes
◊ Surface area of a triangular prism
◊ Word problem involving the surface area of a cylinder
◊ Word problem involving the surface area of rectangular prisms and cylinders
◊ Word problem involving the surface area of rectangular prisms and pyramids
◊ Identifying and naming congruent parts of congruent triangles
◊ Identifying and naming congruent triangles
◊ Identifying similar or congruent shapes on a grid
◊ Triangles and parallel lines
◊ Using right triangles to find the slope of a line
◊ Computing ratios of side lengths, surface areas, and volumes for similar solids
◊ Identifying transformations
◊ Translating a point and giving its coordinates: Two steps
◊ Translating a polygon
◊ Determining if figures are related by a translation
◊ Reflecting a point across an axis and giving its coordinates
◊ Reflecting a polygon across the x–axis or y–axis
◊ Reflecting a polygon over a vertical or horizontal line
◊ Determining if figures are related by a reflection
◊ Drawing lines of symmetry
◊ Rotating a point and giving its coordinates
◊ Rotating a figure about the origin
◊ Determining if figures are related by a rotation
Determining if figures are congruent and related by a transformation
Finding an angle of rotation
Identifying rotational symmetry and angles of rotation
Dilating a segment and giving the coordinates of its endpoints
Dilating a figure
Determining if figures are related by a dilation
Special right triangles: Exact answers
Sine, cosine, and tangent ratios: Variables for side lengths
Using the Pythagorean Theorem to find a trigonometric ratio
Finding trigonometric ratios given a right triangle
Understanding trigonometric ratios through similar right triangles
Relationship between the sines and cosines of complementary angles
Solving a right triangle
Using trigonometry to find a length in a word problem with two right triangles
Simplifying trigonometric expressions
Solving a triangle with the law of sines: Problem type 1
Solving a word problem using the law of sines
Solving a triangle with the law of cosines
Solving a word problem using the law of cosines
Using trigonometry to find the area of a right triangle
Finding the area of a triangle using trigonometry
Heron’s formula

Counting and Probability (29 topics)
Counting using combinations and a complement
Counting five-card hands from a standard deck
Experimental and theoretical probability for compound events
Probabilities of a permutation and a combination
Area as probability
Finding odds in favor and against drawing a card from a standard deck
Making predictions using experimental data for compound events
Computing expected value in a business application
Making reasonable inferences based on proportion statistics
Identifying independent events given descriptions of experiments
Probability of dependent events involving a standard deck of cards
Probability of dependent events involving a survey
Probabilities of draws with replacement
Probability of five-card hands
Using a Venn diagram to understand the multiplication rule for probability
Outcomes and event probability: Conditional probability
Identifying independent events given values of probabilities
Computing conditional probability to make an inference using a two-way frequency table
Tree diagrams for conditional probabilities
Outcomes and event probability: Addition rule
Using a Venn diagram to understand the addition rule for probability
Probability of intersection or union: Word problems
Computing conditional probability using a large two-way frequency table
Probability of the union of two events
Intersection and conditional probability
Law of total probabilities
Bayes' theorem
Using the binomial formula to solve a word problem: Problem type 1
Using the binomial formula to solve a word problem: Problem type 2

Statistics (42 topics)
Choosing an appropriate method for gathering data: Problem type 1
Classification of variables
Making an inference using a two-way frequency table
Discrete versus continuous variables
Finding if a question can be answered by the data
Using a model to find the mean
Understanding the mean graphically: Two bars
Understanding the mean graphically: Four or more bars
Finding the mean of a symmetric distribution
Summation of indexed data
Comparing means without calculation
Finding the mode and range from a line plot
Comparing sample means
Comparing standard deviations without calculation
Sample standard deviation
Computing mean absolute deviation from a list of numerical values
Using box-and-whisker plots to compare data sets
Using the graph of a distribution to find probabilities: Advanced
Normal versus standard normal density curves
Finding a probability given a normal distribution: Advanced
Discrete probability distribution: Basic
Standard normal values: Basic
Standard normal values: Advanced
Finding a raw score given a normal distribution
Chebyshev’s theorem and the empirical rule
Central limit theorem: Sample mean
Identifying independent and dependent variables from equations or real-world situations
Classifying linear and nonlinear relationships from scatter plots
Computing residuals
Interpreting residual plots
Identifying correlation and causation
Choosing a quadratic model and using it to make a prediction
Choosing an exponential model and using it to make a prediction
Identifying outcomes in a random number table used to simulate a simple event
Using a random number table to simulate a simple event
Constructing a percent bar graph
Generating a random number table with technology to simulate a simple event
Identifying outcomes in a random number table used to simulate a compound event
Using a random number table to simulate a compound event
Generating a random number table with technology to simulate a compound event
Generating random samples from a population with known characteristics
Using a random number table to make a fair decision

♦ Voting and Apportionment (4 topics)
  ◊ Creating a preference table from ballots
  ◊ Plurality-with-elimination method: Two eliminations
  ◊ Interpreting an approval table
  ◊ Approval voting

♦ Graph Theory (6 topics)
  ◊ Coloring and chromatic number
  ◊ Coloring a graph in context
  ◊ Drawing a graph to represent relationships
  ◊ Application of graph coloring
  ◊ Connected, disconnected, and bridges: Drawing
Using the cheapest link method to approximate an optimal Hamilton circuit

*Other Topics Available* By default, these topics are NOT included in the course, but can be added using the content editor in the Teacher Module.