Prep for PreCalculus

This course covers the topics outlined below. You can customize the scope and sequence of this course to meet your curricular needs.

Curriculum (246 topics + 58 additional topics)

- Real Numbers (30 topics)
  - Fractions (5 topics)
    - Simplifying a fraction
    - Using a common denominator to order fractions
    - Addition or subtraction of fractions with different denominators
    - Fraction multiplication
    - Fraction division
  - Percents and Proportions (8 topics)
    - Converting between percentages and decimals
    - Applying the percent equation
    - Finding the sale price without a calculator given the original price and percent discount
    - Finding the original price given the sale price and percent discount
    - Finding simple interest without a calculator
    - Solving a proportion of the form \( \frac{x}{a} = \frac{b}{c} \)
    - Word problem on proportions: Problem type 1
    - Word problem on proportions: Problem type 2
- Signed Numbers (15 topics)
  - Integer addition: Problem type 2
  - Integer subtraction: Problem type 3
  - Signed fraction addition or subtraction: Basic
  - Signed fraction addition or subtraction: Advanced
  - Signed decimal addition and subtraction with 3 numbers
  - Integer multiplication and division
  - Signed fraction multiplication: Basic
  - Signed fraction multiplication: Advanced
  - Exponents and integers: Problem type 1
  - Exponents and signed fractions
  - Order of operations with integers and exponents
  - Evaluating a linear expression: Integer multiplication with addition or subtraction
  - Evaluating a quadratic expression: Integers
  - Absolute value of a number
  - Operations with absolute value: Problem type 2
- Properties of Real Numbers (2 topics)
  - Identifying numbers as integers or non–integers
  - Identifying numbers as rational or irrational
- Equations and Inequalities (32 topics)
  - Linear Equations (20 topics)
    - Additive property of equality with integers
    - Multiplicative property of equality with signed fractions
    - Solving a two–step equation with integers
◊ Solving a two–step equation with signed fractions
◊ Solving a linear equation with several occurrences of the variable: Variables on the same side and distribution
◊ Solving a linear equation with several occurrences of the variable: Variables on both sides and fractional coefficients
◊ Solving a linear equation with several occurrences of the variable: Variables on both sides and distribution
◊ Solving a linear equation with several occurrences of the variable: Variables on both sides and two distributions
◊ Solving a linear equation with several occurrences of the variable: Fractional forms with binomial numerators
◊ Solving equations with zero, one, or infinitely many solutions
◊ Algebraic symbol manipulation: Problem type 1
◊ Algebraic symbol manipulation: Problem type 2
◊ Writing a one–step expression for a real–world situation
◊ Translating a phrase into a two–step expression
◊ Translating a sentence into a one–step equation
◊ Solving a word problem with two unknowns using a linear equation
◊ Solving a decimal word problem using a linear equation of the form $Ax + B = C$
◊ Solving a value mixture problem using a linear equation
◊ Solving a percent mixture problem using a linear equation
◊ Solving a distance, rate, time problem using a linear equation

♦ Linear Inequalities (9 topics)
◊ Graphing a linear inequality on the number line
◊ Graphing a compound inequality on the number line
◊ Solving a linear inequality: Problem type 1
◊ Solving a linear inequality: Problem type 2
◊ Solving a linear inequality: Problem type 3
◊ Solving a linear inequality: Problem type 4
◊ Solving a compound linear inequality: Graph solution, basic
◊ Solving a compound linear inequality: Interval notation
◊ Solving a decimal word problem using a two–step linear inequality

♦ Absolute Value Equations and Inequalities (3 topics)
◊ Solving an absolute value equation of the form $a|x| = b$ or $|x|+a = b$
◊ Solving an absolute value equation of the form $|ax+b| = c$
◊ Solving an absolute value inequality: Basic

• Exponents and Polynomials (44 topics)
♦ Properties of Exponents (13 topics)
◊ Evaluating an expression with a negative exponent: Positive fraction base
◊ Evaluating an expression with a negative exponent: Negative integer base
◊ Rewriting an algebraic expression without a negative exponent
◊ Introduction to the product rule of exponents
◊ Product rule with positive exponents: Multivariate
◊ Product rule with negative exponents
◊ Quotient of expressions involving exponents
◊ Quotient rule with negative exponents: Problem type 1
◊ Introduction to the power rules of exponents
◊ Power rules with positive exponents
◊ Power of a power rule with negative exponents
◊ Power rules with negative exponents
◊ Power and product rules with positive exponents

♦ Scientific Notation (2 topics)
◊ Scientific notation with positive exponent
- Scientific notation with negative exponent
- **Polynomial Expressions** (9 topics)
  - Degree and leading coefficient of a univariate polynomial
  - Combining like terms: Advanced
  - Simplifying a sum or difference of two univariate polynomials
  - Multiplying a univariate polynomial by a monomial with a positive coefficient
  - Multiplying a multivariate polynomial by a monomial
  - Multiplying binomials with leading coefficients of 1
  - Multiplying conjugate binomials: Univariate
  - Squaring a binomial: Univariate
  - Multiplication involving binomials and trinomials in two variables
- **Factoring** (9 topics)
  - Introduction to the GCF of two monomials
  - Greatest common factor of two multivariate monomials
  - Factoring out a monomial from a polynomial: Univariate
  - Factoring out a monomial from a polynomial: Multivariate
  - Factoring a quadratic with leading coefficient 1
  - Factoring a quadratic with leading coefficient greater than 1
  - Factoring a product of a quadratic trinomial and a monomial
  - Factoring a difference of squares
  - Factoring a polynomial by grouping: Problem type 1
- **Quadratic Equations** (11 topics)
  - Solving an equation written in factored form
  - Finding the roots of a quadratic equation with leading coefficient 1
  - Finding the roots of a quadratic equation with leading coefficient greater than 1
  - Solving a quadratic equation needing simplification
  - Completing the square
  - Applying the quadratic formula: Exact answers
  - Discriminant of a quadratic equation
  - Solving a word problem using a quadratic equation with rational roots
  - Solving a word problem using a quadratic equation with irrational roots
  - Solving a quadratic inequality written in factored form
- **Lines and Systems** (33 topics)
  - **Ordered Pairs** (3 topics)
    - Plotting a point in the coordinate plane
    - Finding a solution to a linear equation in two variables
    - Determining whether given points lie on one, both, or neither of 2 lines given equations
  - **Graphing Lines** (5 topics)
    - Graphing a line given its x– and y–intercepts
    - Graphing a line given its equation in slope–intercept form
    - Graphing a line given its equation in standard form
    - Graphing a line through a given point with a given slope
    - Graphing a vertical or horizontal line
  - **Equations of Lines** (13 topics)
    - Finding the y–intercept of a line given its equation
    - Finding x– and y–intercepts of a line given the equation: Advanced
    - Finding slope given the graph of a line on a grid
    - Finding slope given two points on the line
    - Finding the slope of a line given its equation
    - Writing an equation of a line given the y–intercept and another point
    - Writing the equation of a line given the slope and a point on the line
    - Writing the equation of the line through two given points
Finding slopes of lines parallel and perpendicular to a line given in the form $Ax + By = C$
Writing equations of lines parallel and perpendicular to a given line through a point
Writing an equation and drawing its graph to model a real-world situation: Advanced
Application problem with a linear function: Finding a coordinate given the slope and a point
Application problem with a linear function: Finding a coordinate given two points

- Graphing Linear Inequalities (3 topics)
  - Graphing a linear inequality in the plane: Standard form
  - Graphing a linear inequality in the plane: Vertical or horizontal line
  - Graphing a linear inequality in the plane: Slope-intercept form

- Systems of Linear Equations (9 topics)
  - Graphically solving a system of linear equations
  - Solving a system of linear equations using substitution
  - Solving a system of linear equations using elimination with multiplication and addition
  - Solving a word problem involving a sum and another basic relationship using a system of linear equations
  - Solving a value mixture problem using a system of linear equations
  - Solving a distance, rate, time problem using a system of linear equations
  - Solving a percent mixture problem using a system of linear equations
  - Interpreting the graphs of two functions
  - Graphing a system of two linear inequalities: Basic

- Functions and Graphs (29 topics)
  - Sets, Relations, and Functions (9 topics)
    - Union and intersection of finite sets
    - Set builder and interval notation
    - Identifying functions from relations
    - Vertical line test
    - Evaluating functions: Linear and quadratic or cubic
    - Evaluating functions: Absolute value, rational, radical
    - Evaluating a piecewise-defined function
    - Variable expressions as inputs of functions: Problem type 1
    - Domain and range from ordered pairs
  - Graphs and Transformations (16 topics)
    - Finding intercepts of a nonlinear function given its graph
    - Finding local maxima and minima of a function given the graph
    - Finding zeros of a polynomial function written in factored form
    - Domain and range from the graph of a continuous function
    - Writing an equation for a function after a vertical translation
    - Writing an equation for a function after a vertical and horizontal translation
    - Translating the graph of a function: One step
    - Translating the graph of a function: Two steps
    - Transforming the graph of a function by reflecting over an axis
    - Transforming the graph of a function by shrinking or stretching
    - Finding the x-intercept(s) and the vertex of a parabola
    - Graphing a parabola of the form $y = ax^2$
    - Graphing a parabola of the form $y = (x-h)^2 + k$
    - Graphing a parabola of the form $y = ax^2 + bx + c$: Integer coefficients
    - Graphing a cubic function of the form $y = ax^3$
    - Graphing an absolute value equation in the plane: Advanced
  - Combining Functions; Composite Functions; Inverse Functions (4 topics)
    - Sum, difference, and product of two functions
    - Quotient of two functions: Basic
    - Composition of two functions: Basic
    - Inverse functions: Linear, discrete
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<thead>
<tr>
<th>Topic</th>
<th>Subtopics</th>
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<td>Rational Expressions (27 topics)</td>
<td>◦ Domain of a rational function: Excluded values</td>
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<td>◦ Simplifying a ratio of polynomials: Problem type 1</td>
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<td>◦ Simplifying a ratio of polynomials: Problem type 2</td>
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<td>◦ Simplifying a ratio of multivariate polynomials</td>
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<td>◦ Multiplying rational expressions involving multivariate monomials</td>
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<td>◦ Multiplying rational expressions involving quadratics with leading coefficients of 1</td>
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<td>◦ Dividing rational expressions involving multivariate monomials</td>
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<td>◦ Introduction to the LCM of two monomials</td>
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<td>◦ Adding rational expressions with common denominators and binomial numerators</td>
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<td>◦ Adding rational expressions with different denominators: ax, bx</td>
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<td>◦ Adding rational expressions with different denominators: x+a, x+b</td>
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<td>◦ Complex fraction without variables: Problem type 1</td>
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<td>◦ Complex fraction without variables: Problem type 2</td>
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<td>◦ Complex fraction involving multivariate monomials</td>
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<td>◦ Complex fraction: GCF and quadratic factoring</td>
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<td>◦ Complex fraction made of sums involving rational expressions</td>
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<td>◦ Dividing a polynomial by a monomial: Univariate</td>
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<td>◦ Polynomial long division: Problem type 1</td>
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<td>◦ Polynomial long division: Problem type 2</td>
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<td>◦ Rational Equations (6 topics)</td>
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<td>◦ Solving a rational equation that simplifies to linear: Denominator x</td>
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<td>◦ Solving a rational equation that simplifies to linear: Denominator x+a</td>
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<td>◦ Solving a rational equation that simplifies to linear: Unlike binomial denominators</td>
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<td>◦ Solving a rational equation that simplifies to linear: Denominators a, x, or ax</td>
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<td>◦ Solving a rational equation that simplifies to quadratic: Binomial denominators, constant numerators</td>
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<td>◦ Solving a rational equation that simplifies to quadratic: Binomial denominators and numerators</td>
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<td>◦ Variation (2 topics)</td>
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<td>◦ Word problem on direct variation</td>
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<td>◦ Word problem on inverse variation</td>
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<td>◦ Radical Expressions (26 topics)</td>
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<td>◦ Radical Functions (2 topics)</td>
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<td>◦ Domain of a square root function: Advanced</td>
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<td>◦ Graphing a square root function</td>
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<td>◦ Radical Expressions (16 topics)</td>
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<td>◦ Square root of a rational perfect square</td>
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<td>◦ Cube root of an integer</td>
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<td>◦ Simplifying the square root of a whole number less than 100</td>
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<td>◦ Square root of a perfect square monomial</td>
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<td>◦ Simplifying a radical expression with an even exponent</td>
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<td>◦ Simplifying a radical expression with two variables</td>
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<td>◦ Simplifying a higher root of a whole number</td>
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<td>◦ Simplifying a higher radical expression: Multivariate</td>
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<td>◦ Square root addition or subtraction</td>
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<td>◦ Simplifying a sum or difference of radical expressions: Multivariate</td>
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<td>◦ Square root multiplication: Advanced</td>
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<td>◦ Simplifying a product of radical expressions: Multivariate</td>
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<td>◦ Simplifying a product involving square roots using the distributive property: Advanced</td>
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<td>◦ Special products of radical expressions: Conjugates and squaring</td>
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<td>◦ Rationalizing the denominator of a radical expression</td>
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<td>◦ Rationalizing the denominator of a radical expression using conjugates</td>
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<td>◦ Rational Exponents (5 topics)</td>
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Converting between radical form and exponent form
◊ Rational exponents: Non-unit fraction exponent with a whole number base
◊ Rational exponents: Negative exponents and fractional bases
◊ Rational exponents: Products and quotients with negative exponents
◊ Rational exponents: Powers of powers with negative exponents

♦ Radical Equations (3 topics)
◊ Solving a radical equation that simplifies to a linear equation: One radical, basic
◊ Solving a radical equation that simplifies to a linear equation: Two radicals
◊ Solving a radical equation that simplifies to a quadratic equation: One radical

♦ Geometry (25 topics)
◆ Perimeter, Area, and Volume (17 topics)
◊ Perimeter of a square or a rectangle
◊ Area of a square or a rectangle
◊ Area of a piecewise rectangular figure
◊ Finding a side length given the perimeter and side lengths with variables
◊ Finding the side length of a rectangle given its perimeter or area
◊ Finding the perimeter or area of a rectangle given one of these values
◊ Area of a parallelogram
◊ Area of a triangle
◊ Circumference and area of a circle
◊ Perimeter involving rectangles and circles
◊ Area involving inscribed figures
◊ Volume of a rectangular prism
◊ Volume of a cylinder
◊ Surface area of a cube or a rectangular prism
◊ Surface area of a cylinder: Exact answers in terms of pi
◊ Similar polygons
◊ Indirect measurement

◆ Angles (3 topics)
◊ Solving equations involving vertical angles
◊ Finding an angle measure of a triangle given two angles
◊ Finding an angle measure for a triangle with an extended side

◆ Coordinate Geometry (5 topics)
◊ Pythagorean Theorem
◊ Distance between two points in the plane: Exact answers
◊ Graphing a circle given its equation in standard form
◊ Graphing a circle given its equation in general form
◊ Writing an equation of a circle given its center and a point on the circle

• Other Topics Available(*) (58 additional topics)
◆ Real Numbers (6 topics)
◊ Fractional part of a circle
◊ Finding the percentage increase or decrease: Advanced
◊ Word problem on unit rates associated with ratios of whole numbers: Decimal answers
◊ Exponents and integers: Problem type 2
◊ Properties of addition
◊ Properties of real numbers

◆ Equations and Inequalities (6 topics)
◊ Solving an equation to find the value of an expression
◊ Solving a decimal word problem using a linear equation with the variable on both sides
◊ Solving a fraction word problem using a linear equation with the variable on both sides
◊ Solving a word problem with three unknowns using a linear equation
Writing a multi-step inequality for a real-world situation
Solving a decimal word problem using a linear inequality with the variable on both sides

Exponents and Polynomials (13 topics)
- Evaluating expressions with exponents of zero
- Ordering numbers with positive exponents
- Ordering numbers with negative exponents
- Power, product, and quotient rules with negative exponents
- Multiplying and dividing numbers written in scientific notation
- Degree of a multivariate polynomial
- Simplifying a sum or difference of three univariate polynomials
- Factoring with repeated use of the difference of squares formula
- Factoring a sum or difference of two cubes
- Solving an equation that can be written in quadratic form: Problem type 1
- Solving a quadratic equation using the square root property: Exact answers, advanced
- Solving a quadratic equation by completing the square: Exact answers
- Solving a quadratic inequality

Lines and Systems (5 topics)
- Writing the equations of vertical and horizontal lines through a given point
- Solving a 3x3 system of linear equations: Problem type 1
- Solving a 2x2 system of linear equations that is inconsistent or consistent dependent
- Solving a tax rate or interest rate problem using a system of linear equations
- Solving a word problem using a 3x3 system of linear equations: Problem type 1

Functions and Graphs (6 topics)
- Set builder notation
- Finding inputs and outputs of a function from its graph
- Finding where a function is increasing, decreasing, or constant given the graph: Interval notation
- Classifying the graph of a function
- Horizontal line test
- Determining whether two functions are inverses of each other

Rational Expressions (6 topics)
- Ordering fractions with variables
- Dividing rational expressions involving quadratics with leading coefficients of 1
- Least common multiple of two monomials
- Adding rational expressions with multivariate monomial denominators: Advanced
- Writing an equation that models variation
- Word problem on combined variation

Radical Expressions (8 topics)
- Rationalizing a denominator: Quotient involving higher radicals and monomials
- Using i to rewrite square roots of negative numbers
- Simplifying a product and quotient involving square roots of negative numbers
- Adding or subtracting complex numbers
- Multiplying complex numbers
- Dividing complex numbers
- Simplifying a power of i
- Solving a quadratic equation with complex roots

Geometry (8 topics)
- Areas of rectangles with the same perimeter
- Finding the radius or the diameter of a circle given its circumference
- Circumference ratios
- Area involving rectangles and circles
- Word problem involving the area between two concentric circles
- Word problem involving the rate of filling or emptying a cylinder
- Midpoint of a line segment in the plane
Writing an equation of a circle given the endpoints of a diameter

Other Topics Available  By default, these topics are NOT included in the course, but can be added using the content editor in the Teacher Module.