



## *College Algebra with Trigonometry*

This course covers the topics outlined below. You can customize the scope and sequence of this course to meet your curricular needs.

Curriculum (556 topics + 614 additional topics)

- Algebra and Geometry Review (126 topics)
  - ◆ Real Numbers and Algebraic Expressions (14 topics)
    - ◇ Signed fraction addition or subtraction: Basic
    - ◇ Signed fraction subtraction involving double negation
    - ◇ Signed fraction multiplication: Basic
    - ◇ Signed fraction division
    - ◇ Computing the distance between two integers on a number line
    - ◇ Exponents and integers: Problem type 1
    - ◇ Exponents and signed fractions
    - ◇ Order of operations with integers
    - ◇ Evaluating a linear expression: Integer multiplication with addition or subtraction
    - ◇ Evaluating a quadratic expression: Integers
    - ◇ Evaluating a linear expression: Signed fraction multiplication with addition or subtraction
    - ◇ Distributive property: Integer coefficients
    - ◇ Using distribution and combining like terms to simplify: Univariate
    - ◇ Using distribution with double negation and combining like terms to simplify: Multivariate
  - ◆ Exponents (20 topics)
    - ◇ Introduction to the product rule of exponents
    - ◇ Product rule with positive exponents: Univariate
    - ◇ Product rule with positive exponents: Multivariate
    - ◇ Introduction to the power of a power rule of exponents
    - ◇ Introduction to the power of a product rule of exponents
    - ◇ Power rules with positive exponents: Multivariate products
    - ◇ Power rules with positive exponents: Multivariate quotients
    - ◇ Simplifying a ratio of multivariate monomials: Basic
    - ◇ Introduction to the quotient rule of exponents
    - ◇ Simplifying a ratio of univariate monomials
    - ◇ Quotient of expressions involving exponents
    - ◇ Evaluating expressions with exponents of zero
    - ◇ Evaluating an expression with a negative exponent: Whole number base
    - ◇ Evaluating an expression with a negative exponent: Positive fraction base
    - ◇ Evaluating an expression with a negative exponent: Negative integer base
    - ◇ Rewriting an algebraic expression without a negative exponent
    - ◇ Introduction to the product rule with negative exponents
    - ◇ Quotient rule with negative exponents: Problem type 1
    - ◇ Power of a power rule with negative exponents
    - ◇ Power rules with negative exponents
  - ◆ Polynomial Expressions (14 topics)
    - ◇ Degree and leading coefficient of a univariate polynomial
    - ◇ Simplifying a sum or difference of two univariate polynomials

- ◇ Multiplying a univariate polynomial by a monomial with a positive coefficient
- ◇ Multiplying a univariate polynomial by a monomial with a negative coefficient
- ◇ Multiplying a multivariate polynomial by a monomial
- ◇ Multiplying binomials with leading coefficients of 1
- ◇ Multiplying binomials with leading coefficients greater than 1
- ◇ Multiplying binomials in two variables
- ◇ Multiplying conjugate binomials: Univariate
- ◇ Squaring a binomial: Univariate
- ◇ Squaring a binomial: Multivariate
- ◇ Multiplying binomials with negative coefficients
- ◇ Multiplication involving binomials and trinomials in one variable
- ◇ Multiplication involving binomials and trinomials in two variables
- ◆ Factoring Polynomials (16 topics)
  - ◇ Greatest common factor of 2 numbers
  - ◇ Factoring a linear binomial
  - ◇ Introduction to the GCF of two monomials
  - ◇ Greatest common factor of two multivariate monomials
  - ◇ Factoring out a monomial from a polynomial: Univariate
  - ◇ Factoring out a monomial from a polynomial: Multivariate
  - ◇ Factoring out a binomial from a polynomial: GCF factoring, basic
  - ◇ Factoring a univariate polynomial by grouping: Problem type 1
  - ◇ Factoring a quadratic with leading coefficient 1
  - ◇ Factoring out a constant before factoring a quadratic
  - ◇ Factoring a quadratic with leading coefficient greater than 1: Problem type 1
  - ◇ Factoring a quadratic with leading coefficient greater than 1: Problem type 2
  - ◇ Factoring a quadratic with a negative leading coefficient
  - ◇ Factoring a perfect square trinomial with leading coefficient 1
  - ◇ Factoring a difference of squares in one variable: Basic
  - ◇ Factoring a difference of squares in one variable: Advanced
- ◆ Rational Expressions (28 topics)
  - ◇ Restriction on a variable in a denominator: Linear
  - ◇ Simplifying a ratio of factored polynomials: Linear factors
  - ◇ Simplifying a ratio of polynomials using GCF factoring
  - ◇ Simplifying a ratio of polynomials by factoring a quadratic with leading coefficient 1
  - ◇ Simplifying a ratio of polynomials: Problem type 1
  - ◇ Multiplying rational expressions made up of linear expressions
  - ◇ Multiplying rational expressions involving quadratics with leading coefficients of 1
  - ◇ Dividing rational expressions involving linear expressions
  - ◇ Dividing rational expressions involving quadratics with leading coefficients of 1
  - ◇ Least common multiple of 2 numbers
  - ◇ Least common multiple of 3 numbers
  - ◇ Introduction to the LCM of two monomials
  - ◇ Finding the LCD of rational expressions with linear denominators: Relatively prime
  - ◇ Writing equivalent rational expressions with polynomial denominators
  - ◇ Introduction to adding fractions with variables and common denominators
  - ◇ Adding rational expressions with common denominators and monomial numerators
  - ◇ Adding rational expressions with common denominators and binomial numerators
  - ◇ Adding rational expressions with common denominators and GCF factoring
  - ◇ Adding rational expressions with common denominators and quadratic factoring
  - ◇ Adding rational expressions with different denominators and a single occurrence of a variable
  - ◇ Adding rational expressions with denominators  $ax$  and  $bx$ : Basic
  - ◇ Adding rational expressions with denominators  $ax$  and  $bx$ : Advanced
  - ◇ Adding rational expressions with linear denominators without common factors: Basic

- ◇ Complex fraction without variables: Problem type 1
- ◇ Complex fraction without variables: Problem type 2
- ◇ Complex fraction involving univariate monomials
- ◇ Complex fraction: GCF factoring
- ◇ Complex fraction made of sums involving rational expressions: Problem type 1
- ◆ Perfect Squares and nth Roots (7 topics)
  - ◇ Square root of a rational perfect square
  - ◇ Square roots of perfect squares with signs
  - ◇ Introduction to simplifying a radical expression with an even exponent
  - ◇ Square root of a perfect square monomial
  - ◇ Introduction to solving an absolute value equation
  - ◇ Cube root of an integer
  - ◇ Finding  $n^{\text{th}}$  roots of perfect  $n^{\text{th}}$  powers with signs
- ◆ Rational Exponents (4 topics)
  - ◇ Converting between radical form and exponent form
  - ◇ Rational exponents: Unit fraction exponents and whole number bases
  - ◇ Rational exponents: Non-unit fraction exponent with a whole number base
  - ◇ Rational exponents: Negative exponents and fractional bases
- ◆ Radical Expressions (19 topics)
  - ◇ Simplifying the square root of a whole number less than 100
  - ◇ Simplifying a radical expression with an even exponent
  - ◇ Introduction to simplifying a radical expression with an odd exponent
  - ◇ Simplifying a radical expression with an odd exponent
  - ◇ Simplifying a higher root of a whole number
  - ◇ Introduction to square root addition or subtraction
  - ◇ Square root addition or subtraction
  - ◇ Introduction to square root multiplication
  - ◇ Square root multiplication: Basic
  - ◇ Square root multiplication: Advanced
  - ◇ Introduction to simplifying a product of radical expressions: Univariate
  - ◇ Introduction to simplifying a product involving square roots using the distributive property
  - ◇ Simplifying a product involving square roots using the distributive property: Basic
  - ◇ Simplifying a product involving square roots using the distributive property: Advanced
  - ◇ Simplifying a quotient of square roots
  - ◇ Simplifying a quotient involving a sum or difference with a square root
  - ◇ Rationalizing a denominator: Quotient involving square roots
  - ◇ Rationalizing a denominator: Square root of a fraction
  - ◇ Rationalizing a denominator using conjugates: Integer numerator
- ◆ Geometry (4 topics)
  - ◇ Circumference of a circle
  - ◇ Volume of a rectangular prism
  - ◇ Introduction to the Pythagorean Theorem
  - ◇ Pythagorean Theorem
- Equations and Inequalities (83 topics)
  - ◆ Linear Equations and Applications (27 topics)
    - ◇ Additive property of equality with signed fractions
    - ◇ Multiplicative property of equality with signed fractions
    - ◇ Solving a multi-step equation given in fractional form
    - ◇ Solving a linear equation with several occurrences of the variable: Variables on the same side and distribution
    - ◇ Solving a linear equation with several occurrences of the variable: Variables on both sides and distribution

- ◇ Solving a linear equation with several occurrences of the variable: Variables on both sides and two distributions
- ◇ Solving a linear equation with several occurrences of the variable: Fractional forms with monomial numerators
- ◇ Solving a two–step equation with signed fractions
- ◇ Solving a linear equation with several occurrences of the variable: Variables on both sides and fractional coefficients
- ◇ Solving a linear equation with several occurrences of the variable: Fractional forms with binomial numerators
- ◇ Solving a proportion of the form  $(x+a)/b = c/d$
- ◇ Solving for a variable in terms of other variables using addition or subtraction: Basic
- ◇ Solving for a variable in terms of other variables using addition or subtraction: Advanced
- ◇ Solving for a variable in terms of other variables using multiplication or division: Basic
- ◇ Solving for a variable in terms of other variables using multiplication or division: Advanced
- ◇ Solving for a variable in terms of other variables using addition or subtraction with division
- ◇ Solving for a variable inside parentheses in terms of other variables
- ◇ Solving for a variable in terms of other variables in a linear equation with fractions
- ◇ Translating a sentence into a one–step equation
- ◇ Translating a sentence into a multi–step equation
- ◇ Solving a word problem with two unknowns using a linear equation
- ◇ Solving a decimal word problem using a linear equation of the form  $Ax + B = C$
- ◇ Solving a word problem with three unknowns using a linear equation
- ◇ Solving a one–step word problem using the formula  $d = rt$
- ◇ Solving a distance, rate, time problem using a linear equation
- ◇ Finding the perimeter or area of a rectangle given one of these values
- ◇ Finding the sale price given the original price and percent discount
- ◆ Absolute Value Equations (2 topics)
  - ◇ Solving an absolute value equation: Problem type 1
  - ◇ Solving an absolute value equation: Problem type 2
- ◆ Linear Inequalities and Applications (7 topics)
  - ◇ Graphing a linear inequality on the number line
  - ◇ Graphing a compound inequality on the number line
  - ◇ Set–builder and interval notation
  - ◇ Identifying solutions to a two–step linear inequality in one variable
  - ◇ Solving a two–step linear inequality: Problem type 1
  - ◇ Solving a two–step linear inequality: Problem type 2
  - ◇ Solving a linear inequality with multiple occurrences of the variable: Problem type 1
- ◆ Rational Equations that Simplify to Linear (8 topics)
  - ◇ Solving a rational equation that simplifies to linear: Denominator  $x$
  - ◇ Solving a rational equation that simplifies to linear: Denominator  $x+a$
  - ◇ Solving a rational equation that simplifies to linear: Denominators  $a$ ,  $x$ , or  $ax$
  - ◇ Solving a rational equation that simplifies to linear: Denominators  $ax$  and  $bx$
  - ◇ Solving a rational equation that simplifies to linear: Like binomial denominators
  - ◇ Solving a rational equation that simplifies to linear: Unlike binomial denominators
  - ◇ Solving for a variable in terms of other variables in a rational equation: Problem type 1
  - ◇ Solving for a variable in terms of other variables in a rational equation: Problem type 2
- ◆ Complex Numbers (4 topics)
  - ◇ Using  $i$  to rewrite square roots of negative numbers
  - ◇ Adding or subtracting complex numbers
  - ◇ Multiplying complex numbers
  - ◇ Dividing complex numbers
- ◆ Quadratic Equations (20 topics)
  - ◇ Solving an equation written in factored form

- ◇ Finding the roots of a quadratic equation of the form  $ax^2 + bx = 0$
- ◇ Finding the roots of a quadratic equation with leading coefficient 1
- ◇ Finding the roots of a quadratic equation with leading coefficient greater than 1
- ◇ Solving a quadratic equation needing simplification
- ◇ Roots of a product of polynomials
- ◇ Writing a quadratic equation given the roots and the leading coefficient
- ◇ Solving a word problem using a quadratic equation with rational roots
- ◇ Solving an equation of the form  $x^2 = a$  using the square root property
- ◇ Solving a quadratic equation using the square root property: Exact answers, basic
- ◇ Solving a quadratic equation using the square root property: Exact answers, advanced
- ◇ Completing the square
- ◇ Solving a quadratic equation by completing the square: Exact answers
- ◇ Applying the quadratic formula: Exact answers
- ◇ Applying the quadratic formula: Decimal answers
- ◇ Solving a quadratic equation with complex roots
- ◇ Discriminant of a quadratic equation
- ◇ Solving a word problem using a quadratic equation with irrational roots
- ◇ Solving an equation using the odd–root property: Problem type 1
- ◇ Solving an equation using the odd–root property: Problem type 2
- ◆ Rational Equations that Simplify to Quadratic (5 topics)
  - ◇ Restriction on a variable in a denominator: Quadratic
  - ◇ Solving a rational equation that simplifies to linear: Factorable quadratic denominator
  - ◇ Solving a rational equation that simplifies to quadratic: Denominator  $x$
  - ◇ Solving a rational equation that simplifies to quadratic: Binomial denominators, constant numerators
  - ◇ Solving a rational equation that simplifies to quadratic: Binomial denominators and numerators
- ◆ Radical Equations (10 topics)
  - ◇ Introduction to solving a radical equation
  - ◇ Solving a radical equation that simplifies to a linear equation: One radical, basic
  - ◇ Solving a radical equation that simplifies to a linear equation: One radical, advanced
  - ◇ Solving a radical equation that simplifies to a linear equation: Two radicals
  - ◇ Solving a radical equation that simplifies to a quadratic equation: One radical, basic
  - ◇ Solving a radical equation that simplifies to a quadratic equation: One radical, advanced
  - ◇ Algebraic symbol manipulation with radicals
  - ◇ Solving an equation with a root index greater than 2: Problem type 1
  - ◇ Solving an equation with a root index greater than 2: Problem type 2
  - ◇ Solving an equation that can be written in quadratic form: Problem type 1
- Graphs and Functions (138 topics)
  - ◆ The Coordinate Plane, Distance, and Midpoint (9 topics)
    - ◇ Reading a point in the coordinate plane
    - ◇ Plotting a point in the coordinate plane
    - ◇ Naming the quadrant or axis of a point given its coordinates
    - ◇ Naming the quadrant or axis of a point given the signs of its coordinates
    - ◇ Table for a linear equation
    - ◇ Distance between two points in the plane: Exact answers
    - ◇ Midpoint of a line segment in the plane
    - ◇ Identifying solutions to a linear equation in two variables
    - ◇ Finding a solution to a linear equation in two variables
  - ◆ Graphs of Equations (16 topics)
    - ◇ Graphing a linear equation of the form  $y = mx$
    - ◇ Graphing a line given its equation in slope–intercept form: Integer slope
    - ◇ Graphing a line given its equation in slope–intercept form: Fractional slope
    - ◇ Graphing a line given its equation in standard form
    - ◇ Graphing a vertical or horizontal line

- ◇ Finding x- and y-intercepts given the graph of a line on a grid
- ◇ Finding x- and y-intercepts of a line given the equation: Basic
- ◇ Finding x- and y-intercepts of a line given the equation: Advanced
- ◇ Graphing a line by first finding its x- and y-intercepts
- ◇ Finding intercepts of a nonlinear function given its graph
- ◇ Finding x- and y-intercepts of the graph of a nonlinear equation
- ◇ Graphing an absolute value equation of the form  $y = A|x|$
- ◇ Graphing a parabola of the form  $y = ax^2$
- ◇ Graphing a parabola of the form  $y = ax^2 + c$
- ◇ Graphing a cubic function of the form  $y = ax^3$
- ◇ Determining if graphs have symmetry with respect to the x-axis, y-axis, or origin
- ◆ Slope and Equations of Lines (17 topics)
  - ◇ Finding slope given the graph of a line on a grid
  - ◇ Finding slope given two points on the line
  - ◇ Finding the slope of horizontal and vertical lines
  - ◇ Graphing a line given its slope and y-intercept
  - ◇ Finding the slope and y-intercept of a line given its equation in the form  $y = mx + b$
  - ◇ Finding the slope and y-intercept of a line given its equation in the form  $Ax + By = C$
  - ◇ Graphing a line by first finding its slope and y-intercept
  - ◇ Writing an equation of a line given its slope and y-intercept
  - ◇ Writing an equation in slope-intercept form given the slope and a point
  - ◇ Finding the slope and a point on a line given its equation in point-slope form
  - ◇ Writing an equation in point-slope form given the slope and a point
  - ◇ Writing an equation of a line given the y-intercept and another point
  - ◇ Writing the equation of the line through two given points
  - ◇ Writing the equations of vertical and horizontal lines through a given point
  - ◇ Finding slopes of lines parallel and perpendicular to a line given in slope-intercept form
  - ◇ Finding slopes of lines parallel and perpendicular to a line given in the form  $Ax + By = C$
  - ◇ Writing equations of lines parallel and perpendicular to a given line through a point
- ◆ Linear Applications (5 topics)
  - ◇ Writing and evaluating a function that models a real-world situation: Advanced
  - ◇ Writing an equation and drawing its graph to model a real-world situation: Advanced
  - ◇ Finding the initial amount and rate of change given a graph of a linear function
  - ◇ Interpreting the parameters of a linear function that models a real-world situation
  - ◇ Application problem with a linear function: Finding a coordinate given two points
- ◆ Circles (6 topics)
  - ◇ Identifying the center and radius to graph a circle given its equation in standard form
  - ◇ Identifying the center and radius to graph a circle given its equation in general form: Basic
  - ◇ Writing the equation of a circle centered at the origin given its radius or a point on the circle
  - ◇ Writing an equation of a circle given its center and radius or diameter
  - ◇ Writing an equation of a circle given its center and a point on the circle
  - ◇ Writing an equation of a circle given the endpoints of a diameter
- ◆ Functions (26 topics)
  - ◇ Identifying functions from relations
  - ◇ Vertical line test
  - ◇ Table for a linear function
  - ◇ Evaluating functions: Linear and quadratic or cubic
  - ◇ Evaluating a rational function: Problem type 1
  - ◇ Evaluating a rational function: Problem type 2
  - ◇ Table for a square root function
  - ◇ Evaluating a cube root function
  - ◇ Evaluating functions: Absolute value, rational, radical
  - ◇ Evaluating a piecewise-defined function

- ◇ Variable expressions as inputs of functions: Problem type 1
- ◇ Variable expressions as inputs of functions: Problem type 2
- ◇ Variable expressions as inputs of functions: Problem type 3
- ◇ Domain and range from ordered pairs
- ◇ Domain of a rational function: Excluded values
- ◇ Domain of a rational function: Interval notation
- ◇ Domain of a square root function: Basic
- ◇ Domain of a square root function: Advanced
- ◇ Finding the domain of a fractional function involving radicals
- ◇ Determining whether an equation defines a function: Basic
- ◇ Determining whether an equation defines a function: Advanced
- ◇ Finding outputs of a one–step function that models a real–world situation: Function notation
- ◇ Finding outputs of a two–step function with decimals that models a real–world situation: Function notation
- ◇ Finding inputs and outputs of a two–step function that models a real–world situation: Function notation
- ◇ Finding a difference quotient for a linear or quadratic function
- ◇ Finding a difference quotient for a rational function
- ◆ Graphs of Functions (27 topics)
  - ◇ Finding an output of a function from its graph
  - ◇ Finding inputs and outputs of a function from its graph
  - ◇ Domain and range from the graph of a continuous function
  - ◇ Domain and range from the graph of a piecewise function
  - ◇ Finding where a function is increasing, decreasing, or constant given the graph
  - ◇ Finding where a function is increasing, decreasing, or constant given the graph: Interval notation
  - ◇ Finding local maxima and minima of a function given the graph
  - ◇ Finding the absolute maximum and minimum of a function given the graph
  - ◇ Finding values and intervals where the graph of a function is zero, positive, or negative
  - ◇ Graphing a function of the form  $f(x) = ax + b$ : Integer slope
  - ◇ Graphing a function of the form  $f(x) = ax + b$ : Fractional slope
  - ◇ Graphing an absolute value equation in the plane: Basic
  - ◇ Graphing an absolute value equation in the plane: Advanced
  - ◇ Graphing a function of the form  $f(x) = ax^2$
  - ◇ Graphing a function of the form  $f(x) = ax^2 + c$
  - ◇ Graphing a parabola of the form  $y = (x-h)^2 + k$
  - ◇ Graphing a square root function: Problem type 1
  - ◇ Graphing a square root function: Problem type 2
  - ◇ Matching parent graphs with their equations
  - ◇ Graphing a piecewise–defined function: Problem type 1
  - ◇ Graphing a piecewise–defined function: Problem type 2
  - ◇ Graphing a piecewise–defined function: Problem type 3
  - ◇ Even and odd functions: Problem type 1
  - ◇ Even and odd functions: Problem type 2
  - ◇ Finding the average rate of change of a function
  - ◇ Finding the average rate of change of a function given its graph
  - ◇ Word problem involving average rate of change
- ◆ Transformations (13 topics)
  - ◇ Translating the graph of a parabola: One step
  - ◇ Translating the graph of a parabola: Two steps
  - ◇ How the leading coefficient affects the shape of a parabola
  - ◇ Translating the graph of an absolute value function: One step
  - ◇ Translating the graph of an absolute value function: Two steps
  - ◇ Writing an equation for a function after a vertical translation

- ◇ Translating the graph of a function: One step
- ◇ Translating the graph of a function: Two steps
- ◇ Transforming the graph of a function by reflecting over an axis
- ◇ Transforming the graph of a function by shrinking or stretching
- ◇ Transforming the graph of a function using more than one transformation
- ◇ Transforming the graph of a quadratic, cubic, square root, or absolute value function
- ◇ Writing an equation for a function after a vertical and horizontal translation
- ◆ Combining Functions; Composite Functions; Inverse Functions (19 topics)
  - ◇ Sum, difference, and product of two functions
  - ◇ Quotient of two functions: Basic
  - ◇ Quotient of two functions: Advanced
  - ◇ Combining functions: Advanced
  - ◇ Introduction to the composition of two functions
  - ◇ Composition of two functions: Basic
  - ◇ Composition of a function with itself
  - ◇ Expressing a function as a composition of two functions
  - ◇ Composition of two functions: Advanced
  - ◇ Composition of two rational functions
  - ◇ Word problem involving composition of two functions
  - ◇ Horizontal line test
  - ◇ Determining whether two functions are inverses of each other
  - ◇ Inverse functions: Linear, discrete
  - ◇ Inverse functions: Quadratic, square root
  - ◇ Inverse functions: Cubic, cube root
  - ◇ Inverse functions: Rational
  - ◇ Graphing the inverse of a function given its graph
  - ◇ Finding, evaluating, and interpreting an inverse function for a given linear relationship
- Polynomial and Rational Functions (64 topics)
  - ◆ Quadratic Functions (16 topics)
    - ◇ Finding the vertex, intercepts, and axis of symmetry from the graph of a parabola
    - ◇ Graphing a parabola of the form  $y = x^2 + bx + c$
    - ◇ Graphing a parabola of the form  $y = a(x-h)^2 + k$
    - ◇ Graphing a parabola of the form  $y = ax^2 + bx + c$ : Integer coefficients
    - ◇ Finding the zeros of a quadratic function given its equation
    - ◇ Using a graphing calculator to find the zeros of a quadratic function
    - ◇ Writing a quadratic function given its zeros
    - ◇ Finding the x-intercept(s) and the vertex of a parabola
    - ◇ Using a graphing calculator to find the x-intercept(s) and vertex of a quadratic function
    - ◇ Rewriting a quadratic function to find its vertex and sketch its graph
    - ◇ Finding the maximum or minimum of a quadratic function
    - ◇ Word problem involving the maximum or minimum of a quadratic function
    - ◇ Word problem involving optimizing area by using a quadratic function
    - ◇ Domain and range from the graph of a quadratic function
    - ◇ Range of a quadratic function
    - ◇ Writing the equation of a quadratic function given its graph
  - ◆ Polynomial Functions (10 topics)
    - ◇ Finding zeros of a polynomial function written in factored form
    - ◇ Finding zeros and their multiplicities given a polynomial function written in factored form
    - ◇ Finding a polynomial of a given degree with given zeros: Real zeros
    - ◇ Finding x- and y-intercepts given a polynomial function
    - ◇ Determining the end behavior of the graph of a polynomial function
    - ◇ Determining end behavior and intercepts to graph a polynomial function
    - ◇ Matching graphs with polynomial functions



- ◇ Inferring properties of a polynomial function from its graph
- ◇ Using a graphing calculator to find local extrema of a polynomial function
- ◇ Using a graphing calculator to solve a word problem involving a local extremum of a polynomial function
- ◆ Division of Polynomials; Remainder and Factor Theorems (6 topics)
  - ◇ Polynomial long division: Problem type 1
  - ◇ Polynomial long division: Problem type 2
  - ◇ Polynomial long division: Problem type 3
  - ◇ Synthetic division
  - ◇ Using the remainder theorem to evaluate a polynomial
  - ◇ The Factor Theorem
- ◆ Real Zeros of Polynomial Functions (7 topics)
  - ◇ Using a given zero to write a polynomial as a product of linear factors: Real zeros
  - ◇ Finding all possible rational zeros using the rational zeros theorem: Problem type 1
  - ◇ Finding all possible rational zeros using the rational zeros theorem: Problem type 2
  - ◇ Using the rational zeros theorem to find all zeros of a polynomial: Rational zeros
  - ◇ Using the rational zeros theorem to find all zeros of a polynomial: Irrational zeros
  - ◇ Using a graphing calculator to find zeros of a polynomial function
  - ◇ Using a graphing calculator to solve a word problem involving a polynomial of degree 3
- ◆ Complex Zeros of Polynomials Functions (4 topics)
  - ◇ Multiplying expressions involving complex conjugates
  - ◇ Finding a polynomial of a given degree with given zeros: Complex zeros
  - ◇ Using a given zero to write a polynomial as a product of linear factors: Complex zeros
  - ◇ Using the rational zeros theorem to find all zeros of a polynomial: Complex zeros
- ◆ Rational Functions (13 topics)
  - ◇ Finding the intercepts, asymptotes, domain, and range from the graph of a rational function
  - ◇ Finding the asymptotes of a rational function: Constant over linear
  - ◇ Finding the asymptotes of a rational function: Linear over linear
  - ◇ Finding horizontal and vertical asymptotes of a rational function: Quadratic numerator or denominator
  - ◇ Finding the asymptotes of a rational function: Quadratic over linear
  - ◇ Graphing a rational function: Constant over linear
  - ◇ Graphing a rational function: Linear over linear
  - ◇ Transforming the graph of a rational function
  - ◇ Graphing a rational function: Quadratic over linear
  - ◇ Graphing rational functions with holes
  - ◇ Matching graphs with rational functions: Two vertical asymptotes
  - ◇ Graphing a rational function with more than one vertical asymptote
  - ◇ Using a graphing calculator to solve a word problem involving a local extremum of a rational function
- ◆ Polynomial and Rational Inequalities (8 topics)
  - ◇ Solving a quadratic inequality written in factored form
  - ◇ Solving a quadratic inequality
  - ◇ Solving a polynomial inequality: Problem type 1
  - ◇ Solving a polynomial inequality: Problem type 2
  - ◇ Solving a polynomial inequality: Problem type 3
  - ◇ Solving a polynomial inequality: Problem type 4
  - ◇ Solving a rational inequality: Problem type 1
  - ◇ Solving a rational inequality: Problem type 2
- Exponential and Logarithmic Functions (50 topics)
  - ◆ Graphing Exponential Functions (8 topics)
    - ◇ Table for an exponential function
    - ◇ Graphing an exponential function and its asymptote:  $f(x)=b^x$

- ◇ Graphing an exponential function and its asymptote:  $f(x) = a(b)^x$
- ◇ Graphing an exponential function and its asymptote:  $f(x) = b^{-x}$  or  $f(x) = -b^{ax}$
- ◇ Translating the graph of an exponential function
- ◇ The graph, domain, and range of an exponential function
- ◇ Transforming the graph of a natural exponential function
- ◇ Graphing an exponential function and its asymptote:  $f(x) = a(e)^{x-b} + c$
- ◆ Applications of Exponential Functions (7 topics)
  - ◇ Using a calculator to evaluate exponential expressions
  - ◇ Evaluating an exponential function that models a real-world situation
  - ◇ Using a calculator to evaluate exponential expressions involving base  $e$
  - ◇ Evaluating an exponential function with base  $e$  that models a real-world situation
  - ◇ Introduction to compound interest
  - ◇ Finding a final amount in a word problem on exponential growth or decay
  - ◇ Finding the final amount in a word problem on compound interest
- ◆ Logarithmic Functions (9 topics)
  - ◇ Using a calculator to evaluate natural and common logarithmic expressions
  - ◇ Converting between logarithmic and exponential equations
  - ◇ Converting between natural logarithmic and exponential equations
  - ◇ Evaluating logarithmic expressions
  - ◇ Solving an equation of the form  $\log_b a = c$
  - ◇ Translating the graph of a logarithmic function
  - ◇ Graphing a logarithmic function: Basic
  - ◇ The graph, domain, and range of a logarithmic function
  - ◇ Domain of a logarithmic function: Advanced
- ◆ Properties of Logarithms (6 topics)
  - ◇ Basic properties of logarithms
  - ◇ Using properties of logarithms to evaluate expressions
  - ◇ Expanding a logarithmic expression: Problem type 1
  - ◇ Expanding a logarithmic expression: Problem type 2
  - ◇ Writing an expression as a single logarithm
  - ◇ Change of base for logarithms: Problem type 1
- ◆ Logarithmic and Exponential Equations (10 topics)
  - ◇ Solving a multi-step equation involving a single logarithm: Problem type 1
  - ◇ Solving a multi-step equation involving a single logarithm: Problem type 2
  - ◇ Solving a multi-step equation involving natural logarithms
  - ◇ Solving an equation involving logarithms on both sides: Problem type 1
  - ◇ Solving an equation involving logarithms on both sides: Problem type 2
  - ◇ Solving an exponential equation by finding common bases: Linear exponents
  - ◇ Solving an exponential equation by using logarithms: Decimal answers, basic
  - ◇ Solving an exponential equation by using natural logarithms: Decimal answers
  - ◇ Solving an exponential equation by using logarithms: Decimal answers, advanced
  - ◇ Solving an exponential equation by using logarithms: Exact answers in logarithmic form
- ◆ Applications (10 topics)
  - ◇ Finding the time to reach a limit in a word problem on exponential growth or decay
  - ◇ Finding the time in a word problem on compound interest
  - ◇ Finding the time given an exponential function with base  $e$  that models a real-world situation
  - ◇ Finding the final amount in a word problem on continuous compound interest
  - ◇ Finding the initial amount in a word problem on continuous compound interest
  - ◇ Finding the final amount in a word problem on continuous exponential growth or decay
  - ◇ Finding the rate or time in a word problem on continuous exponential growth or decay
  - ◇ Finding half-life or doubling time
  - ◇ Writing and evaluating a function modeling continuous exponential growth or decay given doubling time or half-life

- ◇ Writing and evaluating a function modeling continuous exponential growth or decay given two outputs
- Trigonometric Functions (58 topics)
  - ◆ Angles and Their Measure (5 topics)
    - ◇ Converting between degree and radian measure: Problem type 1
    - ◇ Converting between degree and radian measure: Problem type 2
    - ◇ Sketching an angle in standard position
    - ◇ Coterminal angles
    - ◇ Arc length and central angle measure
  - ◆ The Unit Circle and Evaluating Trigonometric Functions (9 topics)
    - ◇ Finding coordinates on the unit circle for special angles
    - ◇ Trigonometric functions and special angles: Problem type 1
    - ◇ Finding trigonometric ratios from a point on the unit circle
    - ◇ Trigonometric functions and special angles: Problem type 2
    - ◇ Trigonometric functions and special angles: Problem type 3
    - ◇ Evaluating expressions involving sine and cosine
    - ◇ Even and odd properties of trigonometric functions
    - ◇ Using a calculator to approximate sine, cosine, and tangent values
    - ◇ Evaluating a sinusoidal function that models a real–world situation
  - ◆ Right Triangle Trigonometry (9 topics)
    - ◇ Sine, cosine, and tangent ratios: Variables for side lengths
    - ◇ Using the Pythagorean Theorem to find a trigonometric ratio
    - ◇ Finding trigonometric ratios given a right triangle
    - ◇ Using a trigonometric ratio to find a side length in a right triangle
    - ◇ Using trigonometry to find a length in a word problem with one right triangle
    - ◇ Using a trigonometric ratio to find an angle measure in a right triangle
    - ◇ Using trigonometry to find angles of elevation or depression in a word problem
    - ◇ Solving a right triangle
    - ◇ Using trigonometry to find a length in a word problem with two right triangles
  - ◆ Trigonometric Functions of Angles (7 topics)
    - ◇ Reference angles: Problem type 1
    - ◇ Reference angles: Problem type 2
    - ◇ Determining the location of a terminal point given the signs of trigonometric values
    - ◇ Finding values of trigonometric functions given information about an angle: Problem type 1
    - ◇ Finding values of trigonometric functions given information about an angle: Problem type 2
    - ◇ Finding values of trigonometric functions given information about an angle: Problem type 3
    - ◇ Finding values of trigonometric functions given information about an angle: Problem type 4
  - ◆ Graphs of Sine and Cosine Functions (14 topics)
    - ◇ Sketching the graph of  $y = a \sin(x)$  or  $y = a \cos(x)$
    - ◇ Sketching the graph of  $y = \sin(bx)$  or  $y = \cos(bx)$
    - ◇ Sketching the graph of  $y = \sin(x) + d$  or  $y = \cos(x) + d$
    - ◇ Sketching the graph of  $y = \sin(x+c)$  or  $y = \cos(x+c)$
    - ◇ Sketching the graph of  $y = a \sin(x+c)$  or  $y = a \cos(x+c)$
    - ◇ Sketching the graph of  $y = a \sin(bx)$  or  $y = a \cos(bx)$
    - ◇ Sketching the graph of  $y = a \sin(bx+c)$  or  $y = a \cos(bx+c)$
    - ◇ Sketching the graph of  $y = a \sin(bx) + d$  or  $y = a \cos(bx) + d$
    - ◇ Amplitude and period of sine and cosine functions
    - ◇ Amplitude, period, and phase shift of sine and cosine functions
    - ◇ Writing the equation of a sine or cosine function given its graph: Problem type 1
    - ◇ Writing the equation of a sine or cosine function given its graph: Problem type 2
    - ◇ Word problem involving a sine or cosine function: Problem type 1
    - ◇ Word problem involving a sine or cosine function: Problem type 2
  - ◆ Graphs of Other Trigonometric Functions (6 topics)

- ◇ Domains and ranges of trigonometric functions
- ◇ Matching graphs and equations for secant, cosecant, tangent, and cotangent functions
- ◇ Sketching the graph of a secant or cosecant function: Problem type 1
- ◇ Sketching the graph of a secant or cosecant function: Problem type 2
- ◇ Sketching the graph of a tangent or cotangent function: Problem type 1
- ◇ Sketching the graph of a tangent or cotangent function: Problem type 2
- ◆ Inverse Trigonometric Functions (8 topics)
  - ◇ Values of inverse trigonometric functions
  - ◇ Composition of a trigonometric function with its inverse trigonometric function: Problem type 1
  - ◇ Composition of a trigonometric function with its inverse trigonometric function: Problem type 2
  - ◇ Composition of a trigonometric function with the inverse of another trigonometric function: Problem type 1
  - ◇ Composition of a trigonometric function with the inverse of another trigonometric function: Problem type 2
  - ◇ Composition of a trigonometric function with the inverse of another trigonometric function: Problem type 3
  - ◇ Composition of trigonometric functions with variable expressions as inputs: Problem type 1
  - ◇ Using a calculator to approximate inverse trigonometric values
- Trigonometric Identities and Equations (32 topics)
  - ◆ Verifying Trigonometric Identities (6 topics)
    - ◇ Simplifying trigonometric expressions
    - ◇ Using cofunction identities
    - ◇ Verifying a trigonometric identity
    - ◇ Proving trigonometric identities: Problem type 1
    - ◇ Proving trigonometric identities: Problem type 2
    - ◇ Proving trigonometric identities: Problem type 3
  - ◆ Sum and Difference Formulas (6 topics)
    - ◇ Sum and difference identities: Problem type 1
    - ◇ Sum and difference identities: Problem type 2
    - ◇ Sum and difference identities: Problem type 3
    - ◇ Sum and difference identities: Problem type 4
    - ◇ Proving trigonometric identities using sum and difference properties: Problem type 1
    - ◇ Proving trigonometric identities using sum and difference properties: Problem type 2
  - ◆ Double–Angle, Half–Angle, Product–to–Sum, and Power Reducing Formulas (8 topics)
    - ◇ Double–angle identities: Problem type 1
    - ◇ Double–angle identities: Problem type 2
    - ◇ Power–reducing identities
    - ◇ Half–angle identities: Problem type 1
    - ◇ Half–angle identities: Problem type 2
    - ◇ Product–to–sum and sum–to–product identities: Problem type 1
    - ◇ Product–to–sum and sum–to–product identities: Problem type 2
    - ◇ Proving trigonometric identities using double–angle properties
  - ◆ Trigonometric Equations (12 topics)
    - ◇ Finding solutions in an interval for a basic equation involving sine or cosine
    - ◇ Finding solutions in an interval for a basic tangent, cotangent, secant, or cosecant equation
    - ◇ Solving a basic trigonometric equation using a calculator
    - ◇ Solving a basic trigonometric equation involving sine or cosine
    - ◇ Solving a basic trigonometric equation involving tangent, cotangent, secant, or cosecant
    - ◇ Finding solutions in an interval for a trigonometric equation in factored form
    - ◇ Finding solutions in an interval for a trigonometric equation with a squared function: Problem type 1
    - ◇ Finding solutions in an interval for a trigonometric equation with a squared function: Problem type 2
    - ◇ Finding solutions in an interval for a trigonometric equation using Pythagorean identities: Problem type 1

- ◇ Finding solutions in an interval for an equation with sine and cosine using double–angle identities
- ◇ Solving a trigonometric equation modeling a real–world situation
- ◇ Finding solutions in an interval for a trigonometric equation with an angle multiplied by a constant
- Additional Topics in Trigonometry (5 topics)
  - ◆ Laws of Sines and Cosines (5 topics)
    - ◇ Solving a triangle with the law of sines: Problem type 1
    - ◇ Solving a triangle with the law of sines: Problem type 2
    - ◇ Solving a word problem using the law of sines
    - ◇ Solving a triangle with the law of cosines
    - ◇ Solving a word problem using the law of cosines
- Other Topics Available(\*) (614 additional topics)
  - ◆ Algebra and Geometry Review (160 topics)
    - ◇ Fractional position on a number line
    - ◇ Plotting rational numbers on a number line
    - ◇ Ordering integers
    - ◇ Estimating a square root
    - ◇ Ordering real numbers
    - ◇ Identifying numbers as integers or non–integers
    - ◇ Identifying numbers as rational or irrational
    - ◇ Signed fraction addition or subtraction: Advanced
    - ◇ Addition and subtraction of 3 fractions involving signs
    - ◇ Signed fraction multiplication: Advanced
    - ◇ Operations with absolute value: Problem type 2
    - ◇ Exponents and integers: Problem type 2
    - ◇ Order of operations with integers and exponents
    - ◇ Converting between temperatures in Fahrenheit and Celsius
    - ◇ Properties of addition
    - ◇ Properties of real numbers
    - ◇ Identifying properties used to simplify an algebraic expression
    - ◇ Understanding the product rule of exponents
    - ◇ Ordering numbers with positive exponents
    - ◇ Understanding the power rules of exponents
    - ◇ Power and product rules with positive exponents
    - ◇ Simplifying a ratio of multivariate monomials: Advanced
    - ◇ Power and quotient rules with positive exponents
    - ◇ Ordering numbers with negative exponents
    - ◇ Product rule with negative exponents
    - ◇ Quotient rule with negative exponents: Problem type 2
    - ◇ Power and quotient rules with negative exponents: Problem type 1
    - ◇ Power and quotient rules with negative exponents: Problem type 2
    - ◇ Power, product, and quotient rules with negative exponents
    - ◇ Scientific notation with positive exponent
    - ◇ Scientific notation with negative exponent
    - ◇ Converting between scientific notation and standard form in a real–world situation
    - ◇ Multiplying numbers written in scientific notation: Basic
    - ◇ Multiplying numbers written in scientific notation: Advanced
    - ◇ Multiplying numbers written in decimal form or scientific notation in a real–world situation
    - ◇ Dividing numbers written in scientific notation: Basic
    - ◇ Dividing numbers written in scientific notation: Advanced
    - ◇ Finding the scale factor between numbers given in scientific notation in a real–world situation
    - ◇ Degree of a multivariate polynomial

- ◇ Simplifying a sum or difference of three univariate polynomials
- ◇ Simplifying a sum or difference of multivariate polynomials
- ◇ Multiplying conjugate binomials: Multivariate
- ◇ Prime numbers
- ◇ Prime factorization
- ◇ Greatest common factor of three univariate monomials
- ◇ Factoring a univariate polynomial by grouping: Problem type 2
- ◇ Factoring a multivariate polynomial by grouping: Problem type 1
- ◇ Factoring a multivariate polynomial by grouping: Problem type 2
- ◇ Factoring a quadratic in two variables with leading coefficient 1
- ◇ Factoring a quadratic with leading coefficient greater than 1: Problem type 3
- ◇ Factoring a quadratic by the ac–method
- ◇ Factoring a quadratic in two variables with leading coefficient greater than 1
- ◇ Factoring a perfect square trinomial with leading coefficient greater than 1
- ◇ Factoring a perfect square trinomial in two variables
- ◇ Factoring a difference of squares in two variables
- ◇ Factoring a polynomial involving a GCF and a difference of squares: Univariate
- ◇ Factoring a polynomial involving a GCF and a difference of squares: Multivariate
- ◇ Factoring a product of a quadratic trinomial and a monomial
- ◇ Factoring with repeated use of the difference of squares formula
- ◇ Factoring a sum or difference of two cubes
- ◇ Factoring out binomials from a polynomial: GCF factoring, advanced
- ◇ Using substitution to factor polynomials
- ◇ Simplifying a ratio of factored polynomials: Factors with exponents
- ◇ Simplifying a ratio of linear polynomials: 1,  $-1$ , and no simplification
- ◇ Simplifying a ratio of polynomials: Problem type 2
- ◇ Simplifying a ratio of polynomials: Problem type 3
- ◇ Simplifying a ratio of multivariate polynomials
- ◇ Multiplying rational expressions involving multivariate monomials
- ◇ Multiplying rational expressions involving quadratics with leading coefficients greater than 1
- ◇ Multiplying rational expressions involving multivariate quadratics
- ◇ Dividing rational expressions involving multivariate monomials
- ◇ Dividing rational expressions involving quadratics with leading coefficients greater than 1
- ◇ Dividing rational expressions involving multivariate quadratics
- ◇ Multiplication and division of 3 rational expressions
- ◇ Least common multiple of two monomials
- ◇ Finding the LCD of rational expressions with linear denominators: Common factors
- ◇ Finding the LCD of rational expressions with quadratic denominators
- ◇ Writing equivalent rational expressions with monomial denominators
- ◇ Writing equivalent rational expressions involving opposite factors
- ◇ Adding rational expressions with denominators  $ax^n$  and  $bx^m$
- ◇ Adding rational expressions with multivariate monomial denominators: Basic
- ◇ Adding rational expressions with multivariate monomial denominators: Advanced
- ◇ Adding rational expressions with linear denominators without common factors: Advanced
- ◇ Adding rational expressions with linear denominators with common factors: Basic
- ◇ Adding rational expressions with linear denominators with common factors: Advanced
- ◇ Adding rational expressions with denominators  $ax-b$  and  $b-ax$
- ◇ Adding rational expressions involving different quadratic denominators
- ◇ Adding 3 rational expressions with different quadratic denominators
- ◇ Complex fraction involving multivariate monomials
- ◇ Complex fraction: Quadratic factoring
- ◇ Complex fraction made of sums involving rational expressions: Problem type 2
- ◇ Complex fraction made of sums involving rational expressions: Problem type 3

- ◇ Complex fraction made of sums involving rational expressions: Problem type 4
- ◇ Complex fraction made of sums involving rational expressions: Problem type 5
- ◇ Complex fraction made of sums involving rational expressions: Problem type 6
- ◇ Complex fraction made of sums involving rational expressions: Multivariate
- ◇ Complex fraction with negative exponents: Problem type 1
- ◇ Complex fraction with negative exponents: Problem type 2
- ◇ Complex fraction that contains a complex fraction
- ◇ Finding all square roots of a number
- ◇ Square roots of integers raised to even exponents
- ◇ Using absolute value to simplify square roots of perfect square monomials
- ◇ Finding the  $n^{\text{th}}$  root of a perfect  $n^{\text{th}}$  power fraction
- ◇ Finding the  $n^{\text{th}}$  root of a perfect  $n^{\text{th}}$  power monomial
- ◇ Using absolute value to simplify higher radical expressions
- ◇ Rational exponents: Unit fraction exponents and bases involving signs
- ◇ Rational exponents: Product rule
- ◇ Rational exponents: Quotient rule
- ◇ Rational exponents: Products and quotients with negative exponents
- ◇ Rational exponents: Power of a power rule
- ◇ Rational exponents: Powers of powers with negative exponents
- ◇ Simplifying the square root of a whole number greater than 100
- ◇ Simplifying a radical expression with two variables
- ◇ Introduction to simplifying a higher radical expression
- ◇ Simplifying a higher radical expression: Univariate
- ◇ Simplifying a higher radical expression: Multivariate
- ◇ Square root addition or subtraction with three terms
- ◇ Introduction to simplifying a sum or difference of radical expressions: Univariate
- ◇ Simplifying a sum or difference of radical expressions: Univariate
- ◇ Simplifying a sum or difference of radical expressions: Multivariate
- ◇ Simplifying a sum or difference of higher roots
- ◇ Simplifying a sum or difference of higher radical expressions
- ◇ Simplifying a product of radical expressions: Univariate
- ◇ Simplifying a product of radical expressions: Multivariate
- ◇ Simplifying a product of radical expressions: Multivariate, fractional expressions
- ◇ Introduction to simplifying a product of higher roots
- ◇ Simplifying a product of higher radical expressions
- ◇ Special products of radical expressions: Conjugates and squaring
- ◇ Classifying sums and products as rational or irrational
- ◇ Rationalizing a denominator: Quotient involving a monomial
- ◇ Rationalizing a denominator using conjugates: Square root in numerator
- ◇ Rationalizing a denominator using conjugates: Variable in denominator
- ◇ Rationalizing a denominator: Quotient involving a higher radical
- ◇ Rationalizing a denominator: Quotient involving higher radicals and monomials
- ◇ Simplifying products or quotients of higher radicals with different indices: Univariate
- ◇ Simplifying products or quotients of higher radicals with different indices: Multivariate
- ◇ Area of a piecewise rectangular figure
- ◇ Word problem involving the area between two rectangles
- ◇ Area of a triangle
- ◇ Area of a parallelogram
- ◇ Area of a trapezoid
- ◇ Perimeter involving rectangles and circles
- ◇ Circumference and area of a circle
- ◇ Circumference and area of a circle: Exact answers in terms of pi
- ◇ Area involving rectangles and circles

- ◇ Word problem involving the area between two concentric circles
- ◇ Area involving inscribed figures
- ◇ Volume of a triangular prism
- ◇ Volume of a pyramid
- ◇ Volume of a cylinder
- ◇ Word problem involving the rate of filling or emptying a cylinder
- ◇ Volume of a cone
- ◇ Volume of a cone: Exact answers in terms of pi
- ◇ Volume of a sphere
- ◇ Surface area of a cube or a rectangular prism
- ◇ Surface area of a triangular prism
- ◇ Surface area of a cylinder
- ◇ Surface area of a cylinder: Exact answers in terms of pi
- ◇ Surface area of a sphere
- ◇ Word problem involving the Pythagorean Theorem
- ◆ Equations and Inequalities (76 topics)
  - ◇ Identifying properties used to solve a linear equation
  - ◇ Solving equations with zero, one, or infinitely many solutions
  - ◇ Solving a decimal word problem using a linear equation with the variable on both sides
  - ◇ Solving a fraction word problem using a linear equation with the variable on both sides
  - ◇ Solving a word problem involving consecutive integers
  - ◇ Writing a multi-step equation for a real-world situation
  - ◇ Solving a value mixture problem using a linear equation
  - ◇ Finding a side length given the perimeter and side lengths with variables
  - ◇ Circumference ratios
  - ◇ Solving equations involving vertical angles
  - ◇ Finding angle measures of a triangle given angles with variables
  - ◇ Finding the value for a new score that will yield a given mean
  - ◇ Finding the multiplier to give a final amount after a percentage increase or decrease
  - ◇ Finding the total cost including tax or markup
  - ◇ Finding the original price given the sale price and percent discount
  - ◇ Computing a percent mixture
  - ◇ Solving a percent mixture problem using a linear equation
  - ◇ Finding simple interest without a calculator
  - ◇ Converting a repeating decimal to a fraction
  - ◇ Solving an absolute value equation: Problem type 3
  - ◇ Solving an absolute value equation: Problem type 4
  - ◇ Solving an absolute value equation of the form  $|ax+b| = |cx+d|$
  - ◇ Translating a sentence into a one-step inequality
  - ◇ Translating a sentence into a multi-step inequality
  - ◇ Writing an inequality for a real-world situation
  - ◇ Writing an inequality given a graph on the number line
  - ◇ Translating a sentence into a compound inequality
  - ◇ Writing a compound inequality given a graph on the number line
  - ◇ Set-builder notation
  - ◇ Union and intersection of finite sets
  - ◇ Union and intersection of intervals
  - ◇ Additive property of inequality with signed fractions
  - ◇ Multiplicative property of inequality with signed fractions
  - ◇ Solving a two-step linear inequality with a fractional coefficient
  - ◇ Solving a linear inequality with multiple occurrences of the variable: Problem type 2
  - ◇ Solving a linear inequality with multiple occurrences of the variable: Problem type 3
  - ◇ Solving inequalities with no solution or all real numbers as solutions



- ◇ Solving a compound linear inequality: Graph solution, basic
- ◇ Solving a compound linear inequality: Interval notation
- ◇ Solving a decimal word problem using a two–step linear inequality
- ◇ Solving a decimal word problem using a linear inequality with the variable on both sides
- ◇ Solving an absolute value inequality: Problem type 1
- ◇ Writing an absolute value inequality given a graph on the number line
- ◇ Solving an absolute value inequality: Problem type 2
- ◇ Solving an absolute value inequality: Problem type 3
- ◇ Solving an absolute value inequality: Problem type 4
- ◇ Solving an absolute value inequality: Problem type 5
- ◇ Solving a proportion of the form  $a/(x+b) = c/x$
- ◇ Solving for a variable in terms of other variables in a rational equation: Problem type 3
- ◇ Word problem on proportions: Problem type 1
- ◇ Word problem on proportions: Problem type 2
- ◇ Similar polygons
- ◇ Similar right triangles
- ◇ Indirect measurement
- ◇ Ratio of volumes
- ◇ Word problem involving multiple rates
- ◇ Solving a work problem using a rational equation
- ◇ Solving a distance, rate, time problem using a rational equation
- ◇ Ordering fractions with variables
- ◇ Simplifying a product and quotient involving square roots of negative numbers
- ◇ Simplifying a power of  $i$
- ◇ Using the Pythagorean Theorem and a quadratic equation to find side lengths of a right triangle
- ◇ Discriminant of a quadratic equation with parameter
- ◇ Solving a rational equation that simplifies to quadratic: Proportional form, basic
- ◇ Solving a rational equation that simplifies to quadratic: Factorable quadratic denominator
- ◇ Solving a rational equation that simplifies to quadratic: Proportional form, advanced
- ◇ Solving a radical equation with a quadratic expression under the radical
- ◇ Solving a radical equation with two radicals that simplifies to  $\sqrt{x} = a$
- ◇ Solving a radical equation that simplifies to a quadratic equation: Two radicals
- ◇ Word problem involving radical equations: Basic
- ◇ Word problem involving radical equations: Advanced
- ◇ Solving an equation with exponent  $1/a$ : Problem type 1
- ◇ Solving an equation with exponent  $1/a$ : Problem type 2
- ◇ Solving an equation with positive rational exponent
- ◇ Solving an equation with negative rational exponent
- ◇ Solving an equation that can be written in quadratic form: Problem type 2
- ◆ Graphs and Functions (61 topics)
  - ◇ Finding the area of a triangle or parallelogram in the coordinate plane
  - ◇ Distance between two points in the plane: Decimal answers
  - ◇ Identifying scalene, isosceles, and equilateral triangles given coordinates of their vertices
  - ◇ Finding an endpoint of a line segment given the other endpoint and the midpoint
  - ◇ Graphing a line given its  $x$ - and  $y$ -intercepts
  - ◇ Testing an equation for symmetry about the axes and origin
  - ◇ Classifying slopes given graphs of lines
  - ◇ Finding the coordinate that yields a given slope
  - ◇ Graphing a line through a given point with a given slope
  - ◇ Identifying linear equations: Advanced
  - ◇ Identifying linear functions given ordered pairs
  - ◇ Rewriting a linear equation in the form  $Ax + By = C$
  - ◇ Writing an equation and graphing a line given its slope and  $y$ -intercept

- ◇ Finding the slope, y–intercept, and equation for a linear function given a table of values
- ◇ Graphing a line given its equation in point–slope form
- ◇ Writing an equation in standard form given the slope and a point
- ◇ Comparing linear functions to the parent function  $y=x$
- ◇ Identifying parallel and perpendicular lines from equations
- ◇ Identifying parallel and perpendicular lines from coordinates
- ◇ Identifying coordinates that give right triangles
- ◇ Graphing ordered pairs and writing an equation from a table of values in context
- ◇ Finding the initial amount and rate of change given a table for a linear function
- ◇ Combining functions to write a new function that models a real–world situation
- ◇ Comparing properties of linear functions given in different forms
- ◇ Application problem with a linear function: Finding a coordinate given the slope and a point
- ◇ Solving a linear equation by graphing
- ◇ Constructing a scatter plot
- ◇ Sketching the line of best fit
- ◇ Scatter plots and correlation
- ◇ Predictions from the line of best fit
- ◇ Approximating the equation of a line of best fit and making predictions
- ◇ Computing residuals
- ◇ Interpreting residual plots
- ◇ Classifying linear and nonlinear relationships from scatter plots
- ◇ Linear relationship and the correlation coefficient
- ◇ Identifying outliers and clustering in scatter plots
- ◇ Finding outliers in a data set
- ◇ Identifying solutions to a system of linear equations
- ◇ Graphically solving a system of linear equations
- ◇ Using a graphing calculator to solve a system of linear equations: Basic
- ◇ Using a graphing calculator to solve a system of linear equations: Advanced
- ◇ Writing a system of linear equations given its graph
- ◇ Solving a system of linear equations using substitution
- ◇ Solving a system of linear equations using elimination with addition
- ◇ Solving a system of linear equations using elimination with multiplication and addition
- ◇ Identifying the center and radius to graph a circle given its equation in general form: Advanced
- ◇ Writing an equation of a circle and identifying points that lie on the circle
- ◇ Deriving the equation of a circle using the Pythagorean Theorem
- ◇ Domains of higher root functions
- ◇ Domain and range of a linear function that models a real–world situation
- ◇ Rewriting a multivariate function as a univariate function given a relationship between its variables
- ◇ Domain and range from the graph of a discrete relation
- ◇ Finding domain and range from a linear graph in context
- ◇ Choosing a graph to fit a narrative: Basic
- ◇ Choosing a graph to fit a narrative: Advanced
- ◇ Graphing an integer function and finding its range for a given domain
- ◇ Graphing a square root function: Problem type 3
- ◇ Graphing a cube root function
- ◇ Writing the equation of a secant line
- ◇ How the leading coefficient affects the graph of an absolute value function
- ◇ Composition of two functions: Domain and range
- ◆ Polynomial and Rational Functions (27 topics)
  - ◇ Graphing a parabola of the form  $y = ax^2 + bx + c$ : Rational coefficients
  - ◇ Rewriting a quadratic function in standard form
  - ◇ Solving a quadratic equation by graphing
  - ◇ Comparing properties of quadratic functions given in different forms

- ◇ Classifying the graph of a function
- ◇ Choosing a quadratic model and using it to make a prediction
- ◇ Identifying polynomial functions
- ◇ Dividing a polynomial by a monomial: Univariate
- ◇ Dividing a polynomial by a monomial: Multivariate
- ◇ Remainder theorem: Advanced
- ◇ Closure properties of integers and polynomials
- ◇ Descartes' Rule of Signs
- ◇ Using the conjugate zeros theorem to find all zeros of a polynomial
- ◇ Linear factors theorem and conjugate zeros theorem
- ◇ Writing the equation of a rational function given its graph
- ◇ Identifying direct variation equations
- ◇ Identifying direct variation from ordered pairs and writing equations
- ◇ Writing a direct variation equation
- ◇ Word problem on direct variation
- ◇ Interpreting direct variation from a graph
- ◇ Writing an inverse variation equation
- ◇ Identifying direct and inverse variation equations
- ◇ Identifying direct and inverse variation from ordered pairs and writing equations
- ◇ Word problem on inverse variation
- ◇ Word problem on inverse proportions
- ◇ Writing an equation that models variation
- ◇ Word problem on combined variation
- ◆ Exponential and Logarithmic Functions (12 topics)
  - ◇ Finding domain and range from the graph of an exponential function
  - ◇ Calculating and comparing simple interest and compound interest
  - ◇ Finding the initial amount and rate of change given an exponential function
  - ◇ Writing an equation that models exponential growth or decay
  - ◇ Writing an exponential function rule given a table of ordered pairs
  - ◇ Choosing an exponential model and using it to make a prediction
  - ◇ Comparing linear, polynomial, and exponential functions
  - ◇ Graphing a logarithmic function: Advanced
  - ◇ Expanding a logarithmic expression: Problem type 3
  - ◇ Change of base for logarithms: Problem type 2
  - ◇ Solving an exponential equation by finding common bases: Linear and quadratic exponents
  - ◇ Solving an exponential equation by using substitution and quadratic factoring
- ◆ Trigonometric Functions (13 topics)
  - ◇ Converting degrees–minutes–seconds to decimal degrees
  - ◇ Converting a decimal degree to degrees–minutes–seconds
  - ◇ Area of a sector of a circle
  - ◇ Angular and linear speed
  - ◇ Finding a point on the unit circle given one coordinate
  - ◇ Using a calculator to approximate cosecant, secant, and cotangent values
  - ◇ Special right triangles: Exact answers
  - ◇ Sine, cosine, and tangent ratios: Numbers for side lengths
  - ◇ Understanding trigonometric ratios through similar right triangles
  - ◇ Relationship between the sines and cosines of complementary angles
  - ◇ Using similar right triangles to find trigonometric ratios
  - ◇ Sketching a graph of a damped sine or cosine function
  - ◇ Composition of trigonometric functions with variable expressions as inputs: Problem type 2
- ◆ Trigonometric Identities and Equations (15 topics)
  - ◇ Proving trigonometric identities: Problem type 4
  - ◇ Proving trigonometric identities using odd and even properties

- ◇ Double–angle identities: Problem type 3
- ◇ Proving trigonometric identities using sum–to–product formulas
- ◇ Finding solutions in an interval for a trigonometric equation using Pythagorean identities: Problem type 2
- ◇ Using a graphing calculator to solve a trigonometric equation
- ◇ Using a graphing calculator to solve a trigonometric inequality
- ◇ Solving a trigonometric equation involving a squared function: Problem type 1
- ◇ Solving a trigonometric equation involving a squared function: Problem type 2
- ◇ Solving a trigonometric equation involving more than one function
- ◇ Solving a trigonometric equation involving an angle multiplied by a constant
- ◇ Finding solutions in an interval for an equation with sine and cosine using sum and difference identities
- ◇ Solving a trigonometric equation using sum and difference identities
- ◇ Solving a trigonometric equation using double–angle identities
- ◇ Solving a trigonometric equation using half–angle identities
- ◆ Additional Topics in Trigonometry (60 topics)
  - ◇ Proving the law of sines
  - ◇ Proving the law of cosines
  - ◇ Using trigonometry to find the area of a right triangle
  - ◇ Finding the area of a triangle using trigonometry
  - ◇ Expressing the area of a triangle in terms of the sine of one of its angles
  - ◇ Heron's formula
  - ◇ Writing a position vector in  $ai+bj$  form given its graph
  - ◇ Writing a vector in  $ai+bj$  form given its initial and terminal points
  - ◇ Writing a vector in component form given its initial and terminal points
  - ◇ Magnitude of a vector given in  $ai+bj$  form
  - ◇ Magnitude of a vector given in component form
  - ◇ Vector addition and scalar multiplication:  $ai+bj$  form
  - ◇ Linear combination of vectors:  $ai+bj$  form
  - ◇ Vector addition and scalar multiplication: Component form
  - ◇ Linear combination of vectors: Component form
  - ◇ Unit vectors
  - ◇ Multiplication of a vector by a scalar: Geometric approach
  - ◇ Vector addition: Geometric approach
  - ◇ Vector subtraction: Geometric approach
  - ◇ Finding the magnitude and direction of a vector given its graph
  - ◇ Finding the components of a vector given its graph
  - ◇ Finding the direction angle of a vector given in  $ai+bj$  form
  - ◇ Writing a vector given its magnitude and direction angle
  - ◇ Writing a vector to represent a force pushing or pulling an object
  - ◇ Finding the magnitude and direction angle of the resultant force of two vectors
  - ◇ Finding magnitudes of forces related to a sum of three vectors
  - ◇ Finding magnitudes of forces related to an object suspended by cables
  - ◇ Dot product of vectors given in  $ai+bj$  form
  - ◇ Dot product of vectors given in component form
  - ◇ Finding the angle between two vectors given in component form
  - ◇ Classifying vector relationships by finding the angle between two vectors given in  $ai + bj$  form
  - ◇ Using the dot product to find perpendicular vectors
  - ◇ Finding the component of a vector along another vector
  - ◇ Decomposing a vector into two orthogonal vectors
  - ◇ Finding the amount of work done given a force vector and a distance
  - ◇ Finding magnitudes of forces related to an object on a ramp
  - ◇ Plotting points in polar coordinates

- ◇ Multiple representations of polar coordinates
- ◇ Converting rectangular coordinates to polar coordinates: Special angles
- ◇ Converting rectangular coordinates to polar coordinates: Decimal answers
- ◇ Converting polar coordinates to rectangular coordinates
- ◇ Converting an equation written in rectangular form to one written in polar form
- ◇ Converting an equation written in polar form to one written in rectangular form: Problem type 1
- ◇ Converting an equation written in polar form to one written in rectangular form: Problem type 2
- ◇ Graphing a polar equation: Basic
- ◇ Graphing a polar equation: Circle
- ◇ Graphing a polar equation: Limacon
- ◇ Graphing a polar equation: Rose
- ◇ Graphing a polar equation: Lemniscate
- ◇ Matching polar equations with their graphs
- ◇ Identifying symmetries of graphs given their polar equations
- ◇ Plotting complex numbers
- ◇ Writing a complex number in standard form given its trigonometric form
- ◇ Writing a complex number in trigonometric form: Special angles
- ◇ Writing a complex number in trigonometric form: Decimal answers
- ◇ Multiplying and dividing complex numbers in trigonometric form
- ◇ De Moivre's Theorem: Answers in trigonometric form
- ◇ De Moivre's Theorem: Answers in standard form
- ◇ Finding the  $n$ th roots of a number: Problem type 1
- ◇ Finding the  $n$ th roots of a number: Problem type 2
- ◆ Systems of Equations and Matrices (72 topics)
  - ◇ Classifying systems of linear equations from graphs
  - ◇ Solving a system of linear equations with fractional coefficients
  - ◇ Solving a system of linear equations with decimal coefficients
  - ◇ Solving a  $2 \times 2$  system of linear equations that is inconsistent or consistent dependent
  - ◇ Creating an inconsistent system of linear equations
  - ◇ Identifying the operations used to create equivalent systems of equations
  - ◇ Consistency and independence of a system of linear equations
  - ◇ Interpreting the graphs of two functions
  - ◇ Solving a word problem involving a sum and another basic relationship using a system of linear equations
  - ◇ Solving a word problem using a system of linear equations of the form  $Ax + By = C$
  - ◇ Solving a word problem using a system of linear equations of the form  $y = mx + b$
  - ◇ Solving a value mixture problem using a system of linear equations
  - ◇ Solving a percent mixture problem using a system of linear equations
  - ◇ Solving a distance, rate, time problem using a system of linear equations
  - ◇ Solving a tax rate or interest rate problem using a system of linear equations
  - ◇ Introduction to solving a  $3 \times 3$  system of linear equations
  - ◇ Solving a  $3 \times 3$  system of linear equations: Problem type 1
  - ◇ Solving a  $3 \times 3$  system of linear equations: Problem type 2
  - ◇ Solving a  $3 \times 3$  system of linear equations that is inconsistent or consistent dependent
  - ◇ Solving a word problem using a  $3 \times 3$  system of linear equations: Problem type 1
  - ◇ Solving a word problem using a  $3 \times 3$  system of linear equations: Problem type 2
  - ◇ Scalar multiplication of a matrix
  - ◇ Addition or subtraction of matrices
  - ◇ Linear combination of matrices
  - ◇ Squaring and multiplying  $2 \times 2$  matrices
  - ◇ Multiplication of matrices: Basic
  - ◇ Multiplication of matrices: Advanced
  - ◇ Word problem involving multiplication of matrices

- ◇ Finding the inverse of a 2x2 matrix
- ◇ Finding the inverse of a 3x3 matrix
- ◇ Finding the determinant of a 2x2 matrix
- ◇ Finding the determinant of a 3x3 matrix
- ◇ Completing Gauss–Jordan elimination with a 2x2 matrix
- ◇ Gauss–Jordan elimination with a 2x2 matrix
- ◇ Writing solutions to 3x3 systems of linear equations from augmented matrices
- ◇ Completing Gauss–Jordan elimination with a 3x3 matrix
- ◇ Solving a system of linear equations given its augmented matrix
- ◇ Finding the inverse of a matrix to solve a 2x2 system of linear equations
- ◇ Using the inverse of a matrix to solve a 3x3 system of linear equations
- ◇ Using Cramer's rule to solve a 2x2 system of linear equations
- ◇ Using Cramer's rule to solve a 3x3 system of linear equations
- ◇ Introduction to partial fraction decomposition with distinct linear factors
- ◇ Partial fraction decomposition with distinct linear factors
- ◇ Partial fraction decomposition with repeated linear factors
- ◇ Partial fraction decomposition with an irreducible quadratic factor
- ◇ Partial fraction decomposition with repeated, irreducible quadratic factors
- ◇ Graphically solving a system of linear and quadratic equations
- ◇ Using a graphing calculator to solve a system of linear and quadratic equations: Basic
- ◇ Using a graphing calculator to solve a system of equations
- ◇ Using a graphing calculator to solve an exponential or logarithmic equation
- ◇ Solving a system of linear and quadratic equations
- ◇ Solving a system of nonlinear equations: Problem type 1
- ◇ Solving a system of nonlinear equations: Problem type 2
- ◇ Solving a word problem involving geometry using a system of nonlinear equations
- ◇ Identifying solutions to a linear inequality in two variables
- ◇ Graphing a linear inequality in the plane: Vertical or horizontal line
- ◇ Graphing a linear inequality in the plane: Slope–intercept form
- ◇ Graphing a linear inequality in the plane: Standard form
- ◇ Writing an inequality given its graph in the plane: Horizontal or vertical boundary line
- ◇ Writing an inequality given its graph in the plane: Slanted boundary line
- ◇ Graphing a quadratic inequality: Problem type 1
- ◇ Graphing a quadratic inequality: Problem type 2
- ◇ Graphing an inequality involving a circle
- ◇ Graphing a system of two linear inequalities: Basic
- ◇ Graphing a system of two linear inequalities: Advanced
- ◇ Graphing a system of three linear inequalities
- ◇ Graphing a system of nonlinear inequalities: Problem type 1
- ◇ Writing a multi–step inequality for a real–world situation
- ◇ Solving a word problem using a system of linear inequalities: Problem type 1
- ◇ Solving a word problem using a system of linear inequalities: Problem type 2
- ◇ Linear programming
- ◇ Solving a word problem using linear programming
- ◆ Conic Sections (38 topics)
  - ◇ Graphing a parabola of the form  $y^2 = ax$  or  $x^2 = ay$
  - ◇ Graphing a parabola of the form  $x=a(y-k)^2+h$  or  $y=a(x-h)^2+k$
  - ◇ Graphing a parabola of the form  $ay^2 + by + cx + d = 0$  or  $ax^2 + bx + cy + d = 0$
  - ◇ Writing an equation of a parabola given the vertex and the focus
  - ◇ Writing an equation of a parabola given the focus and the directrix
  - ◇ Deriving the equation of a parabola given its focus and directrix
  - ◇ Finding the vertex, focus, directrix, and axis of symmetry of a parabola
  - ◇ Finding the focus of a parabola of the form  $ay^2 + by + cx + d = 0$  or  $ax^2 + bx + cy + d = 0$

- ◇ Writing an equation of a parabola given its graph
- ◇ Word problem involving a parabola
- ◇ Graphing an ellipse given its equation in standard form
- ◇ Graphing an ellipse centered at the origin:  $Ax^2 + By^2 = C$
- ◇ Graphing an ellipse given its equation in general form
- ◇ Finding the center, vertices, and foci of an ellipse
- ◇ Finding the foci of an ellipse given its equation in general form
- ◇ Writing an equation of an ellipse given the center, an endpoint of an axis, and the length of the other axis
- ◇ Writing an equation of an ellipse given the foci and the major axis length
- ◇ Graphing a system of nonlinear inequalities: Problem type 2
- ◇ Word problem involving an ellipse
- ◇ Graphing a hyperbola given its equation in standard form
- ◇ Graphing a hyperbola centered at the origin:  $Ax^2 + By^2 = C$
- ◇ Graphing a hyperbola given its equation in general form
- ◇ Finding the center, vertices, foci, and asymptotes of a hyperbola
- ◇ Finding the foci of a hyperbola given its equation in general form
- ◇ Writing an equation of a hyperbola given the foci and the vertices
- ◇ Writing an equation of a hyperbola given the foci and the asymptotes: Basic
- ◇ Writing an equation of a hyperbola given the foci and the asymptotes: Advanced
- ◇ Classifying conics given their equations
- ◇ Completing a table and choosing a graph given a pair of parametric equations
- ◇ Writing the equation of a line and sketching its graph given its parametric equations
- ◇ Writing the equation of a parabola and sketching its graph given its parametric equations
- ◇ Writing the equation of a circle or ellipse and sketching its graph given its parametric equations
- ◇ Graphing a pair of parametric equations with a restricted domain: Line or parabola
- ◇ Graphing a pair of parametric equations with a restricted domain: Circle
- ◇ Graphing a pair of parametric equations with a restricted domain: Ellipse
- ◇ Completing pairs of parametric equations
- ◇ Word problem involving parametric equations for projectile motion: Problem type 1
- ◇ Word problem involving parametric equations for projectile motion: Problem type 2
- ◆ Sequences, Series, and Probability (65 topics)
  - ◇ Finding the first terms of an arithmetic sequence using an explicit rule
  - ◇ Finding the first terms of a geometric sequence using an explicit rule
  - ◇ Finding the first terms of a sequence using an explicit rule with multiple occurrences of n
  - ◇ Finding the next terms of an arithmetic sequence with integers
  - ◇ Finding the first terms of a sequence using a recursive rule
  - ◇ Identifying arithmetic sequences and finding the common difference
  - ◇ Finding a specified term of an arithmetic sequence given the first terms
  - ◇ Finding a specified term of an arithmetic sequence given the common difference and first term
  - ◇ Finding a specified term of an arithmetic sequence given two terms of the sequence
  - ◇ Writing an explicit rule for an arithmetic sequence
  - ◇ Writing a recursive rule for an arithmetic sequence
  - ◇ Sum of the first n terms of an arithmetic sequence
  - ◇ Finding the next terms of a geometric sequence with signed numbers
  - ◇ Identifying arithmetic and geometric sequences
  - ◇ Identifying geometric sequences and finding the common ratio
  - ◇ Finding a specified term of a geometric sequence given the first terms
  - ◇ Finding a specified term of a geometric sequence given the common ratio and first term
  - ◇ Finding a specified term of a geometric sequence given two terms of the sequence
  - ◇ Arithmetic and geometric sequences: Identifying and writing an explicit rule
  - ◇ Writing recursive rules for arithmetic and geometric sequences
  - ◇ Sum of the first n terms of a geometric sequence

- ◇ Sum of an infinite geometric series
- ◇ Identifying linear, quadratic, and exponential functions given ordered pairs
- ◇ Factorial expressions
- ◇ Interpreting a tree diagram
- ◇ Introduction to the counting principle
- ◇ Counting principle
- ◇ Computing permutations and combinations
- ◇ Introduction to permutations and combinations
- ◇ Permutations and combinations: Problem type 1
- ◇ Permutations and combinations: Problem type 2
- ◇ Permutations and combinations: Problem type 3
- ◇ Binomial formula
- ◇ Determining a sample space and outcomes for a simple event
- ◇ Determining a sample space and outcomes for a compound event
- ◇ Probability of an event
- ◇ Experimental and theoretical probability
- ◇ Outcomes and event probability
- ◇ Probabilities of a permutation and a combination
- ◇ Area as probability
- ◇ Probability of independent events: Decimal answers
- ◇ Probability of dependent events
- ◇ Probabilities of draws with replacement
- ◇ Probabilities of draws without replacement
- ◇ Interpreting a Venn diagram of 2 sets
- ◇ Interpreting a Venn diagram of 3 sets
- ◇ Venn diagrams: Two events
- ◇ Shading a Venn diagram with 3 sets to represent a group
- ◇ Probabilities involving two rolls of a die
- ◇ Determining outcomes for compound events and complements of events
- ◇ Using a Venn diagram to understand the addition rule for probability
- ◇ Outcomes and event probability: Addition rule
- ◇ Word problem involving the probability of a union or an intersection
- ◇ Identifying independent events given values of probabilities
- ◇ Probability of the union and intersection of independent events
- ◇ Probability of the union of mutually exclusive events and independent events
- ◇ Using a Venn diagram to understand the multiplication rule for probability
- ◇ Outcomes and event probability: Conditional probability
- ◇ Computing conditional probability using a two–way frequency table
- ◇ Computing conditional probability to make an inference using a two–way frequency table
- ◇ Conditional probability: Basic
- ◇ Intersection and conditional probability
- ◇ Binomial problems: Basic
- ◇ Binomial problems: Advanced
- ◇ Using a random number table to make a fair decision
- ◆ Limits and Continuity (15 topics)
  - ◇ Estimating a limit numerically
  - ◇ Finding limits from a graph
  - ◇ Finding a limit by using the limit laws: Problem type 1
  - ◇ Finding limits for a piecewise–defined function
  - ◇ Finding a limit by using the limit laws: Problem type 2
  - ◇ Finding a limit by using the limit laws: Problem type 3
  - ◇ Squeeze Theorem
  - ◇ Determining points of discontinuity from a graph



- ◇ Determining a parameter to make a function continuous
- ◇ Infinite limits and graphs
- ◇ Limits at infinity and graphs
- ◇ Limits at infinity and rational functions
- ◇ Infinite limits and rational functions
- ◇ Finding a limit of a trigonometric function by using continuity
- ◇ Finding a limit by using special trigonometric limits

**\*Other Topics Available** *By default, these topics are NOT included in the course, but can be added using the content editor in the Teacher Module.*