## PreCalculus for College Readiness

This course covers the topics shown below.
Students navigate learning paths based on their level of readiness.
Institutional users may customize the scope and sequence to meet curricular needs.
Curriculum (597 topics + 646 additional topics)

- Algebra and Geometry Review (126 topics)
- Real Numbers and Algebraic Expressions (14 topics)
- Signed fraction addition or subtraction: Basic
- Signed fraction subtraction involving double negation
- Signed fraction multiplication: Basic
- Signed fraction division
- Computing the distance between two integers on a number line
- Exponents and integers: Problem type 1
- Exponents and signed fractions
- Order of operations with integers
- Evaluating a linear expression: Integer multiplication with addition or subtraction
- Evaluating a quadratic expression: Integers
- Evaluating a linear expression: Signed fraction multiplication with addition or subtraction
- Distributive property: Integer coefficients
- Using distribution and combining like terms to simplify: Univariate
- Using distribution with double negation and combining like terms to simplify: Multivariate
- Exponents (20 topics)
- Introduction to the product rule of exponents
- Product rule with positive exponents: Univariate
- Product rule with positive exponents: Multivariate
- Introduction to the power of a power rule of exponents
- Introduction to the power of a product rule of exponents
- Power rules with positive exponents: Multivariate products
- Power rules with positive exponents: Multivariate quotients
- Simplifying a ratio of multivariate monomials: Basic
- Introduction to the quotient rule of exponents
- Simplifying a ratio of univariate monomials
- Quotient of expressions involving exponents
- Evaluating expressions with exponents of zero
- Evaluating an expression with a negative exponent: Whole number base
- Evaluating an expression with a negative exponent: Positive fraction base
- Evaluating an expression with a negative exponent: Negative integer base
- Rewriting an algebraic expression without a negative exponent
- Introduction to the product rule with negative exponents
- Quotient rule with negative exponents: Problem type 1
- Power of a power rule with negative exponents
- Power rules with negative exponents
- Polynomial Expressions (14 topics)
- Degree and leading coefficient of a univariate polynomial
- Simplifying a sum or difference of two univariate polynomials
- Multiplying a univariate polynomial by a monomial with a positive coefficient
- Multiplying a univariate polynomial by a monomial with a negative coefficient
- Multiplying a multivariate polynomial by a monomial
- Multiplying binomials with leading coefficients of 1
- Multiplying binomials with leading coefficients greater than 1
- Multiplying binomials in two variables
- Multiplying conjugate binomials: Univariate
- Squaring a binomial: Univariate
- Squaring a binomial: Multivariate
- Multiplying binomials with negative coefficients
- Multiplication involving binomials and trinomials in one variable
- Multiplication involving binomials and trinomials in two variables
- Factoring Polynomials (16 topics)
- Greatest common factor of 2 numbers
- Factoring a linear binomial
- Introduction to the GCF of two monomials
- Greatest common factor of two multivariate monomials
- Factoring out a monomial from a polynomial: Univariate
- Factoring out a monomial from a polynomial: Multivariate
- Factoring out a binomial from a polynomial: GCF factoring, basic
- Factoring a univariate polynomial by grouping: Problem type 1
- Factoring a quadratic with leading coefficient 1
- Factoring out a constant before factoring a quadratic
- Factoring a quadratic with leading coefficient greater than 1: Problem type 1
- Factoring a quadratic with leading coefficient greater than 1: Problem type 2

Factoring a quadratic with a negative leading coefficient
Factoring a perfect square trinomial with leading coefficient 1

- Factoring a difference of squares in one variable: Basic

Factoring a difference of squares in one variable: Advanced

- Rational Expressions (28 topics)
- Restriction on a variable in a denominator: Linear

Simplifying a ratio of factored polynomials: Linear factors
Simplifying a ratio of polynomials using GCF factoring
Simplifying a ratio of polynomials by factoring a quadratic with leading coefficient 1
Simplifying a ratio of polynomials: Problem type 1
Multiplying rational expressions involving linear expressions
Multiplying rational expressions involving quadratics with leading coefficients of 1
Dividing rational expressions involving linear expressions
Dividing rational expressions involving quadratics with leading coefficients of 1
Least common multiple of 2 numbers
Least common multiple of 3 numbers
Introduction to the LCM of two monomials
Finding the LCD of rational expressions with linear denominators: Relatively prime
Writing equivalent rational expressions with polynomial denominators
Introduction to adding fractions with variables and common denominators
Adding rational expressions with common denominators and monomial numerators
Adding rational expressions with common denominators and binomial numerators
Adding rational expressions with common denominators and GCF factoring
Adding rational expressions with common denominators and quadratic factoring
Adding rational expressions with different denominators and a single occurrence of a variable
Adding rational expressions with denominators ax and bx: Basic
Adding rational expressions with denominators ax and bx: Advanced
Adding rational expressions with linear denominators without common factors: Basic
Complex fraction without variables: Problem type 1
Complex fraction without variables: Problem type 2
Complex fraction involving univariate monomials
Complex fraction: GCF fact oring
Complex fraction made of sums involving rational expressions: Problem type 1

- Perfect Squares and nth Roots (7 topics)
- Square root of a rational perfect square

Square roots of perfect squares with signs
Introduction to simplifying a radical expression with an even exponent
Square root of a perfect square monomial
Introduction to solving an absolute value equation

- Cube root of an integer

Finding $\mathrm{n}^{\text {th }}$ roots of perfect $\mathrm{n}^{\text {th }}$ powers with signs

- Rational Exponents (4 topics)
- Converting between radical form and exponent form

Rational exponents: Unit fraction exponents and whole number bases
Rational exponents: Non-unit fraction exponent with a whole number base
Rational exponents: Negative exponents and fractional bases

- Radical Expressions (19 topics)

Simplifying the square root of a whole number less than 100
Simplifying a radical expression with an even exponent
Introduction to simplifying a radical expression with an odd exponent
Simplifying a radical expression with an odd exponent
Simplifying a higher root of a whole number
Introduction to square root addition or subtraction
Square root addition or subtraction
Introduction to square root multiplication
Square root multiplication: Basic
Square root multiplication: Advanced
Introduction to simplifying a product of radical expressions: Univariate
Introduction to simplifying a product involving square roots using the distributive property
Simplifying a product involving square roots using the distributive property: Basic
Simplifying a product involving square roots using the distributive property: Advanced
Simplifying a quotient of square roots
Simplifying a quotient involving a sum or difference with a square root
Rationalizing a denominator: Quotient involving square roots

- Rationalizing a denominator: Square root of a fraction
- Rationalizing a denominator using conjugates: Integer numerator
- Geometry (4 topics)
- Circumference of a circle
- Volume of a rectangular prism
- Introduction to the Pythagorean Theorem
- Pythagorean Theorem
- Equations and Inequalities (83 topics)
- Linear Equations and Applications (27 topics)
- Additive property of equality with signed fractions
- Multiplicative property of equality with signed fractions
- Solving a multi-step equation given in fractional form
- Solving a linear equation with several occurrences of the variable: Variables on the same side and distribution
- Solving a linear equation with several occurrences of the variable: Variables on both sides and distribution
- Solving a linear equation with several occurrences of the variable: Variables on both sides and two distributions
- Solving a linear equation with several occurrences of the variable: Fractional forms with monomial numerators
- Solving a two-step equation with signed fractions
- Solving a linear equation with several occurrences of the variable: Variables on both sides and fractional coefficients
- Solving a linear equation with several occurrences of the variable: Fractional forms with binomial numerators
- Solving a proportion of the form $(x+a) / b=c / d$
- Solving for a variable in terms of other variables using addition or subtraction: Basic
- Solving for a variable in terms of other variables using addition or subtraction: Advanced
- Solving for a variable in terms of other variables using multiplication or division: Basic
- Solving for a variable in terms of other variables using multiplication or division: Advanced
- Solving for a variable in terms of other variables using addition or subtraction with division
- Solving for a variable inside parentheses in terms of other variables
- Solving for a variable in terms of other variables in a linear equation with fractions
- Translating a sentence into a one-step equation
- Translating a sentence into a multi-step equation
- Solving a word problem with two unknowns using a linear equation
- Solving a decimal word problem using a linear equation of the form $A x+B=C$
- Solving a word problem with three unknowns using a linear equation
- Solving a one-step word problem using the formula $d=r t$
- Solving a distance, rate, time problem using a linear equation
- Finding the perimeter or area of a rectangle given one of these values
- Finding the sale price given the original price and percent discount
- Absolute Value Equations (2 topics)
- Solving an absolute value equation: Problem type 1
- Solving an absolute value equation: Problem type 2
- Linear Inequalities and Applications (7 topics)
- Graphing a linear inequality on the number line
- Graphing a compound inequality on the number line
- Set-builder and interval notation
- Identifying solutions to a two-step linear inequality in one variable
- Solving a two-step linear inequality: Problem type 1
- Solving a two-step linear inequality: Problem type 2
- Solving a linear inequality with multiple occurrences of the variable: Problem type 1
- Rational Equations that Simplify to Linear (8 topics)
- Solving a rational equation that simplifies to linear: Denominator $x$
- Solving a rational equation that simplifies to linear: Denominator $x+a$
- Solving a rational equation that simplifies to linear: Denominators a, x, or ax
- Solving a rational equation that simplifies to linear: Denominators ax and bx
- Solving a rational equation that simplifies to linear: Like binomial denominators
- Solving a rational equation that simplifies to linear: Unlike binomial denominators
- Solving for a variable in terms of other variables in a rational equation: Problem type 1
- Solving for a variable in terms of other variables in a rational equation: Problem type 2
- Complex Numbers (4 topics)
- Using ito rewrite square roots of negative numbers
- Adding or subtracting complex numbers
- Multiplying complex numbers
- Dividing complex numbers
- Quadratic Equations (20 topics)
- Solving an equation written in factored form
- Finding the roots of a quadratic equation of the form $\mathrm{ax}^{2}+\mathrm{bx}=0$
- Finding the roots of a quadratic equation with leading coefficient 1
- Finding the roots of a quadratic equation with leading coefficient greater than 1
- Solving a quadratic equation needing simplification
- Roots of a product of polynomials
- Writing a quadratic equation given the roots and the leading coefficient
- Solving a word problem using a quadratic equation with rational roots
- Solving an equation of the form $x^{2}=a$ using the square root property
- Solving a quadratic equation using the square root property: Exact answers, basic
- Solving a quadratic equation using the square root property: Exact answers, advanced
- Completing the square
- Solving a quadratic equation by completing the square: Exact answers
- Applying the quadratic formula: Exact answers
- Applying the quadratic formula: Decimal answers
- Solving a quadratic equation with complex roots
- Discriminant of a quadratic equation
- Solving a word problem using a quadratic equation with irrational roots
- Solving an equation using the odd-root property: Problem type 1
- Solving an equation using the odd-root property: Problem type 2
- Rational Equations that Simplify to Quadratic (5 topics)
- Restriction on a variable in a denominator: Quadratic
- Solving a rational equation that simplifies to linear: Factorable quadratic denominator
- Solving a rational equation that simplifies to quadratic: Denominator x
- Solving a rational equation that simplifies to quadratic: Binomial denominators, constant numerators
- Solving a rational equation that simplifies to quadratic: Binomial denominators and numerators
- Radical Equations (10 topics)
- Introduction to solving a radical equation
- Solving a radical equation that simplifies to a linear equation: One radical, basic
- Solving a radical equation that simplifies to a linear equation: One radical, advanced
- Solving a radical equation that simplifies to a linear equation: Two radicals
- Solving a radical equation that simplifies to a quadratic equation: One radical, basic
- Solving a radical equation that simplifies to a quadratic equation: One radical, advanced
- Solving for a variable in terms of other variables in an equation involving radicals
- Solving an equation with a root index greater than 2: Problem type 1
- Solving an equation with a root index greater than 2: Problem type 2
- Solving an equation that can be written in quadratic form: Problem type 1
- Graphs and Functions (139 topics)
- The Coordinate Plane, Distance, and Midpoint (9 topics)
- Reading a point in the coordinate plane
- Plotting a point in the coordinate plane
- Naming the quadrant or axis of a point given its coordinates
- Naming the quadrant or axis of a point given the signs of its coordinates
- Table for a linear equation
- Distance between two points in the plane: Exact answers
- Midpoint of a line segment in the plane
- Identifying solutions to a linear equation in two variables
- Finding a solution to a linear equation in two variables
- Graphs of Equations (16 topics)
- Graphing a linear equation of the form $y=m x$
- Graphing a line given its equation in slope-intercept form: Integer slope
- Graphing a line given its equation in slope-intercept form: Fractional slope
- Graphing a line given its equation in standard form
- Graphing a vertical or horizontal line
- Finding $x$ - and $y$-intercepts given the graph of a line on a grid
- Finding $x$ - and $y$-intercepts of a line given the equation: Basic
- Finding $x$ - and $y$-intercepts of a line given the equation: Advanced
- Graphing a line by first finding its $x$ - and $y$-intercepts
- Finding intercepts of a nonlinear function given its graph
- Finding $x$ - and $y$-intercepts of the graph of a nonlinear equation
- Graphing an absolute value equation of the form $y=A|x|$
- Graphing a parabola of the form $y=a x^{2}$
- Graphing a parabola of the form $y=a x^{2}+c$
- Graphing a cubic function of the form $y=a x^{3}$
- Determining if graphs have symmetry with respect to the $x$-axis, $y$-axis, or origin
- Slope and Equations of Lines (17 topics)
- Finding slope given the graph of a line on a grid
- Finding slope given two points on a line
- Finding the slopes of horizontal and vertical lines
- Graphing a line given its slope and y-intercept
- Finding the slope and $y$-intercept of a line given its equation in the form $y=m x+b$
- Finding the slope and y-intercept of a line given its equation in the form $A x+B y=C$
- Graphing a line by first finding its slope and y-intercept

Writing an equation of a line given its slope and $y$-intercept
Writing an equation in slope-intercept form given the slope and a point
Finding the slope and a point on a line given its equation in point-slope form
Writing the equation of a line in point-slope form given the slope and a point
Writing the equation of a line given the y-intercept and another point
Writing the equation of a line through two given points
Writing the equations of vertical and horizontal lines through a given point
Finding slopes of lines parallel and perpendicular to a line given in slope-intercept form
Finding slopes of lines parallel and perpendicular to a line given in the form Ax + By = C
Writing equations of lines parallel and perpendicular to a given line through a point

- Linear Applications (5 topics)
- Writing and evaluating a function that models a real-world situation: Advanced

Writing an equation and drawing its graph to model a real-world situation: Advanced
Finding the intercepts and rate of change given a graph of a linear function
Interpreting the parameters of a linear function that models a real-world situation
Application problem with a linear function: Finding a coordinate given two points

- Circles (6 topics)

Identifying the center and radius to graph a circle given its equation in standard form
Identifying the center and radius to graph a circle given its equation in general form: Basic
Writing the equation of a circle centered at the origin given its radius or a point on the circle
Writing an equation of a circle given its center and radius or diameter
Writing an equation of a circle given its center and a point on the circle
Writing an equation of a circle given the endpoints of a diameter

- Functions (26 topics)

Identifying functions from relations
Vertical line test
Table for a linear function
Evaluating functions: Linear and quadratic or cubic
Evaluating a rational function: Problem type 1
Evaluating a rational function: Problem type 2
Table for a square root function
Evaluating a cube root function
Evaluat ing functions: Absolute value, rational, radical
Evaluating a piecewise-defined function
Variable expressions as inputs of functions: Problem type 1
Variable expressions as inputs of functions: Problem type 2
Variable expressions as inputs of functions: Problem type 3
Domain and range from ordered pairs
Domain of a rational function: Excluded values
Domain of a rational function: Interval notation
Domain of a square root function: Basic
Domain of a square root function: Advanced
Finding the domain of a fractional function involving radicals
Determining whether an equation defines a function: Basic
Determining whether an equation defines a function: Advanced
Finding outputs of a one-step function that models a real-world situation: Function notation
Finding outputs of a two-step function with decimals that models a real-world situation: Function notation
Finding inputs and outputs of a two-step function that models a real-world situation: Function notation
Finding a difference quotient for a linear or quadratic function
Finding a difference quotient for a rational function

- Graphs of Functions (28 topics)

Finding an output of a function from its graph
Finding inputs and outputs of a function from its graph
Domain and range from the graph of a continuous function
Domain and range from the graph of a piecewise function
Finding where a function is increasing, decreasing, or constant given the graph
Finding where a function is increasing, decreasing, or constant given the graph: Interval notation
Finding local maxima and minima of a function given the graph
Finding the absolute maximum and minimum of a function given the graph
Finding values and intervals where the graph of a function is zero, positive, or negative
Graphing a function of the form $f(x)=a x+b$ : Integer slope
Graphing a function of the form $f(x)=a x+b$ : Fractional slope
Graphing an absolute value equation in the plane: Basic
Graphing an absolute value equation in the plane: Advanced
Graphing a function of the form $f(x)=a x^{2}$
Graphing a function of the form $f(x)=a x^{2}+c$
Graphing a parabola of the form $y=(x-h)^{2}+k$
Graphing a square root function: Problem type 1

- Graphing a square root function: Problem type 2
- Matching parent graphs with their equations
- Graphing a piecewise-defined function: Problem type 1
- Introduction to graphing a piecewise-defined function involving lines with non-zero slope
- Graphing a piecewise-defined function: Problem type 2
- Graphing a piecewise-defined function: Problem type 3
- Even and odd functions: Problem type 1
- Even and odd functions: Problem type 2
- Finding the average rate of change of a function
- Finding the average rate of change of a function given its graph
- Word problem involving average rate of change
- Transformations (13 topics)
- Translating the graph of a parabola: One step
- Translating the graph of a parabola: Two steps
- How the leading coefficient affects the shape of a parabola
- Translating the graph of an absolute value function: One step
- Translating the graph of an absolute value function: Two steps
- Writing an equation for a function after a vertical translation
- Translating the graph of a function: One step
- Translating the graph of a function: Two steps
- Transforming the graph of a function by reflecting over an axis
- Transforming the graph of a function by shrinking or stretching
- Transforming the graph of a function using more than one transformation
- Transforming the graph of a quadratic, cubic, square root, or absolute value function
- Writing an equation for a function after a vertical and horizontal translation
- Combining Functions; Composite Functions; Inverse Functions (19 topics)
- Sum, difference, and product of two functions
- Quotient of two functions: Basic
- Quotient of two functions: Advanced
- Combining functions: Advanced
- Introduction to the composition of two functions
- Composition of two functions: Basic
- Composition of a function with itself
- Expressing a function as a composition of two functions
- Composition of two functions: Advanced
- Composition of two rational functions
- Word problem involving composition of two functions
- Horizontal line test
- Determining whether two functions are inverses of each other
- Inverse functions: Linear, discrete

Inverse functions: Quadratic, square root
Inverse functions: Cubic, cube root
Inverse functions: Rational
Graphing the inverse of a function given its graph

- Finding, evaluating, and interpreting an inverse function for a given linear relationship
- Polynomial and Rational Functions (64 topics)
- Quadratic Functions (16 topics)
- Finding the vertex, intercepts, and axis of symmetry from the graph of a parabola
- Graphing a parabola of the form $y=x^{2}+b x+c$
- Graphing a parabola of the form $y=a(x-h)^{2}+k$
- Graphing a parabola of the form $y=a x^{2}+b x+c$ : Integer coefficients
- Finding the zeros of a quadratic function given its equation
- Using a graphing calculator to find the zeros of a quadratic function
- Writing a quadratic function given its zeros
- Finding the x-intercept(s) and the vertex of a parabola
- Using a graphing calculator to find the x-intercept(s) and vertex of a quadratic function
- Rewriting a quadratic function to find its vertex and sketch its graph
- Finding the maximum or minimum of a quadratic function
- Word problem involving the maximum or minimum of a quadratic function
- Word problem involving optimizing area by using a quadratic function
- Domain and range from the graph of a quadratic function
- Range of a quadratic function
- Writing the equation of a quadratic function given its graph
- Polynomial Functions (10 topics)
- Finding zeros of a polynomial function written in factored form
- Finding zeros and their multiplicities given a polynomial function written in factored form
- Finding a polynomial of a given degree with given zeros: Real zeros
- Finding $x$ - and $y$-intercepts given a polynomial function
- Determining the end behavior of the graph of a polynomial function
- Determining end behavior and intercepts to graph a polynomial function
- Matching graphs with polynomial functions
- Inferring properties of a polynomial function from its graph
- Using a graphing calculator to find local extrema of a polynomial function
- Using a graphing calculator to solve a word problem involving a local extremum of a polynomial function
- Division of Polynomials; Remainder and Factor Theorems (6 topics)
- Polynomial long division: Problem type 1
- Polynomial long division: Problem type 2
- Polynomial long division: Problem type 3
- Synthetic division
- Using the remainder theorem to evaluate a polynomial
- The Factor Theorem
- Real Zeros of Polynomial Functions (7 topics)
- Using a given zero to write a polynomial as a product of linear factors: Real zeros
- Finding all possible rational zeros using the rational zeros theorem: Problem type 1
- Finding all possible rational zeros using the rational zeros theorem: Problem type 2
- Using the rational zeros theorem to find all zeros of a polynomial: Rational zeros
- Using the rational zeros theorem to find all zeros of a polynomial: Irrational zeros
- Using a graphing calculat or to find zeros of a polynomial function
- Using a graphing calculator to solve a word problem involving a polynomial of degree 3
- Complex Zeros of Polynomials Functions (4 topics)
- Multiplying expressions involving complex conjugates
- Finding a polynomial of a given degree with given zeros: Complex zeros
- Using a given zero to write a polynomial as a product of linear factors: Complex zeros
- Using the rational zeros theorem to find all zeros of a polynomial: Complex zeros
- Rational Functions (13 topics)
- Finding the intercepts, asymptotes, domain, and range from the graph of a rational function
- Finding the asymptotes of a rational function: Constant over linear
- Finding the asymptotes of a rational function: Linear over linear
- Finding horizontal and vertical asymptotes of a rational function: Quadratic numerator or denominator
- Finding the asymptotes of a rational function: Quadratic over linear
- Graphing a rational function: Constant over linear
- Graphing a rational function: Linear over linear
- Transforming the graph of a rational function
- Graphing a rational function: Quadratic over linear
- Graphing rational functions with holes
- Matching graphs with rational functions: Two vertical asymptotes
- Graphing a rational function with more than one vertical asymptote
- Using a graphing calculator to solve a word problem involving a local extremum of a rational function
- Polynomial and Rational Inequalities (8 topics)
- Solving a quadratic inequality written in factored form
- Solving a quadratic inequality
- Solving a polynomial inequality: Problem type 1
- Solving a polynomial inequality: Problem type 2
- Solving a polynomial inequality: Problem type 3
- Solving a polynomial inequality: Problem type 4
- Solving a rational inequality: Problem type 1
- Solving a rational inequality: Problem type 2
- Exponential and Logarithmic Functions (50 topics)
- Graphing Exponential Functions (8 topics)
- Table for an exponential function
- Graphing an exponential function and its asymptote: $f(x)=b^{x}$
- Graphing an exponential function and its asymptote: $f(x)=a(b)^{x}$
- Graphing an exponential function and its asymptote: $f(x)=b^{-x}$ or $f(x)=-b^{x}$ or $f(x)=-b^{-x}$
- Translating the graph of an exponential function
- Graphing an exponential function and finding its domain and range
- Transforming the graph of a natural exponential function and finding its domain and range
- Graphing an exponential function and its asymptote: $f(x)=a(e)^{x-b}+c$
- Applications of Exponential Functions (7 topics)
- Using a calculator to evaluate exponential expressions
- Evaluating an exponential function that models a real-world situation
- Using a calculator to evaluate exponential expressions involving base e
- Evaluating an exponential function with base e that models a real-world situation
- Introduction to compound interest
- Finding a final amount in a word problem on exponential growth or decay
- Finding the final amount in a word problem on compound interest
- Logarithmic Functions (9 topics)
- Using a calculat or to evaluate natural and common logarithmic expressions
- Converting between logarithmic and exponential equations
- Converting between natural logarithmic and exponential equations
- Evaluating logarithmic expressions
- Solving an equation of the form $\log _{b} a=c$
- Translating the graph of a logarithmic function
- Graphing a logarithmic function: Basic
- Graphing a logarithmic function and finding its domain and range
- Domain of a logarithmic function: Advanced
- Properties of Logarithms (6 topics)
- Basic properties of logarithms
- Using properties of logarithms to evaluate expressions
- Expanding a logarithmic expression: Problem type 1
- Expanding a logarithmic expression: Problem type 2
- Writing an expression as a single logarithm
- Change of base for logarithms: Problem type 1
- Logarithmic and Exponential Equations (10 topics)
- Solving a multi-step equation involving a single logarithm: Problem type 1
- Solving a multi-step equation involving a single logarithm: Problem type 2
- Solving a multi-step equation involving natural logarithms
- Solving an equation involving logarithms on both sides: Problem type 1
- Solving an equation involving logarithms on both sides: Problem type 2
- Solving an exponential equation by finding common bases: Linear exponents
- Solving an exponential equation by using logarithms: Decimal answers, basic
- Solving an exponential equation by using natural logarithms: Decimal answers
- Solving an exponential equation by using logarithms: Decimal answers, advanced
- Solving an exponential equation by using logarithms: Exact answers in logarithmic form
- Applications (10 topics)
- Finding the time to reach a limit in a word problem on exponential growth or decay
- Finding the time in a word problem on compound interest
- Finding the time given an exponential function with base e that models a real-world situation
- Finding the final amount in a word problem on continuous compound interest
- Finding the initial amount in a word problem on continuous compound interest
- Finding the final amount in a word problem on continuous exponential growth or decay
- Finding the rate or time in a word problem on continuous exponential growth or decay
- Finding half-life or doubling time
- Writing and evaluating a function modeling continuous exponential growth or decay given doubling time or half-life
- Writing and evaluating a function modeling continuous exponential growth or decay given two outputs
- Trigonometric Functions (80 topics)
- Angles and Their Measure (6 topics)
- Converting degrees to radians and radians to degrees: Problem type 1
- Converting degrees to radians and radians to degrees: Problem type 2
- Sketching an angle with absolute value less than 360 degrees in standard position
- Sketching an angle with absolute value less than $2 \pi$ radians in standard position
- Coterminal angles
- Arc length and central angle measure
- The Unit Circle and Evaluating Trigonometric Functions (15 topics)
- Finding coordinates on the unit circle for special angles
- Using the coordinates of points on the unit circle to define sine and cosine for all real numbers
- Special triangles with a hypotenuse of length 1
- Drawing a reference triangle on the unit circle and using it to derive values of trigonometric functions: Radians
- Trigonometric functions and special angles: Problem type 1: Degrees
- Trigonometric functions and special angles: Problem type 1: Radians
- Finding values of trigonometric functions from a point on the unit circle
- Trigonometric functions and special angles: Problem type 2
- Using the coordinates of points on the unit circle to define trigonometric functions for all real numbers
- Trigonometric functions and special angles: Problem type 3
- Using the unit circle to understand the odd and even identities for sine and cosine
- Evaluating expressions involving sine or cosine
- Odd and even identities for trigonometric functions
- Using a calculat or to approximate sine, cosine, and tangent values
- Evaluating a sinusoidal function that models a real-world situation
- Right Triangle Trigonometry (10 topics)
- Sine, cosine, and tangent ratios: Variables for side lengths
- Using the Pythagorean Theorem to find a sine, cosine, or tangent ratio in a right triangle
- Using the Pythagorean Theorem to find several trigonometric ratios in a right triangle
- Using a trigonometric ratio to find a side length in a right triangle
- Using trigonometry to find a length in a word problem with one right triangle
- Using trigonometric functions and the formula $d=r t$ in a real-world situation
- Using a trigonometric ratio to find an angle measure in a right triangle
- Using trigonometry to find angles of elevation or depression in a word problem
- Solving a right triangle
- Using trigonometry to find a length in a word problem with two right triangles
- Trigonometric Functions of Angles (12 topics)
- Sketching an angle with absolute value less than 360 degrees, and also its reference angle
- Reference angles in degrees: Problem type 1
- Reference angles in degrees: Problem type 2
- Sketching an angle with absolute value less than $2 \pi$ radians, and also its reference angle
- Reference angles in radians: Problem type 1
- Sketching an angle with absolute value greater than $2 \pi$ radians, and also its reference angle
- Reference angles in radians: Problem type 2
- Determining the location of a terminal point given the signs of trigonometric values
- Finding values of trigonometric functions given information about an angle: Problem type 1
- Finding values of trigonometric functions given information about an angle: Problem type 2
- Finding values of trigonometric functions given information about an angle: Problem type 3
- Finding values of trigonometric functions given information about an angle: Problem type 4
- Graphs of Sine and Cosine Functions (23 topics)
- Sketching the graph of $y=a \sin (x)$ or $y=a \cos (x)$
- Sket ching the graph of $y=\sin (b x)$ or $y=\cos (b x)$
- Using transformations to graph y = $\pm \sin (\mathrm{bx})$ or $\mathrm{y}= \pm \cos (\mathrm{bx})$
- Sketching the graph of $y=\sin (x)+d$ or $y=\cos (x)+d$
- Using transformations to graph $y= \pm \sin (x)+d$ or $y= \pm \cos (x)+d$
- Using transformations to graph $y=a \sin (x)+d$ or $y=a \cos (x)+d$
- Using transformations to graph $y= \pm \sin (b x)+d$ or $y= \pm \cos (b x)+d$
- Sketching the graph of $y=\sin (x+c)$ or $y=\cos (x+c)$
- Sketching the graph of $y=a \sin (x+c)$ or $y=a \cos (x+c)$
- Using transformations to graph $y=a \sin (x+c)+d$ or $y=a \cos (x+c)+d$
- Sketching the graph of $y=a \sin (b x)$ or $y=a \cos (b x)$
- Using transformations to graph $y=\sin (b x+c)$ or $y=\cos (b x+c)$
- Sketching the graph of $y=a \sin (b x+c)$ or $y=a \cos (b x+c)$
- Sketching the graph of $y=a \sin (b x)+d$ or $y=a \cos (b x)+d$
- Using transformations to graph $y=a \sin (b x+c)+d$ or $y=a \cos (b x+c)+d$
- Amplitude and period of a sine or cosine function
- Amplitude, period, and phase shift of a sine or cosine function
- Interpreting the graph of a sinusoidal function that models a real-world situation
- Writing the equation of a sine or cosine function given its graph: Problem type 1
- Writing the equation of a sine or cosine function given its graph: Problem type 2
- Word problem involving a sine or cosine function: Problem type 1
- Developing a sinusoidal model for a real-world situation
- Word problem involving a sine or cosine function: Problem type 2
- Graphs of Other Trigonometric Functions (6 topics)
- Domains and ranges of trigonometric functions
- Matching graphs and equations for secant, cosecant, tangent, and cotangent functions
- Sketching the graph of a secant or cosecant function: Problem type 1
- Sketching the graph of a secant or cosecant function: Problem type 2
- Sketching the graph of a tangent or cotangent function: Problem type 2
- Sketching the graph of a tangent or cotangent function: Problem type 1
- Inverse Trigonometric Functions (8 topics)
- Values of inverse trigonometric functions
- Composition of a trigonometric function with its inverse trigonometric function: Problem type 1
- Composition of a trigonometric function with its inverse trigonometric function: Problem type 2
- Composition of a trigonometric function with the inverse of another trigonometric function: Problem type 1
- Composition of a trigonometric function with the inverse of another trigonometric function: Problem type 2
- Composition of a trigonometric function with the inverse of another trigonometric function: Problem type 3
- Composition of trigonometric functions with variable expressions as inputs: Problem type 1
- Using a calculator to approximate inverse trigonometric values
- Trigonometric Identities and Equations (49 topics)
- Verifying Trigonometric Identities (13 topics)
- Using reciprocal and quotient identities to simplify a trigonometric expression
- Using Pythagorean identities to simplify a trigonometric expression
- Using cofunction identities
- Verifying a trigonometric identity: Problem type 1
- Verifying a trigonometric identity: Problem type 2
- Verifying a trigonometric identity: Problem type 3
- Proving an identity using fundamental trigonometric identities: Problem type 1
- Proving an identity using fundamental trigonometric identities: Problem type 2
- Proving an identity using fundamental trigonometric identities: Problem type 3
- Proving an identity using fundamental trigonometric identities: Problem type 4
- Proving an identity using fundamental trigonometric identities: Problem type 5
- Proving an identity using fundamental trigonometric identities: Problem type 6
- Proving an identity using fundamental trigonometric identities: Problem type 7
- Sum and Difference Formulas (9 topics)
- Sum and difference identities: Problem type 1: Degrees
- Sum and difference identities: Problem type 1: Radians
- Sum and difference identities: Problem type 2: Degrees
- Sum and difference identities: Problem type 2: Radians
- Sum and difference identities: Problem type 3
- Sum and difference identities: Problem type 4
- Proving trigonometric identities using sum and difference identities: Problem type 1
- Proving trigonometric identities using sum and difference identities: Problem type 2
- Proving trigonometric identities using sum and difference identities: Problem type 3
- Double-Angle, Half-Angle, Product-to-Sum, and Power Reducing Formulas (11 topics)
- Double-angle identities: Problem type 1
- Double-angle identities: Problem type 2
- Power-reducing identities
- Half-angle identities: Problem type 1: Degrees
- Half-angle identities: Problem type 1: Radians
- Half-angle identities: Problem type 2
- Product-to-sum and sum-to-product identities: Problem type 1: Degrees
- Product-to-sum and sum-to-product identities: Problem type 1: Radians
- Product-to-sum and sum-to-product identities: Problem type 2
- Proving trigonometric identities using double-angle identities: Problem type 1
- Proving trigonometric identities using double-angle identities: Problem type 2
- Trigonometric Equations (16 topics)
- Finding solutions in an interval for a basic trigonometric equation involving sine or cosine
- Finding solutions in an interval for a basic trigonometric equation involving tangent, cotangent, secant, or cosecant
- Finding solutions in an interval for a basic trigonometric equation using a calculator
- Solving a basic trigonometric equation involving sine or cosine
- Solving a basic trigonometric equation involving tangent, cotangent, secant, or cosecant
- Finding solutions in an interval for a trigonometric equation involving sine and cosine and written in factored form
- Finding solutions in an interval for a trigonometric equation written in factored form
- Finding solutions in an interval for a trigonometric equation involving a squared function: Problem type 1
- Factoring to find solutions in an interval for a trigonometric equation involving sine or cosine
- Factoring to find solutions in an interval for a trigonometric equation

Using a Pythagorean identity to find solutions in an interval for a trigonometric equation involving sine and cosine:

- Problem type 1
- Using a Pythagorean identity to find solutions in an interval for a trigonometric equation: Problem type 1
- Finding solutions in an interval for a trigonometric equation involving sine and/or cosine using double-angle identities
- Solving a trigonometric equation modeling a real-world situation

Finding solutions in an interval for a trigonometric equation involving sine or cosine and an angle multiplied by a

- constant
- Finding solutions in an interval for a trigonometric equation involving an angle multiplied by a constant


## - Additional Topics in Trigonometry (6 topics)

- Laws of Sines and Cosines (6 topics)
- Solving a triangle with the law of sines: Problem type 1
- Solving a triangle with the law of sines: Problem type 2
- Solving a word problem using the law of sines
- Solving a triangle with the law of cosines
- Solving a word problem using the law of cosines
- Solving a word problem using the law of sines and the law of cosines
- Other Topics Available(*) (646 additional topics)
- Algebra and Geometry Review (160 topics)
- Fractional position on a number line
- Plotting rational numbers on a number line
- Ordering integers
- Estimating a square root
- Ordering real numbers
- Identifying numbers as integers or non-integers

Identifying numbers as rational or irrational
Signed fraction addition or subtraction: Advanced
Addition and subtraction of 3 fractions involving signs
Signed fraction multiplication: Advanced
Operations with absolute value: Problem type 2
Exponents and integers: Problem type 2
Order of operations with integers and exponents
Converting between temperatures in Fahrenheit and Celsius
Properties of addition
Properties of real numbers
Identifying properties used to simplify an algebraic expression
Understanding the product rule of exponents
Ordering numbers with positive exponents
Understanding the power rules of exponents
Power and product rules with positive exponents
Simplifying a ratio of multivariate monomials: Advanced
Power and quotient rules with positive exponents
Ordering numbers with negative exponents
Product rule with negative exponents
Quotient rule with negative exponents: Problem type 2
Power and quotient rules with negative exponents: Problem type 1
Power and quotient rules with negative exponents: Problem type 2
Power, product, and quotient rules with negative exponents
Scientific notation with a positive exponent
Scientific notation with a negative exponent
Converting between scientific notation and standard form in a real-world situation
Multiplying numbers written in scientific notation: Basic
Multiplying numbers written in scientific notation: Advanced
Multiplying numbers written in decimal form or scientific notation in a real-world situation
Dividing numbers written in scientific notation: Basic
Dividing numbers written in scientific notation: Advanced
Finding the scale factor between numbers given in scientific notation in a real-world situation
Degree of a multivariate polynomial
Simplifying a sum or difference of three univariate polynomials
Simplifying a sum or difference of multivariate polynomials
Multiplying conjugate binomials: Multivariate
Prime numbers
Prime factorization
Greatest common factor of three univariate monomials
Factoring a univariate polynomial by grouping: Problem type 2
Factoring a multivariate polynomial by grouping: Problem type 1
Factoring a multivariate polynomial by grouping: Problem type 2
Factoring a quadratic in two variables with leading coefficient 1
Factoring a quadratic with leading coefficient greater than 1: Problem type 3
Factoring a quadratic by the ac-method
Factoring a quadratic in two variables with leading coefficient greater than 1
Factoring a perfect square trinomial with leading coefficient greater than 1
Factoring a perfect square trinomial in two variables
Factoring a difference of squares in two variables
Factoring a polynomial involving a GCF and a difference of squares: Univariate
Factoring a polynomial involving a GCF and a difference of squares: Multivariate
Factoring a product of a quadratic trinomial and a monomial
Factoring with repeated use of the difference of squares formula
Factoring a sum or difference of two cubes
Factoring out binomials from a polynomial: GCF factoring, advanced
Using substitution to factor polynomials
Simplifying a ratio of factored polynomials: Factors with exponents
Simplifying a ratio of linear polynomials: $1,-1$, and no simplification
Simplifying a ratio of polynomials: Problem type 2
Simplifying a ratio of polynomials: Problem type 3
Simplifying a ratio of multivariate polynomials
Multiplying rational expressions involving multivariate monomials
Multiplying rational expressions involving quadratics with leading coefficients greater than 1
Multiplying rational expressions involving multivariate quadratics
Dividing rational expressions involving multivariate monomials
Dividing rational expressions involving quadratics with leading coefficients greater than 1
Dividing rational expressions involving multivariate quadratics
Multiplication and division of 3 rational expressions
Least common multiple of two monomials
Finding the LCD of rational expressions with linear denominators: Common factors
Finding the LCD of rational expressions with quadratic denominators
Writing equivalent rational expressions with monomial denominators
Writing equivalent rational expressions involving opposite factors
Adding rational expressions with denominators $a x^{n}$ and $b x^{m}$

- Adding rational expressions with multivariate monomial denominators: Basic
- Adding rational expressions with multivariate monomial denominators: Advanced

Adding rational expressions with linear denominators without common factors: Advanced
Adding rational expressions with linear denominators with common factors: Basic

- Adding rational expressions with linear denominators with common factors: Advanced

Adding rational expressions with denominators ax-b and b-ax
Adding rational expressions involving different quadratic denominators
Adding 3 rational expressions with different quadratic denominators
Complex fraction involving multivariate monomials
Complex fraction: Quadratic factoring
Complex fraction made of sums involving rational expressions: Problem type 2
Complex fraction made of sums involving rational expressions: Problem type 3
Complex fraction made of sums involving rational expressions: Problem type 4
Complex fraction made of sums involving rational expressions: Problem type 5
Complex fraction made of sums involving rational expressions: Problem type 6
Complex fraction made of sums involving rational expressions: Multivariate
Complex fraction with negative exponents: Problem type 1
Complex fraction with negative exponents: Problem type 2
Complex fraction that contains a complex fraction
Finding all square roots of a number
Square roots of integers raised to even exponents
Using absolute value to simplify square roots of perfect square monomials
Finding the $n^{\text {th }}$ root of a perfect $n^{\text {th }}$ power fraction
Finding the $\mathrm{n}^{\text {th }}$ root of a perfect $\mathrm{n}^{\text {th }}$ power monomial
Using absolute value to simplify higher radical expressions
Rational exponents: Unit fraction exponents and bases involving signs
Rational exponents: Product rule
Rational exponents: Quotient rule
Rational exponents: Products and quotients with negative exponents
Rational exponents: Power of a power rule
Rational exponents: Powers of powers with negative exponents
Simplifying the square root of a whole number greater than 100
Simplifying a radical expression with two variables
Introduction to simplifying a higher radical expression
Simplifying a higher radical expression: Univariate
Simplifying a higher radical expression: Multivariate
Square root addition or subtraction with three terms
Introduction to simplifying a sum or difference of radical expressions: Univariate
Simplifying a sum or difference of radical expressions: Univariate
Simplifying a sum or difference of radical expressions: Multivariate
Simplifying a sum or difference of higher roots
Simplifying a sum or difference of higher radical expressions
Simplifying a product of radical expressions: Univariate
Simplifying a product of radical expressions: Multivariate
Simplifying a product of radical expressions: Multivariate, fractional expressions
Introduction to simplifying a product of higher roots
Simplifying a product of higher radical expressions
Special products of radical expressions: Conjugates and squaring
Classifying sums and products as rational or irrational
Rationalizing a denominator: Quotient involving a monomial
Rationalizing a denominator using conjugates: Square root in numerator
Rationalizing a denominator using conjugates: Variable in denominator
Rationalizing a denominator: Quotient involving a higher radical
Rationalizing a denominator: Quotient involving higher radicals and monomials
Simplifying products or quotients of higher radicals with different indices: Univariate
Simplifying products or quotients of higher radicals with different indices: Multivariate
Area of a piecewise rectangular figure
Word problem involving the area between two rectangles
Area of a triangle
Area of a parallelogram
Area of a trapezoid
Perimeter involving rectangles and circles
Circumference and area of a circle
Circumference and area of a circle: Exact answers in terms of pi
Area involving rectangles and circles
Word problem involving the area between two concentric circles
Area involving inscribed figures
Volume of a triangular prism
Volume of a pyramid
Volume of a cylinder
Word problem involving the rate of filling or emptying a cylinder
Volume of a cone
Volume of a cone: Exact answers in terms of pi
Volume of a sphere

- Surface area of a cube or a rectangular prism
- Surface area of a triangular prism
- Surface area of a cylinder
- Surface area of a cylinder: Exact answers in terms of pi
- Surface area of a sphere
- Word problem involving the Pythagorean Theorem
- Equations and Inequalities (76 topics)
- Identifying properties used to solve a linear equation
- Solving equations with zero, one, or infinitely many solutions
- Solving a decimal word problem using a linear equation with the variable on both sides
- Solving a fraction word problem using a linear equation with the variable on both sides
- Solving a word problem involving consecutive integers
- Writing a multi-step equation for a real-world situation

Solving a value mixture problem using a linear equation
Finding a side length given the perimeter and side lengths with variables
Circumference ratios
Solving equations involving vertical angles

- Finding angle measures of a triangle given angles with variables

Finding the value for a new score that will yield a given mean
Finding the multiplier to give a final amount after a percentage increase or decrease
Finding the total cost including tax or markup
Finding the original price given the sale price and percent discount
Computing a percent mixture
Solving a percent mixture problem using a linear equation
Finding simple interest without a calculator
Converting a repeating decimal to a fraction
Solving an absolute value equation: Problem type 3
Solving an absolute value equation: Problem type 4
Solving an absolute value equation of the form |ax+b| = |cx+d|
Translating a sentence into a one-step inequality
Translating a sentence into a multi-step inequality
Writing an inequality for a real-world situation
Writing an inequality given a graph on the number line
Translating a sentence into a compound inequality
Writing a compound inequality given a graph on the number line
Writing sets of integers using set-builder and roster forms
Union and intersection of finite sets
Union and intersection of intervals
Additive property of inequality with signed fractions
Multiplicative property of inequality with signed fractions
Solving a two-step linear inequality with a fractional coefficient
Solving a linear inequality with multiple occurrences of the variable: Problem type 2
Solving a linear inequality with multiple occurrences of the variable: Problem type 3
Solving inequalities with no solution or all real numbers as solutions
Solving a compound linear inequality: Graph solution, basic
Solving a compound linear inequality: Interval notation
Solving a decimal word problem using a two-step linear inequality
Solving a decimal word problem using a linear inequality with the variable on both sides
Solving an absolute value inequality: Problem type 1
Writing an absolute value inequality given a graph on the number line
Solving an absolute value inequality: Problem type 2
Solving an absolute value inequality: Problem type 3
Solving an absolute value inequality: Problem type 4
Solving an absolute value inequality: Problem type 5
Solving a proportion of the form $\mathrm{a} /(\mathrm{x}+\mathrm{b})=\mathrm{c} / \mathrm{x}$
Solving for a variable in terms of other variables in a rational equation: Problem type 3
Word problem on proportions: Problem type 1
Word problem on proportions: Problem type 2
Similar polygons
Similar right triangles
Indirect measurement
Ratio of volumes
Word problem involving multiple rates
Solving a work problem using a rational equation
Solving a distance, rate, time problem using a rational equation
Ordering fractions with variables
Simplifying a product and quotient involving square roots of negative numbers
Simplifying a power of i
Using the Pythagorean Theorem and a quadratic equation to find side lengths of a right triangle
Discriminant of a quadratic equation with a parameter
Solving a rational equation that simplifies to quadratic: Proportional form, basic
Solving a rational equation that simplifies to quadratic: Factorable quadratic denominator

- Solving a rational equation that simplifies to quadratic: Proportional form, advanced
- Solving a radical equation with a quadratic expression under the radical
- Solving a radical equation with two radicals that simplifies to $\operatorname{sqrt}(x)=$ a
- Solving a radical equation that simplifies to a quadratic equation: Two radicals
- Word problem involving radical equations: Basic
- Word problem involving radical equations: Advanced
- Solving an equation with exponent 1/a: Problem type 1
- Solving an equation with exponent 1/a: Problem type 2
- Solving an equation with a positive rational exponent
- Solving an equation with a negative rational exponent
- Solving an equation that can be written in quadratic form: Problem type 2
- Graphs and Functions (61 topics)
- Finding the area of a triangle or parallelogram in the coordinate plane
- Distance between two points in the plane: Decimal answers
- Identifying scalene, isosceles, and equilateral triangles given coordinates of their vertices
- Finding an endpoint of a line segment given the other endpoint and the midpoint
- Graphing a line given its $x$ - and $y$-intercepts
- Testing an equation for symmetry about the axes and origin
- Classifying slopes given graphs of lines
- Finding the coordinate that yields a given slope
- Graphing a line through a given point with a given slope
- Identifying linear equations: Advanced
- Identifying linear functions given ordered pairs
- Rewriting a linear equation in the form $A x+B y=C$
- Writing an equation and graphing a line given its slope and y-intercept
- Finding the slope, y-intercept, and equation for a linear function given a table of values
- Graphing a line given its equation in point-slope form
- Writing the equation of a line in standard form given the slope and a point
- Comparing linear functions to the parent function $y=x$
- Identifying parallel and perpendicular lines from equations
- Identifying parallel and perpendicular lines from coordinates
- Identifying coordinates that give right triangles
- Graphing ordered pairs and writing an equation from a table of values in context
- Finding the initial amount and rate of change given a table for a linear function
- Combining functions to write a new function that models a real-world situation
- Comparing properties of linear functions given in different forms
- Application problem with a linear function: Finding a coordinate given the slope and a point
- Solving a linear equation by graphing
- Constructing a scatter plot
- Sketching the line of best fit
- Scatter plots and correlation
- Predictions from the line of best fit
- Approximating the equation of a line of best fit and making predictions
- Computing residuals
- Interpreting residual plots
- Classifying linear and nonlinear relationships from scatter plots
- Linear relationship and the correlation coefficient
- Identifying outliers and clustering in scatter plots
- Finding outliers in a data set
- Identifying solutions to a system of linear equations
- Graphically solving a system of linear equations
- Using a graphing calculator to solve a system of linear equations: Basic
- Using a graphing calculator to solve a system of linear equations: Advanced
- Writing a system of linear equations given its graph
- Solving a system of linear equations using substitution
- Solving a system of linear equations using elimination with addition
- Solving a system of linear equations using elimination with multiplication and addition
- Identifying the center and radius to graph a circle given its equation in general form: Advanced
- Writing an equation of a circle and identifying points that lie on the circle
- Deriving the equation of a circle using the Pythagorean Theorem

Domains of higher root functions

- Domain and range of a linear function that models a real-world situation
- Rewriting a multivariate function as a univariate function given a relationship between its variables

Domain and range from the graph of a discrete relation
Finding domain and range from a linear graph in context
Choosing a graph to fit a narrative: Basic
Choosing a graph to fit a narrative: Advanced
Graphing an integer function and finding its range for a given domain
Graphing a square root function: Problem type 3
Graphing a cube root function
Writing the equation of a secant line
How the leading coefficient affects the graph of an absolute value function
Composition of two functions: Domain and range

- Polynomial and Rational Functions (27 topics)
- Graphing a parabola of the form $y=a x^{2}+b x+c$ : Rational coefficients
- Rewriting a quadratic function in standard form
- Solving a quadratic equation by graphing
- Comparing properties of quadratic functions given in different forms
- Classifying the graph of a function
- Choosing a quadratic model and using it to make a prediction
- Identifying polynomial functions
- Dividing a polynomial by a monomial: Univariate
- Dividing a polynomial by a monomial: Multivariate
- Remainder theorem: Advanced
- Closure properties of integers and polynomials
- Descartes' Rule of Signs
- Using the conjugate zeros theorem to find all zeros of a polynomial
- Linear factors theorem and conjugate zeros theorem
- Writing the equation of a rational function given its graph

Identifying direct variation equations
Identifying direct variation from ordered pairs and writing equations
Writing a direct variation equation
Word problem on direct variation
Interpreting direct variation from a graph
Writing an inverse variation equation
Identifying direct and inverse variation equations
Identifying direct and inverse variation from ordered pairs and writing equations
Word problem on inverse variation
Word problem on inverse variation involving the completion of a task

- Writing an equation that models variation
- Word problem on combined variation
- Exponential and Logarithmic Functions (12 topics)

Finding domain and range from the graph of an exponential function
Calculating and comparing simple interest and compound interest
Finding the initial amount and rate of change given an exponential function
Writing an equation that models exponential growth or decay
Writing an exponential function rule given a table of ordered pairs
Choosing an exponential model and using it to make a prediction
Comparing linear, polynomial, and exponential functions
Graphing a logarithmic function: Advanced
Expanding a logarithmic expression: Problem type 3
Change of base for logarithms: Problem type 2
Solving an exponential equation by finding common bases: Linear and quadratic exponents
Solving an exponential equation by using substitution and quadratic factoring

- Trigonometric Functions (38 topics)

Converting degrees-minutes-seconds to decimal degrees
Converting decimal degrees to degrees-minutes-seconds
Sketching an approximation of an angle given in radians
Sketching an angle in standard position given in degrees and finding a coterminal angle
Sketching an angle in standard position given in radians and finding a coterminal angle
Sketching an angle with absolute value greater than 360 degrees in standard position
Sketching an angle with absolute value greater than $2 \pi$ radians in standard position
Sketching an angle with absolute value greater than 360 degrees and finding coterminal angles
Sketching an angle with absolute value greater than $2 \pi$ radians and finding coterminal angles
Drawing an arc to find a central angle or an arc length on the unit circle
Drawing an arc to find a central angle or an arc length on a non-unit circle
Relating an angle and an arc length in a real-world situation
Relating two angle measures in a real-world situation that involves interlocking gears
Area of a sector of a circle
Using the area formula for a sector of a circle in a real-world situation
Angular and linear speed
Finding a point on the unit circle given one coordinate and the quadrant
Drawing a reference triangle on the unit circle and using it to derive values of trigonometric functions: Degrees
Using symmetries on the unit circle to understand trigonometric identities: Problem type 1
Using the unit circle to understand that sine and cosine are periodic
Using symmetries on the unit circle to understand trigonometric identities: Problem type 2
Simplifying a trigonometric expression: Rationalizing the denominator using conjugates
Using a calculator to approximate cosecant, secant, and cotangent values
Special right triangles: Exact answers
Sine, cosine, and tangent ratios: Numbers for side lengths
Understanding trigonometric ratios through similar right triangles
Relationship between the sines and cosines of complementary angles
Using similar right triangles to find trigonometric ratios
Word problem involving a triangle whose side lengths change with time: Problem type 1
Word problem involving a triangle whose side lengths change with time: Problem type 2

- Using trigonometry to find lengths in a figure involving two right triangles
- Sketching an angle with absolute value greater than 360 degrees, and also its reference angle
- Using graphing to solve a trigonometric equation involving sine or cosine
- Average rate of change involving a sinusoidal function
- Understanding how changes to the amplitude, period, phase shift, and vertical shift affect a sinusoidal graph Sketching the graph of a sinusoidal function that models a real-world situation and using the graph to approximate
- solutions to an equation
- Sketching a graph of a damped sine or cosine function
- Composition of trigonometric functions with variable expressions as inputs: Problem type 2
- Trigonometric Identities and Equations (20 topics)
- Proving an identity using fundamental trigonometric identities: Problem type 8
- Proving trigonometric identities using odd and even identities
- Proving identities involving trigonometric functions and logarithmic functions
- Using a double-angle identity to find the exact value of a composition of trigonometric functions
- Double-angle identities: Problem type 3

Proving trigonometric identities using sum-to-product identities: Problem type 1

- Proving trigonometric identities using sum-to-product identities: Problem type 2

Finding solutions in an interval for an equation involving a trigonometric expression and either exponentials or
logarithms
Using a Pythagorean identity to find solutions in an interval for a trigonometric equation involving sine and cosine:
Problem type 2
Using a Pythagorean identity to find solutions in an interval for a trigonometric equation: Problem type 2
Using a graphing calculat or to solve a trigonometric equation
Using a graphing calculat or to solve a trigonometric inequality
Solving a trigonometric equation involving a squared function: Problem type 1
Solving a trigonometric equation involving a squared function: Problem type 2
Solving a trigonometric equation involving more than one function
Solving a trigonometric equation involving an angle multiplied by a constant
Finding solutions in an interval for a trigonometric equation involving sine and cosine using sum and difference identities
Solving a trigonometric equation using sum and difference identities
Solving a trigonometric equation using double-angle identities
Solving a trigonometric equation using half-angle identities

- Additional Topics in Trigonometry (60 topics)
- Proving the law of sines

Proving the law of cosines
Using trigonometry to find the area of a right triangle
Using trigonometry to find the area of a triangle
Expressing the area of a triangle in terms of the sine of one of its angles
Heron's formula
Writing a position vector in ai+bj form given its graph
Writing a vector in ai+bj form given its initial and terminal points
Writing a vector in component form given its initial and terminal points
Magnitude of a vector given in ai+bj form
Magnitude of a vector given in component form
Vector addition and scalar multiplication: ai+bj form
Linear combination of vectors: ai+bj form
Vector addition and scalar multiplication: Component form
Linear combination of vectors: Component form
Unit vectors
Multiplication of a vector by a scalar: Geometric approach
Vector addition: Geometric approach
Vector subtraction: Geometric approach
Finding the magnitude and direction of a vector given its graph
Finding the components of a vector given its graph
Finding the direction angle of a vector given in ai+bj form
Writing a vector given its magnitude and direction angle
Writing a vector to represent a force pushing or pulling an object
Finding the magnitude and direction angle of the resultant force of two vectors
Finding magnitudes of forces related to a sum of three vectors
Finding magnitudes of forces related to an object suspended by cables
Dot product of vectors given in ai+bj form
Dot product of vectors given in component form
Finding the angle between two vectors given in component form
Classifying vector relationships by finding the angle between two vectors given in ai + bj form
Using the dot product to find perpendicular vectors
Finding the component of a vector along another vector
Decomposing a vector into two orthogonal vectors
Finding the amount of work done given a force vector and a distance
Finding magnitudes of forces related to an object on a ramp
Plotting points in polar coordinates
Multiple representations of polar coordinates
Converting rectangular coordinates to polar coordinates: Special angles

- Converting rectangular coordinates to polar coordinates: Decimal answers
- Converting polar coordinates to rectangular coordinates
- Converting an equation written in rectangular form to one written in polar form

Converting an equation written in polar form to one written in rectangular form: Problem type 1

- Converting an equation written in polar form to one written in rectangular form: Problem type 2

Graphing a polar equation: Basic
Graphing a polar equation: Circle
Graphing a polar equation: Limacon
Graphing a polar equation: Rose
Graphing a polar equation: Lemniscate
Matching polar equations with their graphs
Identifying symmetries of graphs given their polar equations
Plotting complex numbers
Writing a complex number in standard form given its trigonometric form
Writing a complex number in trigonometric form: Special angles
Writing a complex number in trigonometric form: Decimal answers
Multiplying and dividing complex numbers in trigonometric form
De Moivre's Theorem: Answers in trigonometric form
De Moivre's Theorem: Answers in standard form
Finding the nth roots of a number: Problem type 1
Finding the nth roots of a number: Problem type 2

- Systems of Equations and Matrices (72 topics)

Classifying systems of linear equations from graphs
Solving a system of linear equations with fractional coefficients
Solving a system of linear equations with decimal coefficients
Solving a $2 \times 2$ system of linear equations that is inconsistent or consistent dependent
Creating an inconsistent system of linear equations
Identifying the operations used to create equivalent systems of equations
Consistency and independence of a system of linear equations
Interpreting the graphs of two functions
Solving a word problem involving a sum and another basic relationship using a system of linear equations
Solving a word problem using a system of linear equations of the form $A x+B y=C$
Solving a word problem using a system of linear equations of the form $y=m x+b$
Solving a value mixture problem using a system of linear equations
Solving a percent mixture problem using a system of linear equations
Solving a distance, rate, time problem using a system of linear equations
Solving a tax rate or interest rate problem using a system of linear equations
Introduction to solving a $3 \times 3$ system of linear equations
Solving a $3 \times 3$ system of linear equations: Problem type 1
Solving a $3 \times 3$ system of linear equations: Problem type 2
Solving a $3 \times 3$ system of linear equations that is inconsistent or consistent dependent
Solving a word problem using a $3 \times 3$ system of linear equations: Problem type 1
Solving a word problem using a $3 \times 3$ system of linear equations: Problem type 2
Scalar multiplication of a matrix
Addition or subtraction of matrices
Linear combination of matrices
Squaring and multiplying $2 \times 2$ matrices
Multiplication of matrices: Basic
Multiplication of matrices: Advanced
Word problem involving multiplication of matrices
Finding the inverse of a $2 \times 2$ matrix
Finding the inverse of a $3 \times 3$ matrix
Finding the determinant of a $2 \times 2$ matrix
Finding the determinant of a $3 \times 3$ matrix
Completing Gauss-Jordan elimination with a $2 \times 2$ matrix
Gauss-Jordan elimination with a $2 \times 2$ matrix
Writing solutions to $3 \times 3$ systems of linear equations from augmented matrices
Completing Gauss-Jordan elimination with a $3 \times 3$ matrix
Solving a system of linear equations given its augmented matrix
Finding the inverse of a matrix to solve a $2 \times 2$ system of linear equations
Using the inverse of a matrix to solve a $3 \times 3$ system of linear equations
Using Cramer's rule to solve a $2 \times 2$ system of linear equations
Using Cramer's rule to solve a $3 \times 3$ system of linear equations
Introduction to partial fraction decomposition with distinct linear factors
Partial fraction decomposition with distinct linear factors
Partial fraction decomposition with repeated linear factors
Partial fraction decomposition with an irreducible quadratic factor
Partial fraction decomposition with repeated, irreducible quadratic factors
Graphically solving a system of linear and quadratic equations
Using a graphing calculator to solve a nonlinear system of equations: Basic
Using a graphing calculat or to solve a nonlinear system of equations: Advanced
Using a graphing calculator to solve an exponential or logarithmic equation
Solving a system of linear and quadratic equations

- Solving a system of nonlinear equations: Problem type 1
- Solving a system of nonlinear equations: Problem type 2
- Solving a word problem involving geometry using a system of nonlinear equations
- Identifying solutions to a linear inequality in two variables
- Graphing a linear inequality in the plane: Vertical or horizontal line
- Graphing a linear inequality in the plane: Slope-intercept form
- Graphing a linear inequality in the plane: Standard form
- Writing an inequality given its graph in the plane: Horizontal or vertical boundary line
- Writing an inequality given its graph in the plane: Slanted boundary line
- Graphing a quadratic inequality: Problem type 1
- Graphing a quadratic inequality: Problem type 2
- Graphing an inequality involving a circle
- Graphing a system of two linear inequalities: Basic
- Graphing a system of two linear inequalities: Advanced
- Graphing a system of three linear inequalities
- Graphing a system of nonlinear inequalities: Problem type 1
- Writing a multi-step inequality for a real-world situation
- Solving a word problem using a system of linear inequalities: Problem type 1
- Solving a word problem using a system of linear inequalities: Problem type 2
- Linear programming
- Solving a word problem using linear programming
- Conic Sections (38 topics)
- Graphing a parabola of the form $y^{2}=a x$ or $x^{2}=a y$

Graphing a parabola of the form $x=a(y-k)^{2}+h$ or $y=a(x-h)^{2}+k$
Graphing a parabola of the form $a y^{2}+b y+c x+d=0$ or $a x^{2}+b x+c y+d=0$
Writing an equation of a parabola given the vertex and the focus
Writing an equation of a parabola given the focus and the directrix

- Deriving the equation of a parabola given its focus and directrix
- Finding the vertex, focus, directrix, and axis of symmetry of a parabola

Finding the focus of a parabola of the form $a y^{2}+b y+c x+d=0$ or $a x^{2}+b x+c y+d=0$
Writing an equation of a parabola given its graph
Word problem involving a parabola
Graphing an ellipse given its equation in standard form
Graphing an ellipse centered at the origin: $A x^{2}+B y^{2}=C$
Graphing an ellipse given its equation in general form
Finding the center, vertices, and foci of an ellipse
Finding the foci of an ellipse given its equation in general form
Writing an equation of an ellipse given the center, an endpoint of an axis, and the length of the other axis
Writing an equation of an ellipse given the foci and the major axis length
Graphing a system of nonlinear inequalities: Problem type 2
Word problem involving an ellipse
Graphing a hyperbola given its equation in standard form
Graphing a hyperbola centered at the origin: $A x^{2}+B y^{2}=C$
Graphing a hyperbola given its equation in general form
Finding the center, vertices, foci, and asymptotes of a hyperbola
Finding the foci of a hyperbola given its equation in general form
Writing an equation of a hyperbola given the foci and the vertices
Writing an equation of a hyperbola given the foci and the asymptotes: Basic
Writing an equation of a hyperbola given the foci and the asymptotes: Advanced
Classifying conics given their equations
Completing a table and choosing a graph given a pair of parametric equations
Writing the equation of a line and sketching its graph given its parametric equations
Writing the equation of a parabola and sketching its graph given its parametric equations
Writing the equation of a circle or ellipse and sketching its graph given its parametric equations
Graphing a pair of parametric equations with a restricted domain: Line or parabola
Graphing a pair of parametric equations with a restricted domain: Circle
Graphing a pair of parametric equations with a restricted domain: Ellipse
Completing pairs of parametric equations
Word problem involving parametric equations for projectile motion: Problem type 1

- Word problem involving parametric equations for projectile motion: Problem type 2
- Sequences, Series, and Probability (67 topics)

Finding the first terms of an arithmetic sequence using an explicit rule
Finding the first terms of a geometric sequence using an explicit rule
Finding the first terms of a sequence using an explicit rule with multiple occurrences of $n$
Finding the next terms of an arithmetic sequence with integers
Finding the first terms of a sequence using a recursive rule
Identifying arithmetic sequences and finding the common difference
Finding a specified term of an arithmetic sequence given the first terms
Finding a specified term of an arithmetic sequence given the common difference and first term
Finding a specified term of an arithmetic sequence given two terms of the sequence
Writing an explicit rule for an arithmetic sequence

- Writing a recursive rule for an arithmetic sequence
- Sum of the first $n$ terms of an arithmetic sequence

Finding the next terms of a geometric sequence with signed numbers
Identifying arithmetic and geometric sequences
Identifying geometric sequences and finding the common ratio
Finding a specified term of a geometric sequence given the first terms
Finding a specified term of a geometric sequence given the common ratio and first term
Finding a specified term of a geometric sequence given two terms of the sequence
Arithmetic and geometric sequences: Identifying and writing an explicit rule
Writing recursive rules for arithmetic and geometric sequences
Sum of the first $n$ terms of a geometric sequence
Sum of an infinite geometric series
Identifying linear, quadratic, and exponential functions given ordered pairs
Factorial expressions
Interpreting a tree diagram
Introduction to the counting principle
Counting principle
Computing permutations and combinations
Introduction to permutations and combinations
Permutations and combinations: Problem type 1
Permutations and combinations: Problem type 2
Permutations and combinations: Problem type 3
Binomial formula
Determining a sample space and outcomes for an event: Experiment involving a single selection
Determining a sample space and outcomes for an event: Experiment involving multiple selections
Probability involving one die or choosing from $n$ distinct objects
Probability involving choosing from objects that are not distinct
Experimental and theoretical probability
Outcomes and event probability
Probabilities of a permutation and a combination
Area as probability
Probability of independent events: Decimal answers
Probability of dependent events: Decimal answers
Probabilities of draws with replacement
Probabilities of draws without replacement
Interpreting a Venn diagram of 2 sets
Interpreting a Venn diagram of 3 sets
Introduction to shading a Venn diagram with 2 events
Shading a Venn diagram with 2 events: Unions, intersections, and complements
Shading a Venn diagram with 3 sets to represent a group
Probabilities involving two rolls of a die
Determining outcomes for unions, intersections, and complements of events
Using a Venn diagram to understand the addition rule for probability
Outcomes and event probability: Addition rule
Word problem involving the probability of a union or an intersection
Identifying independent events given values of probabilities
Probability of the union and intersection of independent events
Probability of the union of mutually exclusive events and independent events
Using a Venn diagram to understand the multiplication rule for probability
Outcomes and event probability: Conditional probability
Computing conditional probability using a two-way frequency table
Computing conditional probability to make an inference using a two-way frequency table
Conditional probability: Basic
Intersection and conditional probability
Binomial problems: Basic
Binomial problems: Advanced
Using a random number table to make a fair decision

- Limits and Continuity (15 topics)
- Estimating a limit numerically

Finding limits from a graph
Finding a limit by using the limit laws: Problem type 1
Finding limits for a piecewise-defined function
Finding a limit by using the limit laws: Problem type 2
Finding a limit by using the limit laws: Problem type 3
Squeeze Theorem
Determining points of discontinuity from a graph
Determining a parameter to make a function continuous
Infinite limits and graphs
Limits at infinity and graphs
Limits at infinity and rational functions
Infinite limits and rational functions
Finding a limit of a trigonometric function by using continuity
Finding a limit by using special trigonometric limits
*Other Topics Available By default, these topics are NOT included in the course, but can be added using the content editor in the Teacher Module.

